

Seeds of axion miniclusters

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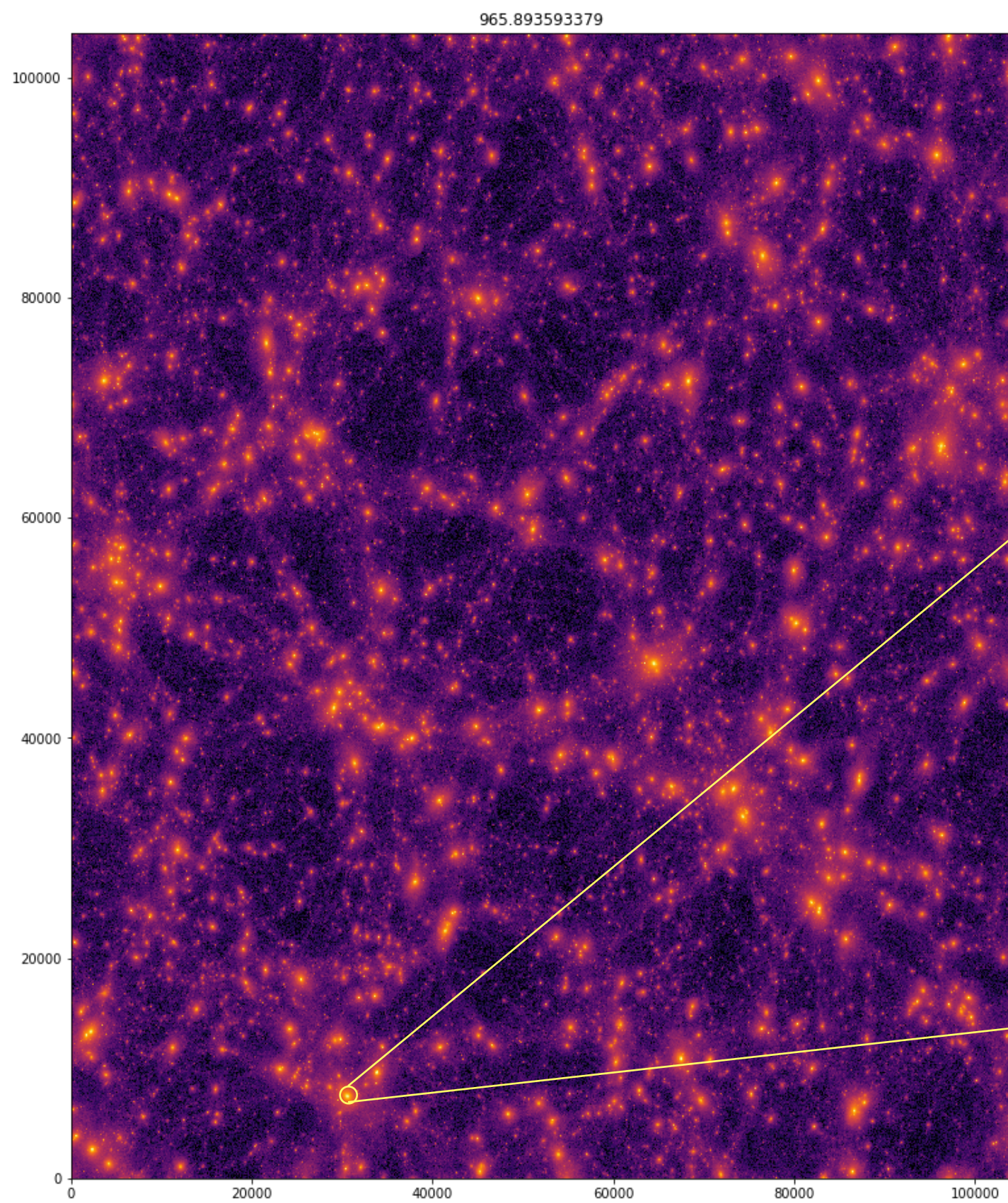


Dep. Theoretical Physics
Universidad de Zaragoza

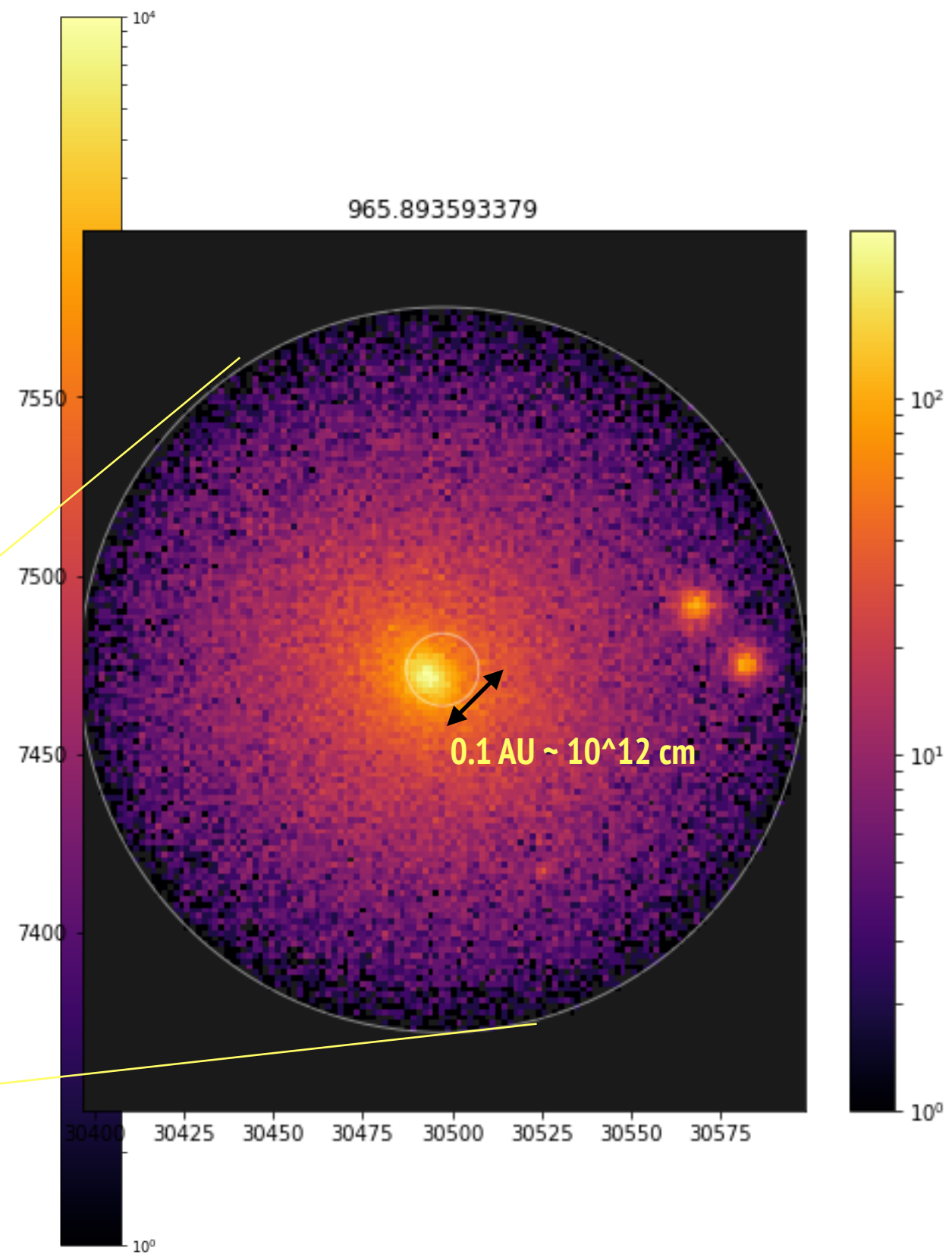


MAX-PLANCK-GESELLSCHAFT

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comoving scale [AU]~ 1000 AU



Storyline

- **Intro: Axions and ALPs**
- **(QCD) Axion dark matter in the post-inflationary scenario**
- **Seeds of axion miniclusters (Sim 1)**
- **Gravitational evolution (Sim 2)**

Axions

- Motivated by the strong CP problem, $\mathcal{L}_{\text{SM}} \in -\frac{\alpha_s}{8\pi} \text{tr}\{G_{a\mu\nu} \tilde{G}_a^{\mu\nu}\} \theta$ why are nuclear EDMs sooo small?

- Why is $\theta < 10^{-10}$?

- Peccei-Quinn, if theta is a field implies $\theta = 0$ Peccei, Quinn, Weinberg, Wilczek 1978

Axion field = Goldstone boson of a new Global Spontaneously-broken colour-anomalous U(1) symmetry = θ

- QCD Axion and axion-like particles fit BSM (pseudo Nambu-Goldstone bosons, stringy axions...)

- Low-energy effective action is restricted by U(1) shift symmetry $a \rightarrow a + \text{ct.}$

$$\mathcal{L}_a = \frac{1}{2} (\partial_\mu a) (\partial^\mu a) + \sum_f g_{af} [\bar{f} \gamma^\mu \gamma_5 f] \frac{\partial_\mu a}{m_f} - \frac{g_{a\gamma}}{4} F_{\mu\nu} \tilde{F}^{\mu\nu} a - C_{ag} \frac{\alpha_s}{8\pi} \{G_{i\mu\nu} \tilde{G}_i^{\mu\nu}\} \frac{a}{f_a}$$

$$g_{ai} \propto \frac{C_{ai} \sim O(1)}{f_a} \begin{array}{l} \longrightarrow \text{O(1) model-dependent parameters} \\ \longrightarrow \text{new energy scale (decay constant)} \end{array}$$

Shift-symmetry breaking corrections can generate a small mass + ...

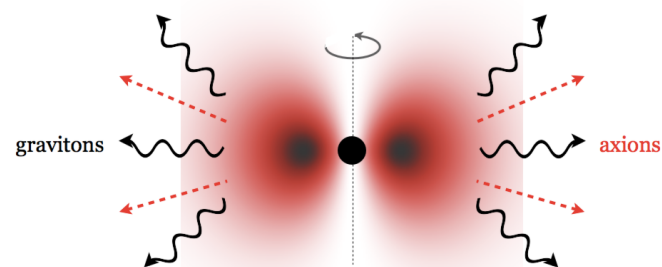
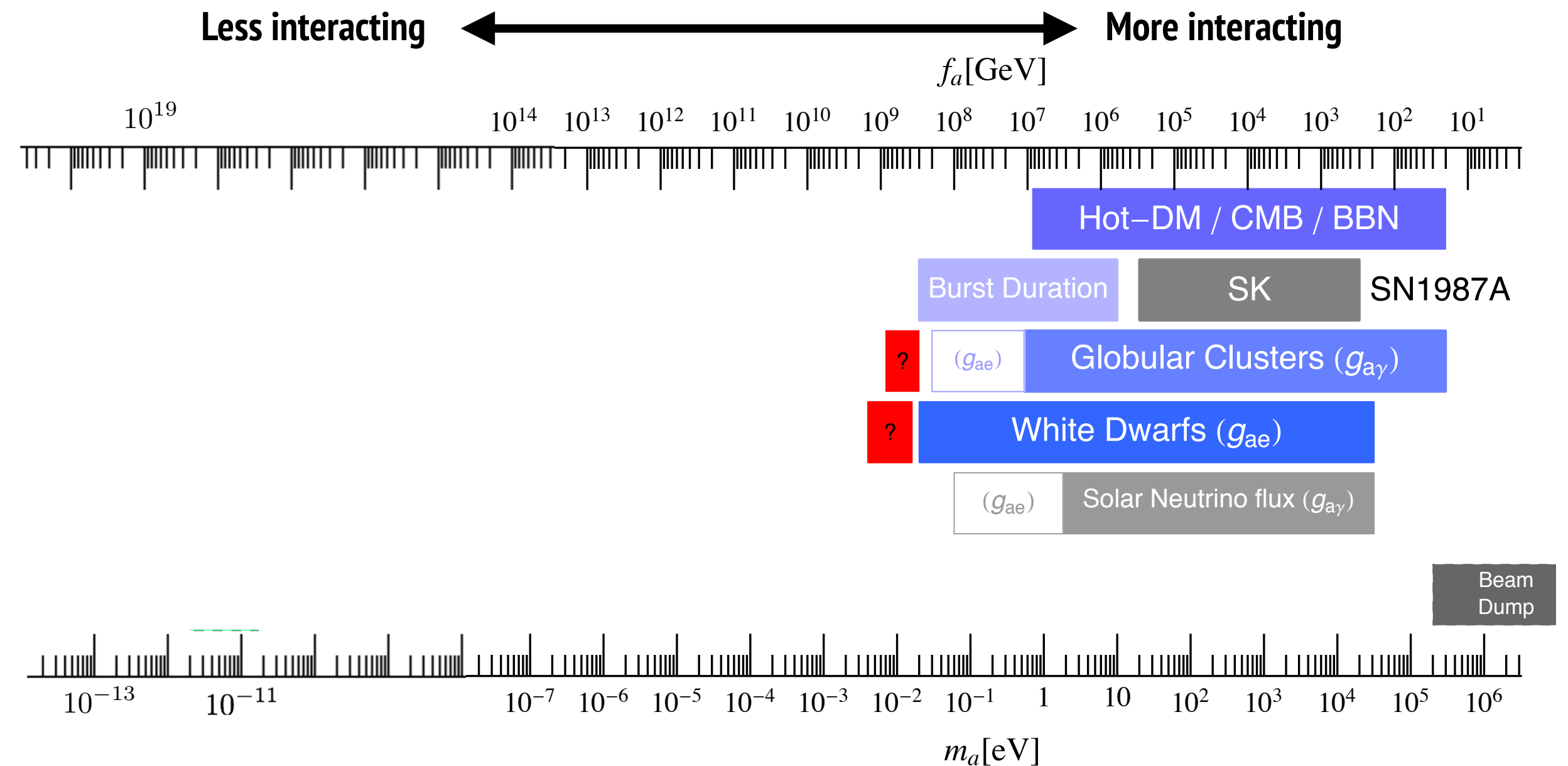
$$\mathcal{L}_a \ni -\frac{1}{2} m_a^2 a^2 \dots$$

If C_{ag} is non-zero, you ALP is the QCD axion $\frac{a(x)}{f_a} \equiv \theta(x)$

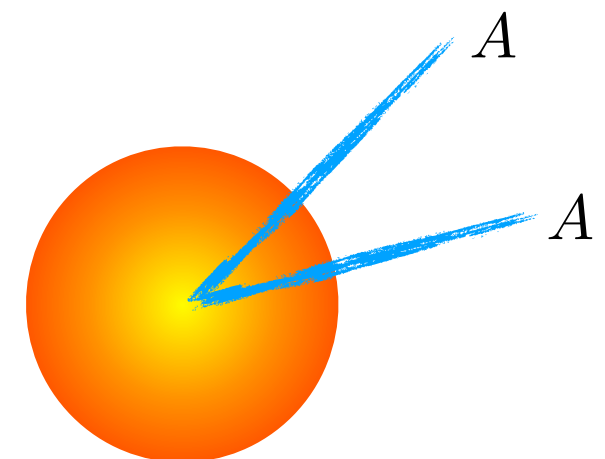
At low-energies $V_{\text{QCD}}(\theta) \sim \chi(1 - \cos \theta)$

$$m_A = \frac{\sqrt{\chi}}{f_A} \sim 60 \mu\text{eV} \frac{10^{12} \text{GeV}}{f_a}$$

what do we know about f_A ?

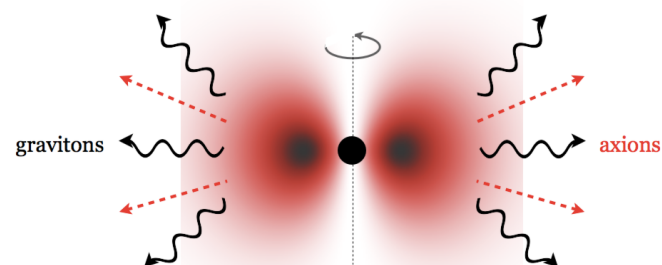
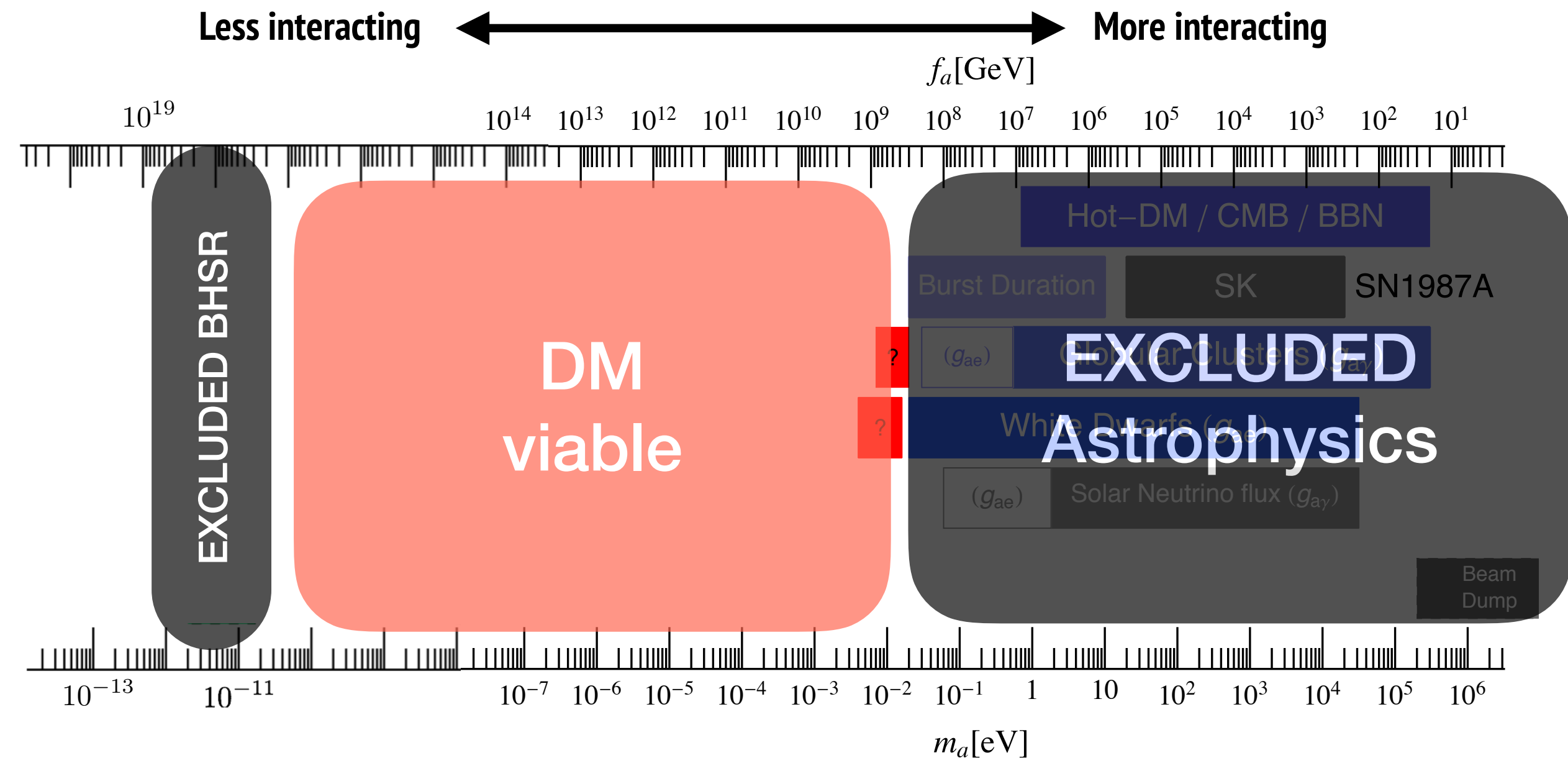


Black hole spin radiated

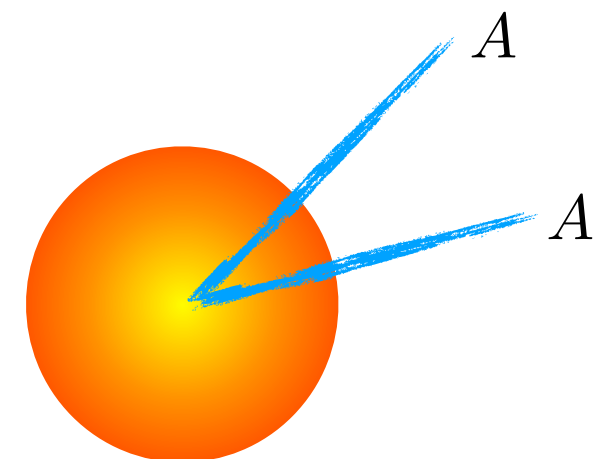


Stellar evolution accelerated*

what do we know about f_A ?



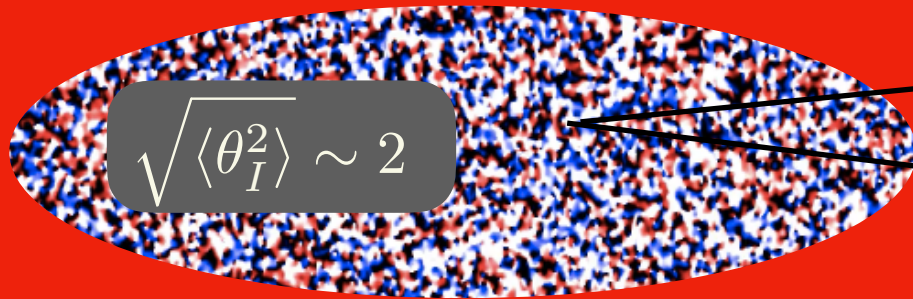
Black hole spin radiated



Stellar evolution accelerated*

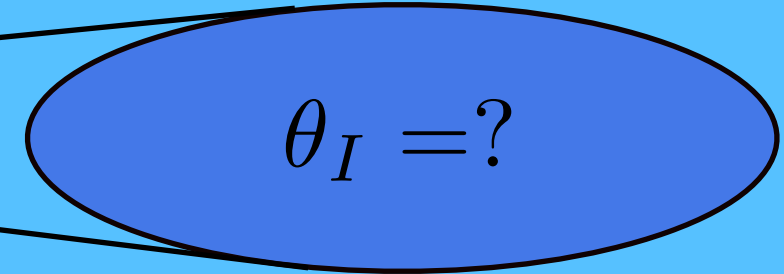
Axion dark matter in a nutshell

5: Scenario B : Initial conditions after inflation



dark matter inhomogeneous at scales below $\sim \text{pc}$

6: Scenario A : Inflation AFTER initial conditions



dark matter homogeneous

4: Axion dark matter abundance depends:

- Axion mass
- Initial angle

$$\Omega_c h^2 \sim 0.12 \theta_I^2 \left(\frac{10 \mu\text{eV}}{m_A} \right)^{1.17}$$

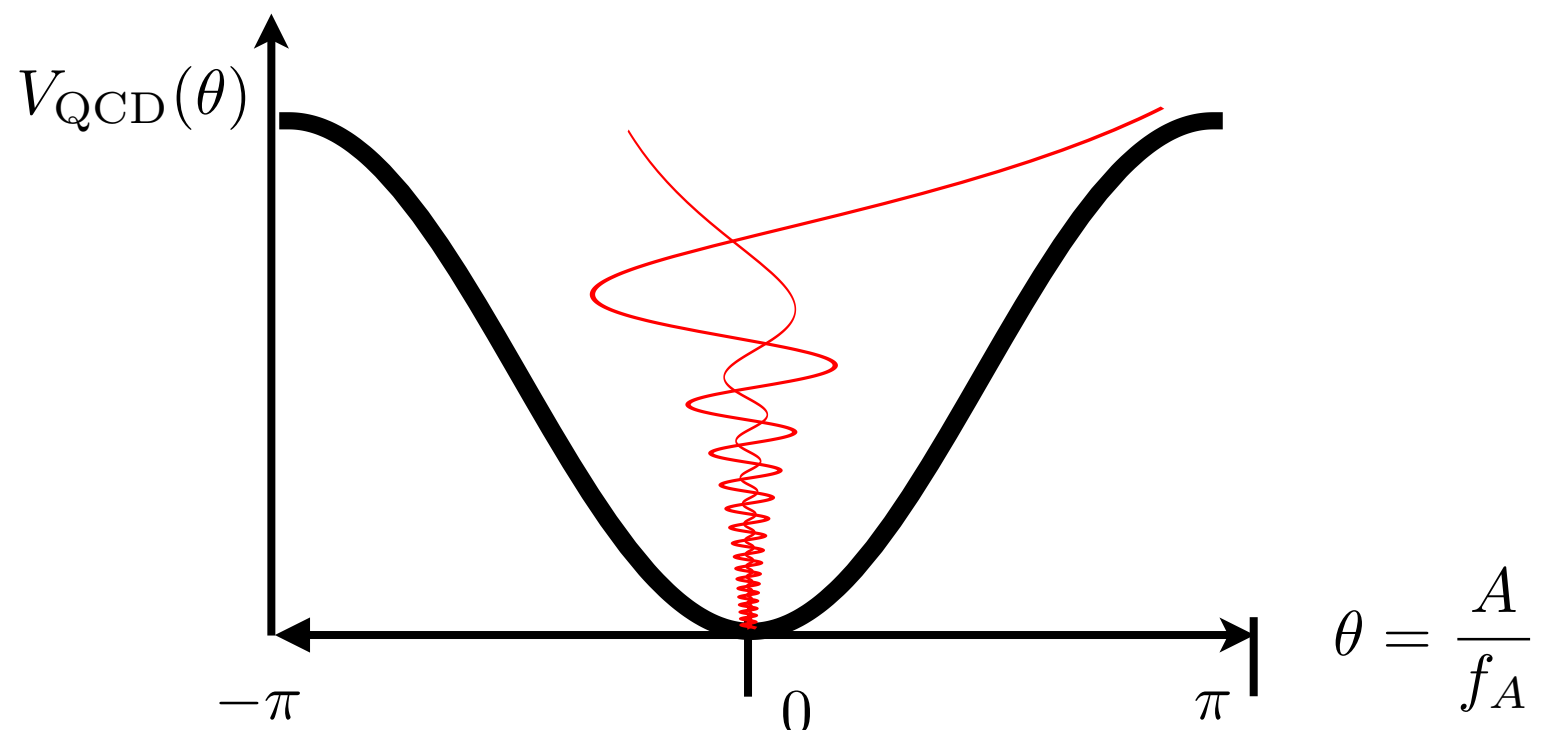
3: Axions field rolls down potential at

$$t_{\text{osc}} \sim 1/m_A$$

and becomes dark matter (like inflaton)

2: The QCD vacuum energy depends on θ
it has a minimum at $\theta = 0$!!!!

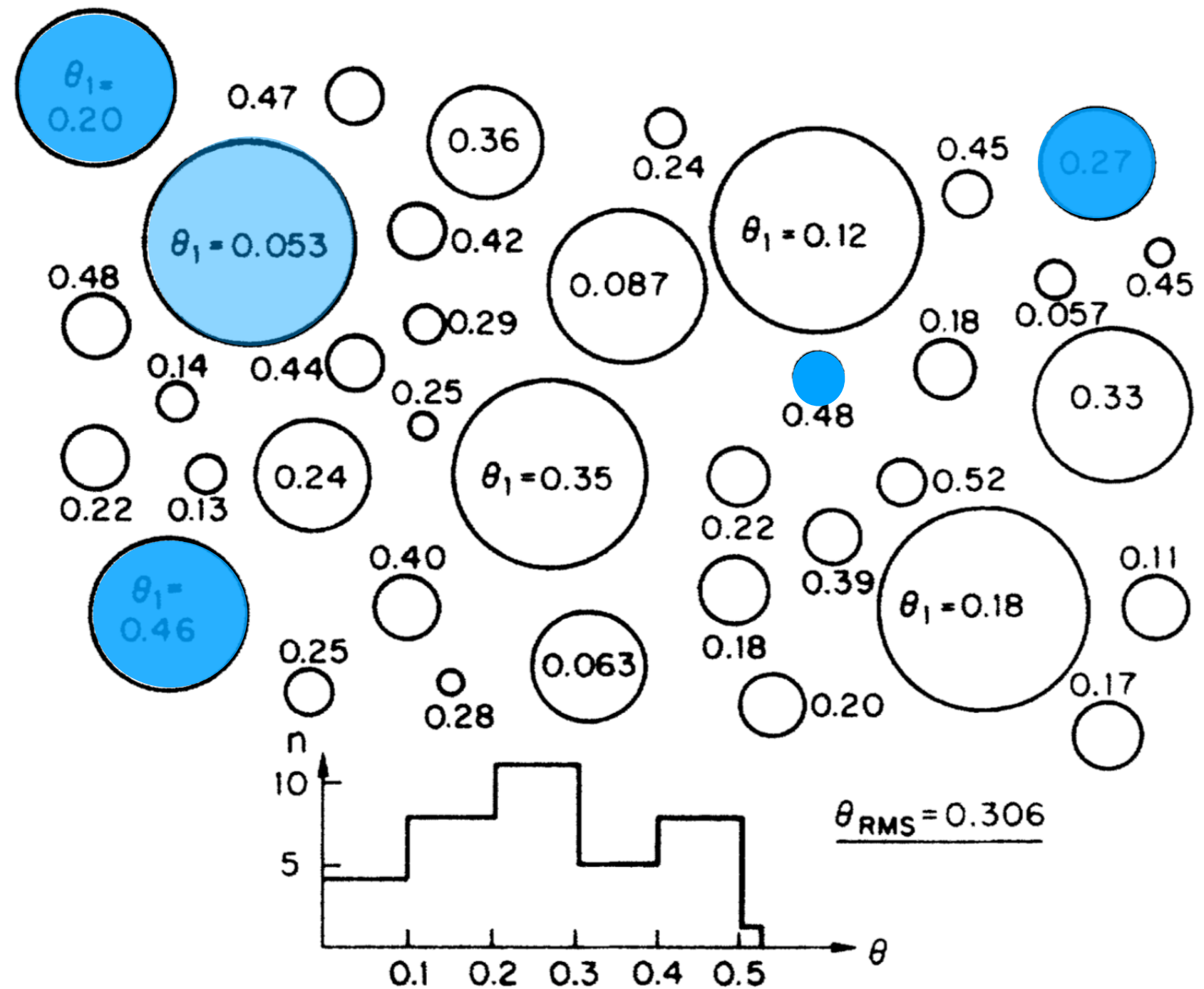
1: The axion field (A) is the dynamical
version of the theta angle of QCD
We observe $\theta \simeq 0$



post-inflationary scenario

After the Phase transition, initial misalignment angle is different in causally disconnected regions of the Universe

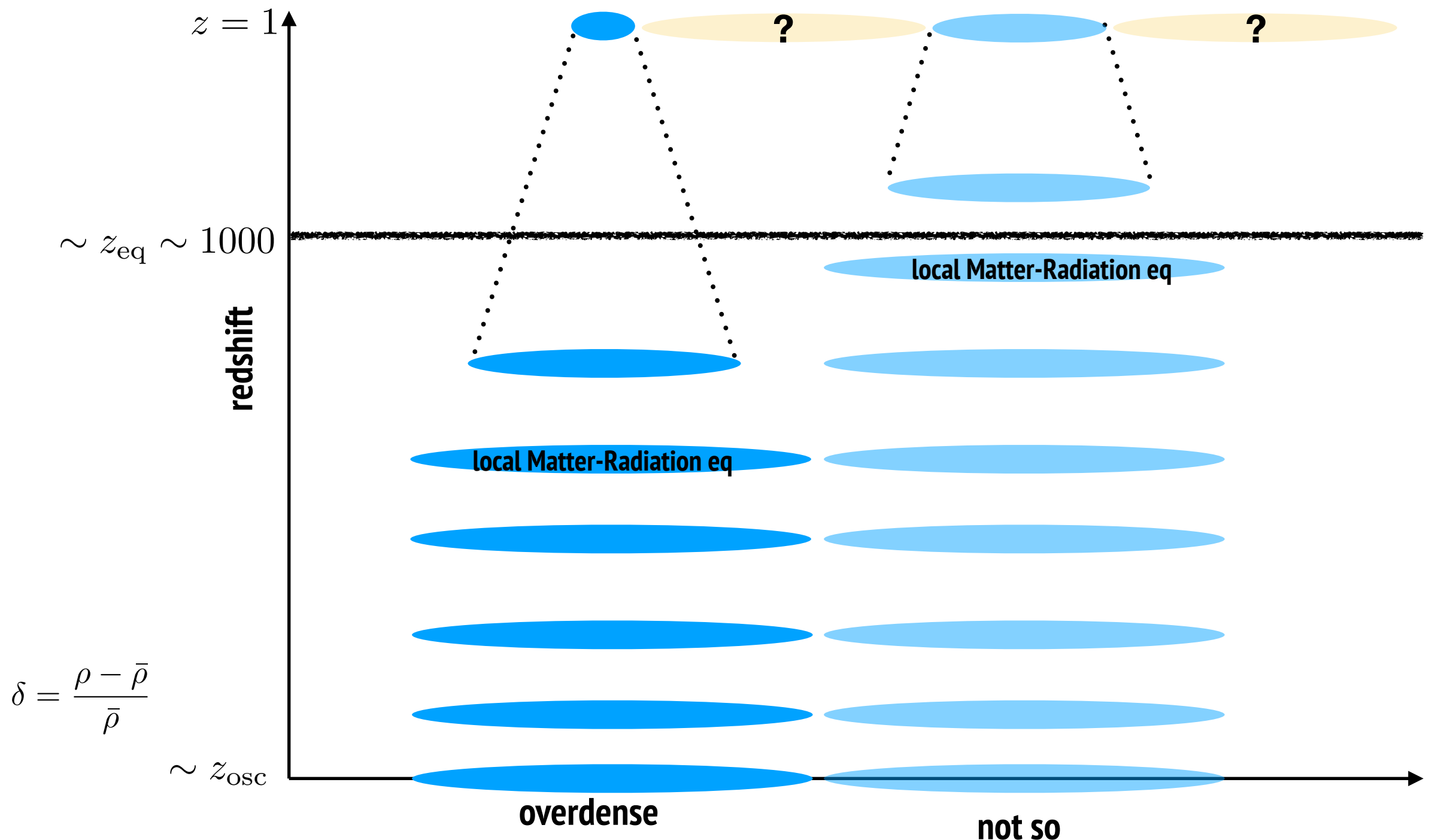
$$\rho_{\text{DM}} \propto \theta_i^2$$



miniclusters

DM distribution is frozen shortly after T_1 : the density field expands with the Universe

Regions with overdensity δ collapse gravitationally at $z_{\text{col}} \sim z_{\text{eq}} \delta$ (keep a fixed size)



miniclusters

Kolb-Tkachev, properties determined by δ

$$R_{mc} \sim L_1 / (z_{eq} \delta) \\ \sim 10^{12} \text{cm}$$

$$M \sim (1 + \delta) M_0 \\ \frac{4\pi}{3} R_{mc}^3 \rho_{DM} \sim 10^{-12} M_\odot$$

$$\rho \sim \rho_{eq} \delta^3 (1 + \delta) \\ \sim 10^{-12} \text{g/cm}^3$$

Important issues are quantitative:

- how many MCs?, which mass and radius?
- how void is the space between them? (direct detection?)
- encounter rates with Earth?
- sensitivity to lensing?

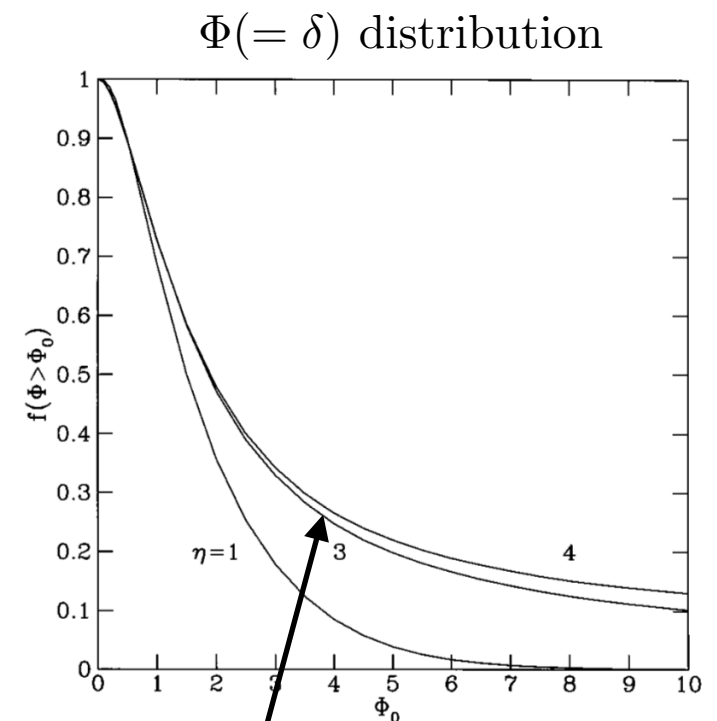


FIG. 2.—Mass fraction of axions in miniclusters with $\Phi > \Phi_0$ as a function of Φ_0 . By $\eta = 4$ the evolution has very nearly frozen.

Kolb-Tkachev 1996

this was not a MC
probability distribution!

first simulations (Scalar Miniclusters ScaMs)

Zurek Hogan Quinn 2007

- Simulated axion field $\ddot{\theta} + 3H\dot{\theta} - \frac{1}{R^2}\nabla^2\theta + m_A^2(T)\sin\theta = 0$
- Initial conditions ad-hoc (tuned to avoid domain-walls) white noise in field values

$$\theta = A \sum_{k=1,\dots,6/L} \sin(k_x x) \sin(k_y y) \sin(k_z z)$$

- Evolve until density field is frozen -> switch to N-body simulations
- Generalisation to ALPs, Femtolensing estimates, no MC distribution function, IC-dependent!

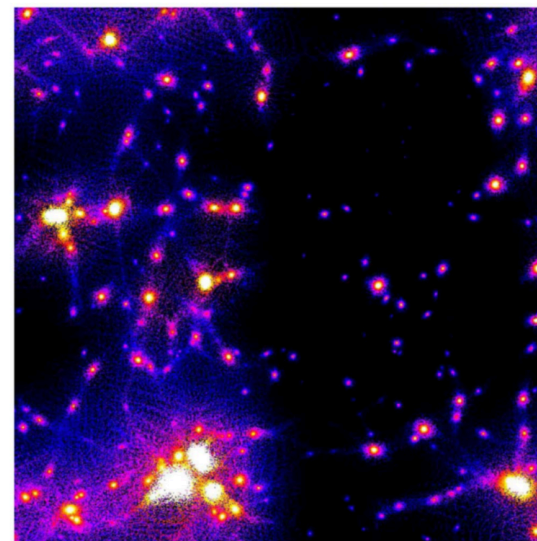
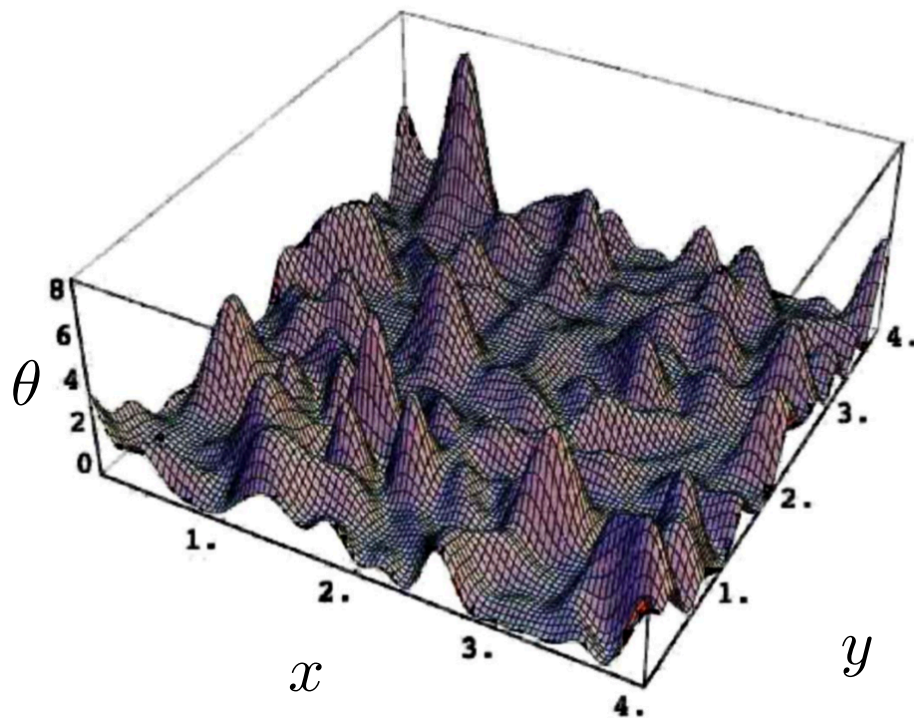


FIG. 5 (color online). Snapshot of structure formation at $z = 3000$ for axion-like ScaMs; the plot is colored according to the logarithm of the density. The scale here is $0.4h^{-1}$ kpc, in physical coordinates, although the result is expected to be invariant for any box size, given that we rescale the smoothing scale accordingly. Note that structure formation has already commenced before matter-radiation equality.

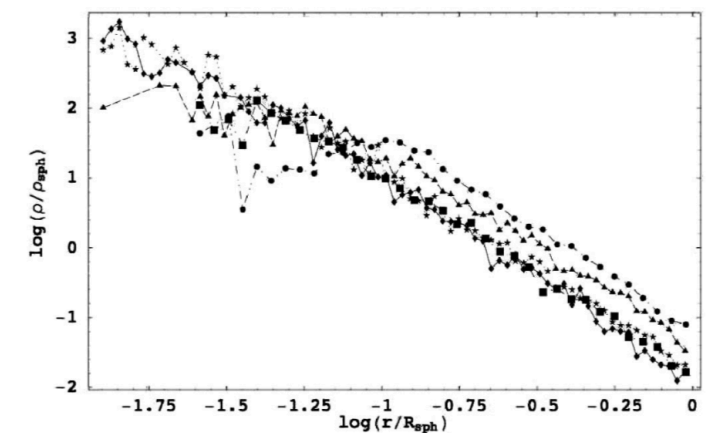
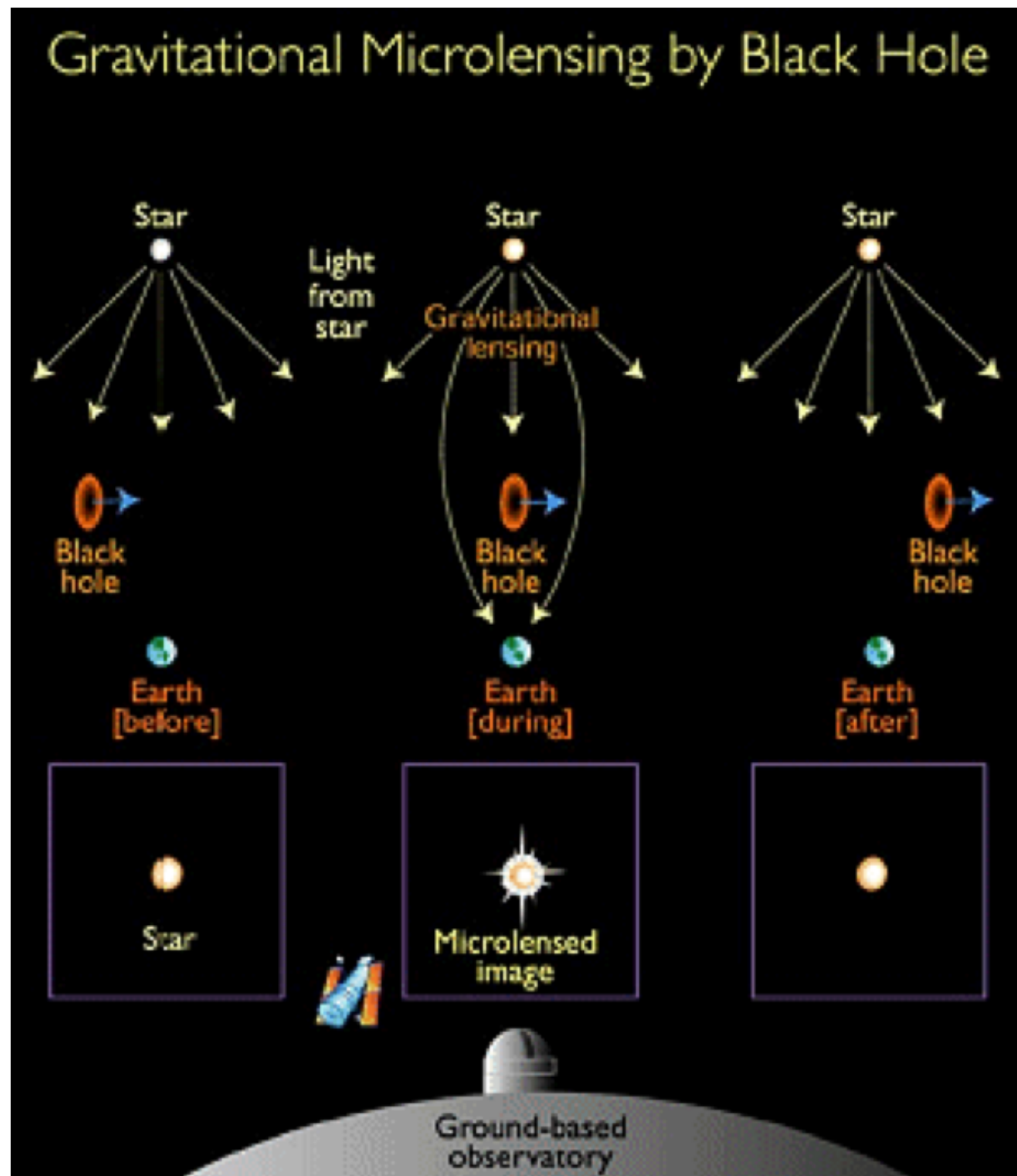


FIG. 7. Axion-like ScaM density profiles for five gravitationally collapsed ScaMs. Vertical axis is $\log(\rho(r)/\rho_{\text{sph}})$, where $\rho_{\text{sph}}(\delta = 1) = 280\rho_{\text{eq}}$; that is, we normalized the density profile against the uniform density prediction of the spherical model, Eq. (14), with $\delta = 1$. Horizontal axis is $\log(r/R_{\text{sph}})$, where R_{sph} is the radius computed from ρ_{sph} and the total mass contained within the horizon at the phase transition, $d_H(T_{\text{trans}})$.

- Recent semi-analytical estimates with linear equation have the same IC problem

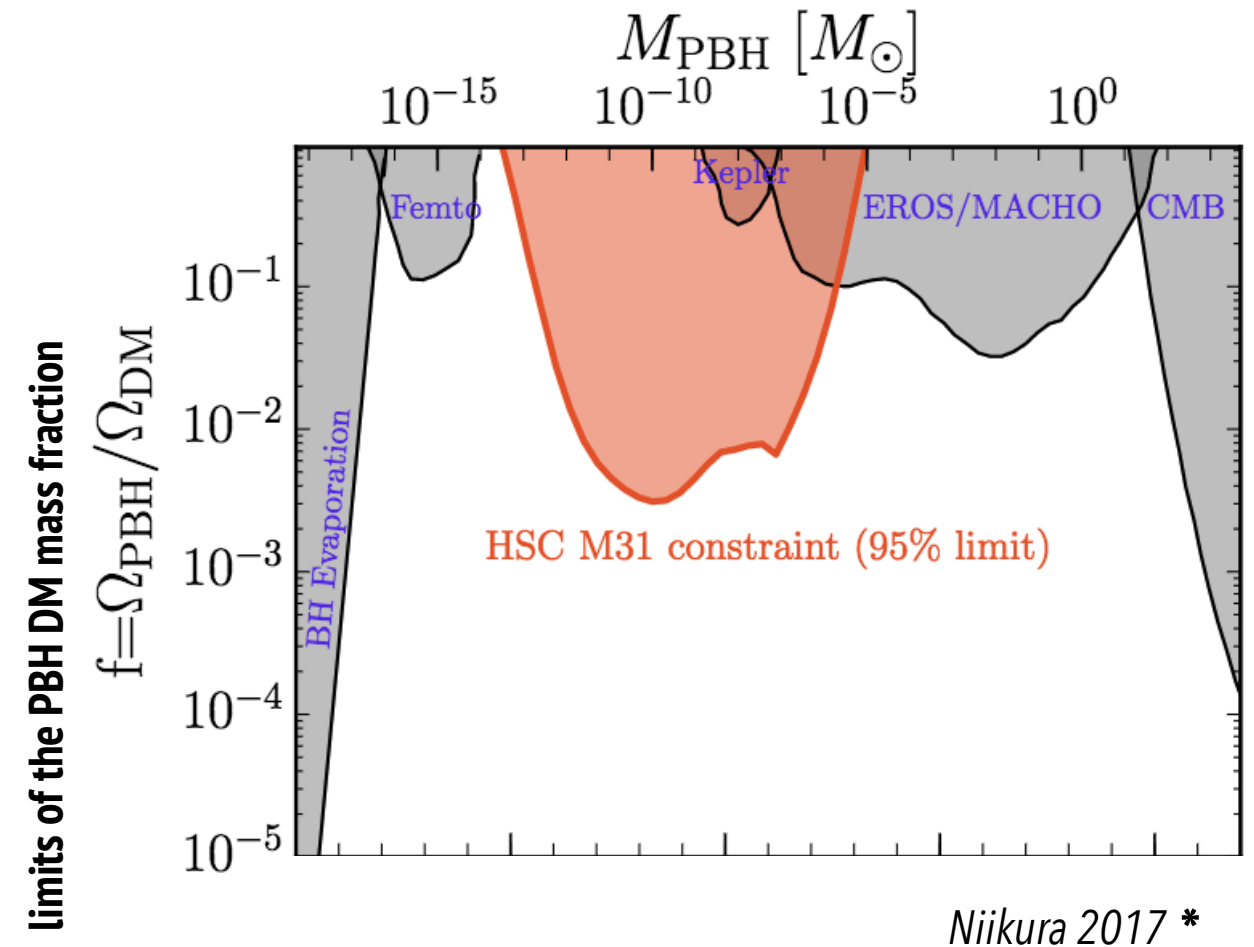
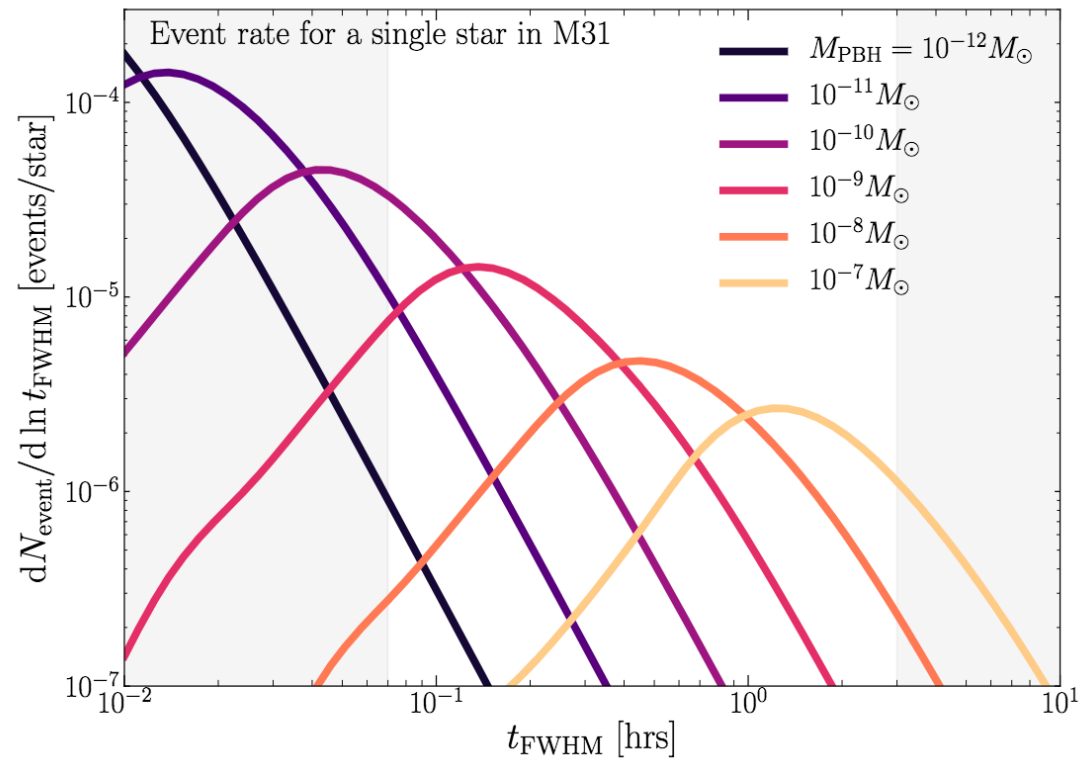
$$\ddot{\theta} + 3H\dot{\theta} + m_A^2(T)\theta = 0 \quad \text{Enander 2017}$$

Gravitational Microlensing



Microlensing

- Subaru HSC dedicated search of Primordial Planck hole events along M31
- 10^7 stars, $t \sim 2$ min sampling rate



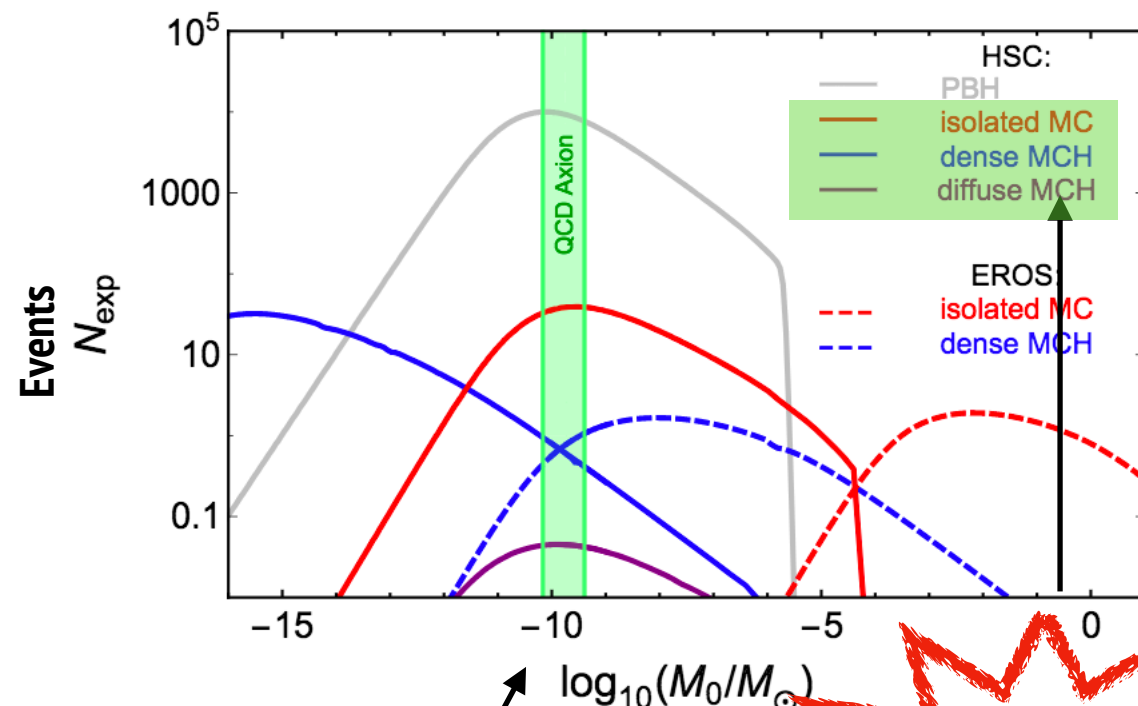
*See however Inomata 2018 (Wave effect decreases constraints below $10^{-10} M_{\text{sun}}$)

Microlensing by MCs

- Axion MCs are fluffier than PBHs (less signal, more duration) but could be detected!

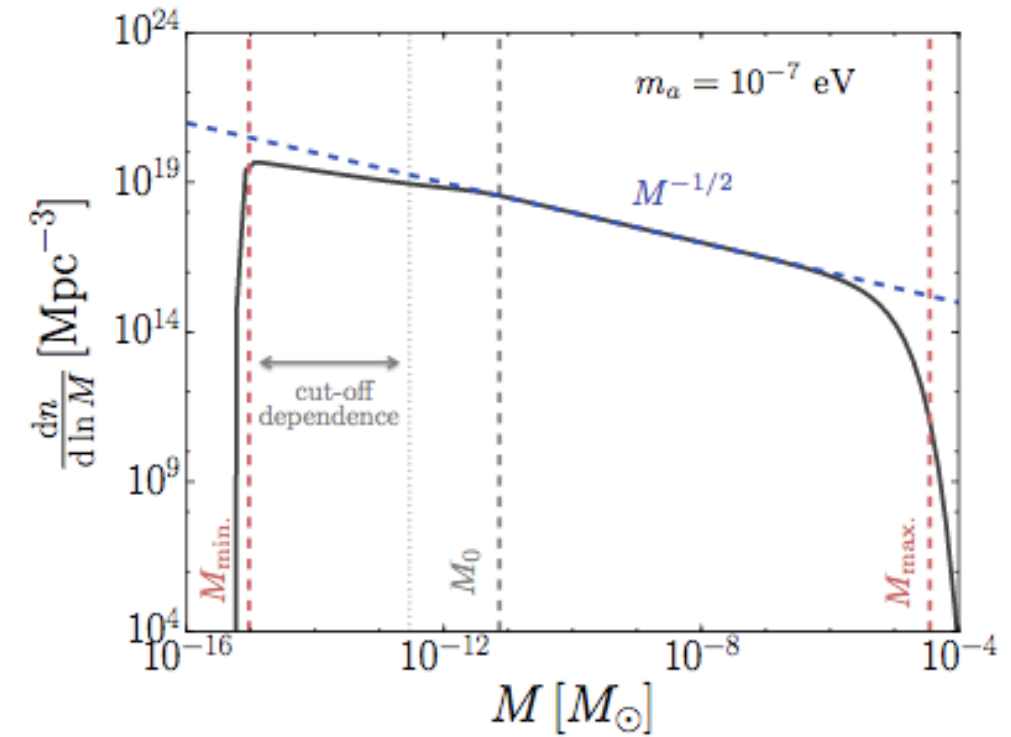
Marsh, Fairbairn, Quevillon 2017

- model the MC mass function by Press-Schechter
- Used a generous value of $M_0 \sim (\pi)^3 M_{0,\text{Tkachev}}$

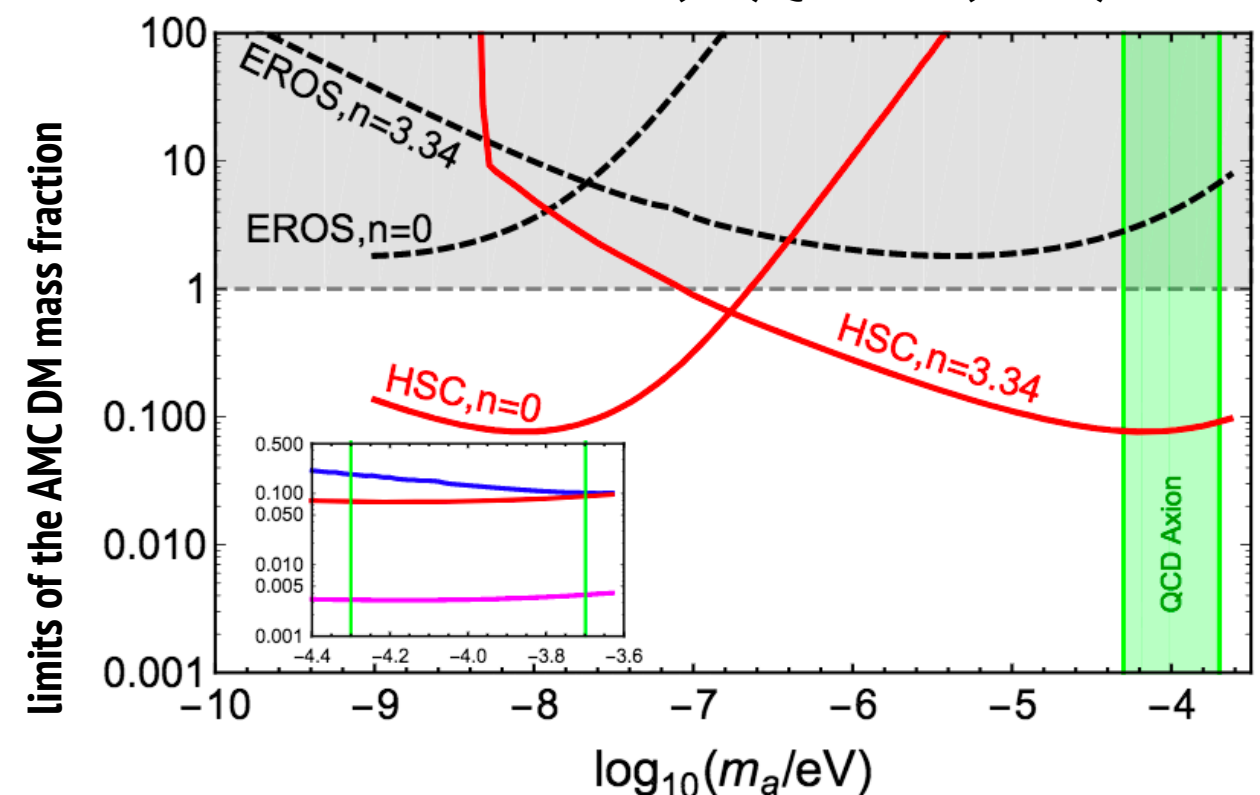


note the relevance of M_0

Uncertainties in the
MC mass, profile,
mass function dn/dM
merging history



Constraints ALP (n=0) QCD axion (n=3.34)

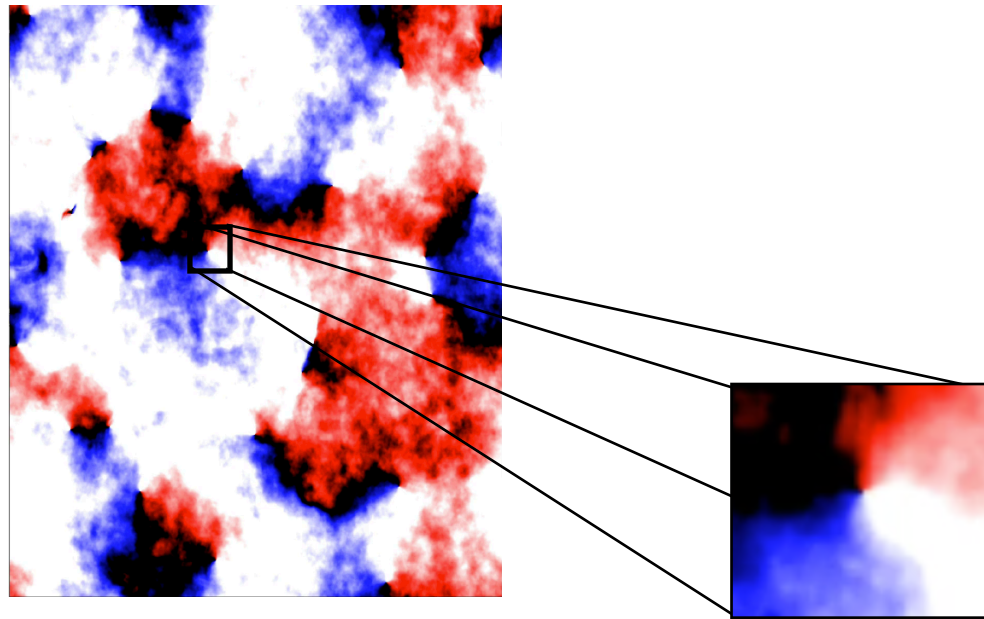
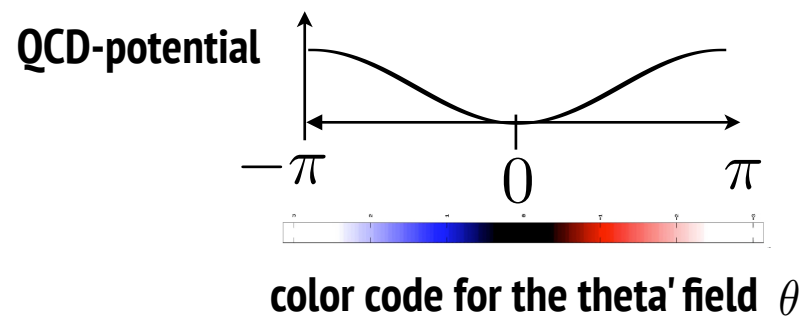


New simulations of the axion field

Vaquero, Stadler, JR 2018

- Previous works used inconsistent ICs
- Random initial conditions in theta imply a network of cosmic (global) strings

Kibble 1980



$$\theta \in (0, 2\pi)$$

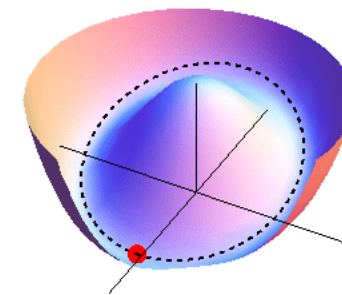
around one point (2D) one line (3D)

String tension - divergent, needs UV

$$\mu = \pi f_a^2 \log \frac{r_{UV}}{r_{IR}} \sim \pi f_a^2 \log \frac{f_a}{H}$$

- Simplest UV completion $\Phi = \rho e^{i\theta}$ to regularise string core

$$\ddot{\phi} - \frac{1}{R^2} \nabla^2 \phi + 3H\dot{\phi} + \lambda_\phi \phi (|\phi|^2 - f_a^2) + m_a^2 f_a = 0$$



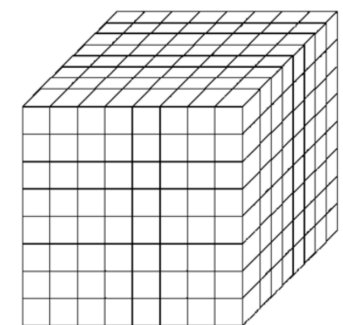
$V(\Phi)$

- Evolve in large cartesian grids (as much dynamical range as possible)

Phi simulation -> theta only simulation -> theta frozen... (?)

Compute final density distribution

Public MPI/OpenMP code developed ready for HPC <https://github.com/veintemillas/jaxions>

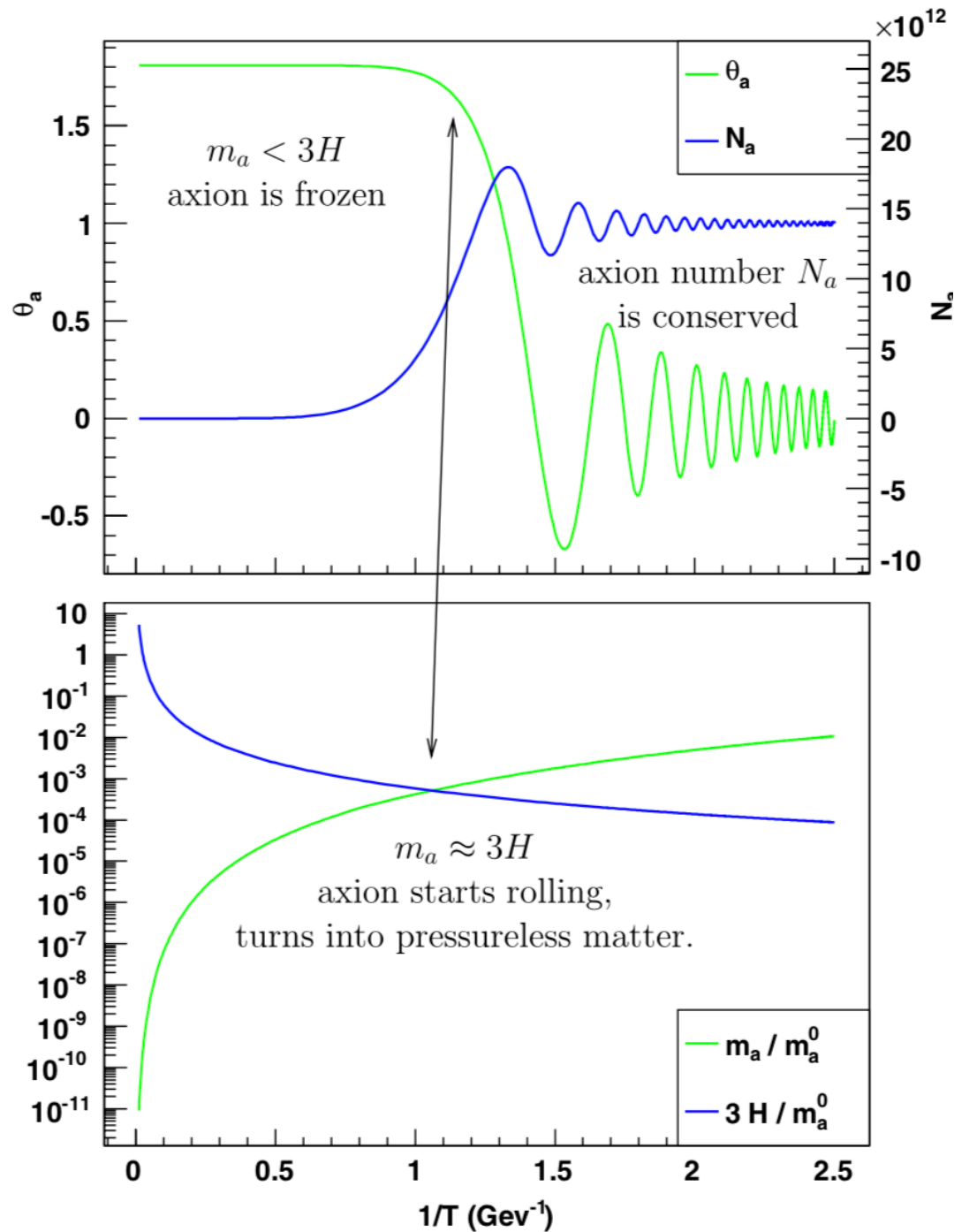


- High-effective tension models available later (work in progress) *Klaer and Moore 2017*

Evolution, time scales

Zero mode is "frozen" and starts to oscillate when $m_a(t_{\text{osc}})t_{\text{osc}} \sim O(1)$

$$m_A(T_1) = H(T_1) = H_1$$



Wantz-Shellard 2010

Temperature

$$T_1 \simeq 1.694 \text{ GeV} \left(\frac{m_A}{50 \mu\text{eV}} \right)^{0.1638},$$

Hubble rate

$$H_1 \simeq 3.45 \times 10^{-3} \mu\text{eV} \left(\frac{m_A}{50 \mu\text{eV}} \right)^{0.338}$$

Redshift

$$1 + z_1 \simeq R_1^{-1} = 1.956 \times 10^{13} \left(\frac{m_A}{50 \mu\text{eV}} \right)^{0.1712}$$

Comoving Horizon size

$$L_1 \equiv \frac{1}{H_1 R_1} \simeq 1.116 \times 10^{17} \text{ cm} \left(\frac{50 \mu\text{eV}}{m_A} \right)^{0.167} = 0.0362 \text{ pc} \left(\frac{50 \mu\text{eV}}{m_A} \right)^{0.167}$$

m_A, H from Borsanyi 2016

Axion number in comoving volume > adiabatic invariant

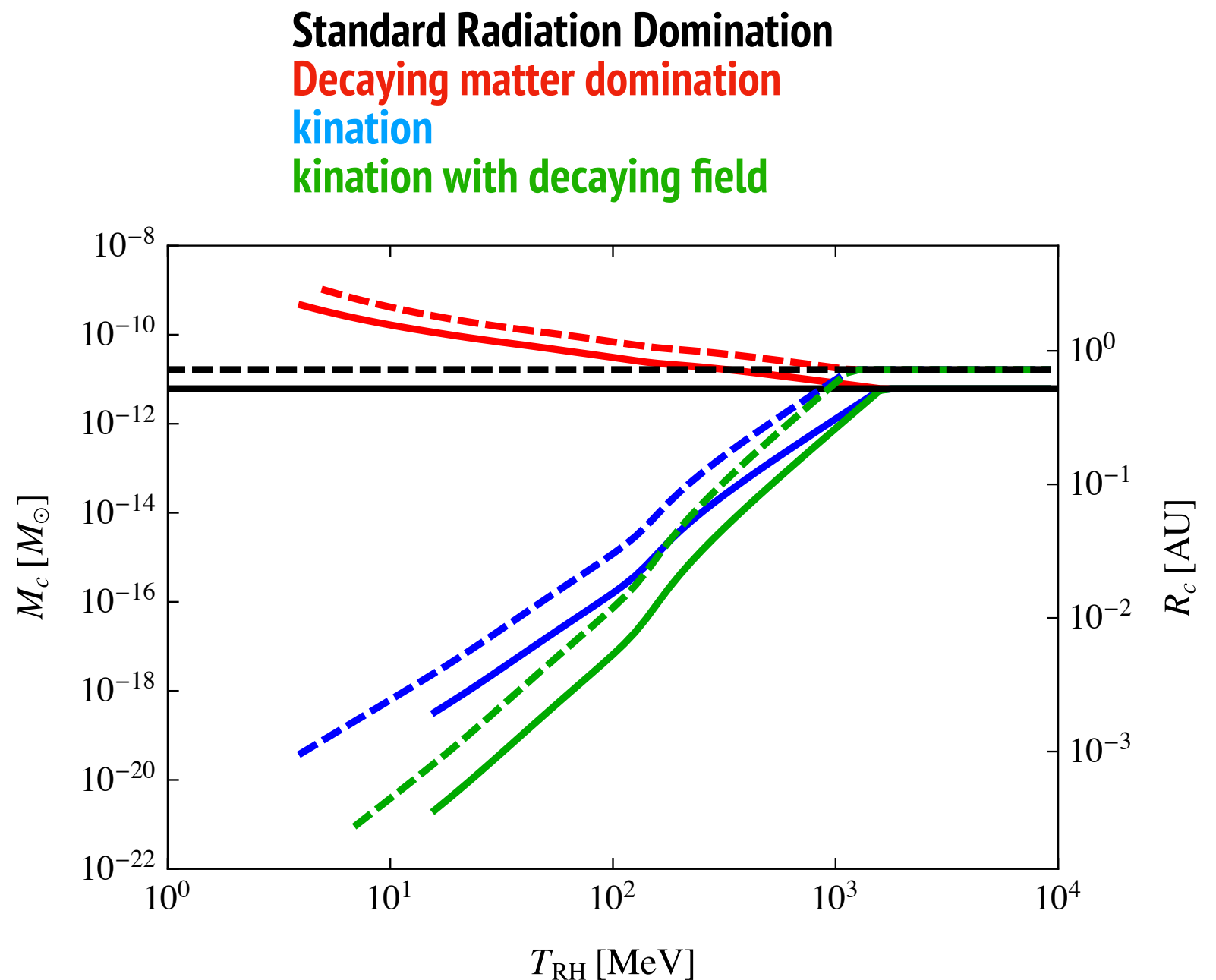
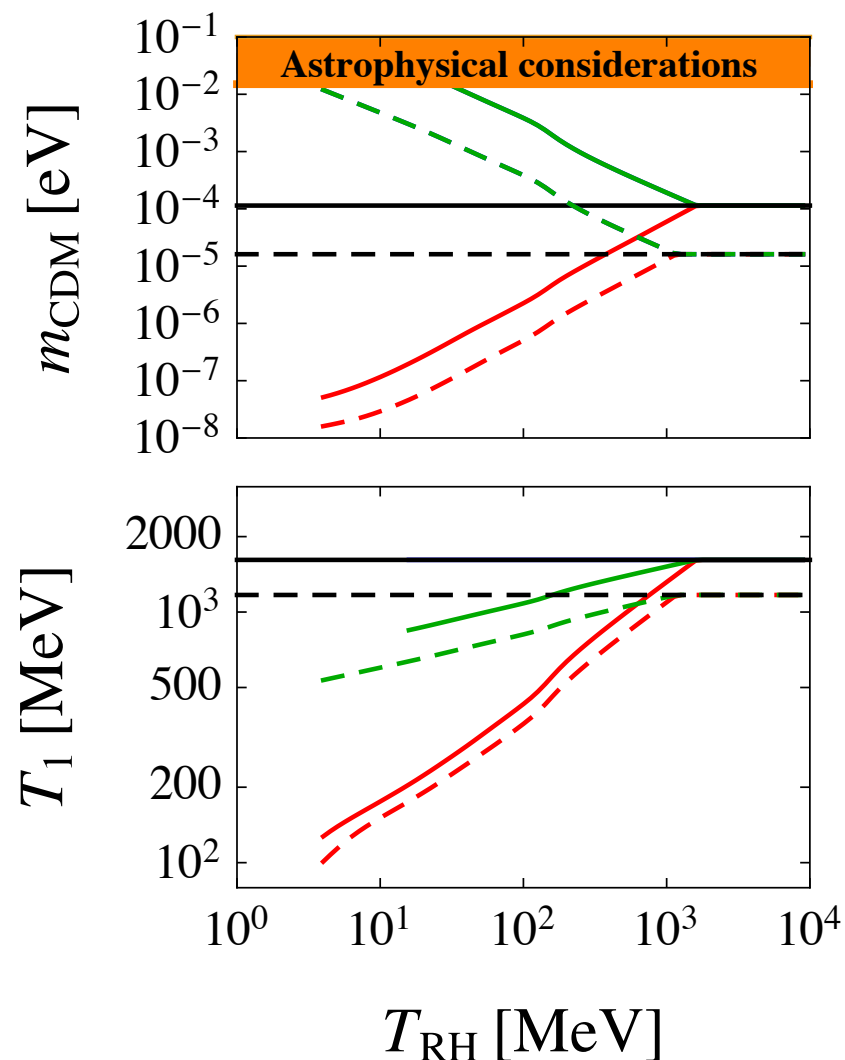
$$N_a \sim \frac{\rho_a}{m_a} R^3$$

Cosmological model dependence...

Visinelli, Redondo 2018

Alternative pre-BBN cosmologies change T_1 and R_1 and so:

- the suitable axion mass
- The typical Minicluster mass and radius



~Scale-invariant equations

Switching to conformal coordinates and field normalised to natural values, $L_1, H_1, \dots$

and approximating $m_A^2 \sim m_A^2(T_1) \left(\frac{T_1}{T}\right)^n = H_1^2 \tau^n$ (τ conformal time)

the dependence on L1 is implicit $\Phi'' - \nabla^2 \Phi - \lambda \Phi(|\phi|^2 - \tau^2) - \tau^{n+3} = 0$

Simulations valid for all consistent values of L1 (function of axion mass today)

Parameters

Volume $L/L_1 \gtrsim 6$

Around $\tau \sim 2$ strings are
strongly pulled by axionic domain
walls to collapse in loops

String tension

$$\lambda = \lambda_\phi \frac{f_a^2}{H_1^2} = \frac{m_s^2}{H_1^2} \sim 10^{60}$$

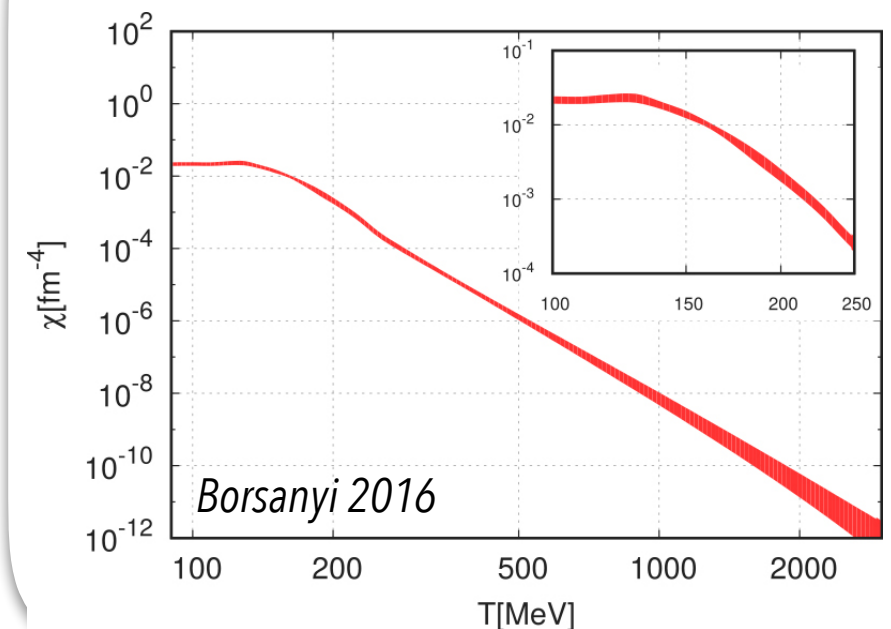
(dynamical range²)

Largest simulations + PRS

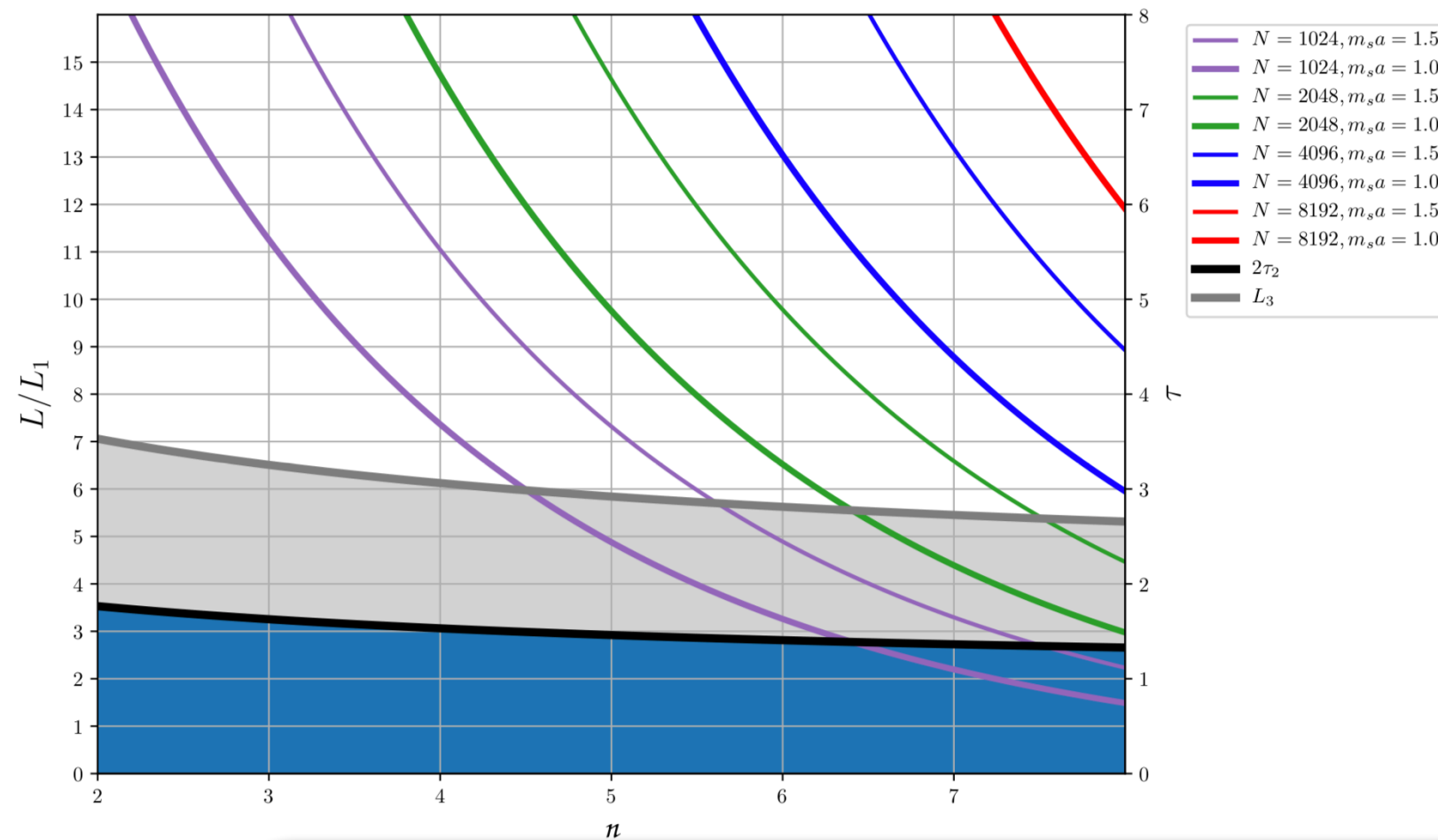
$$\lambda \sim \frac{2 \times 10^6}{\tau^2} \quad \log \frac{m_s}{H} \sim 8$$

(8192³, L=6)

n~7-7.5 in the relevant T-range



Constraints

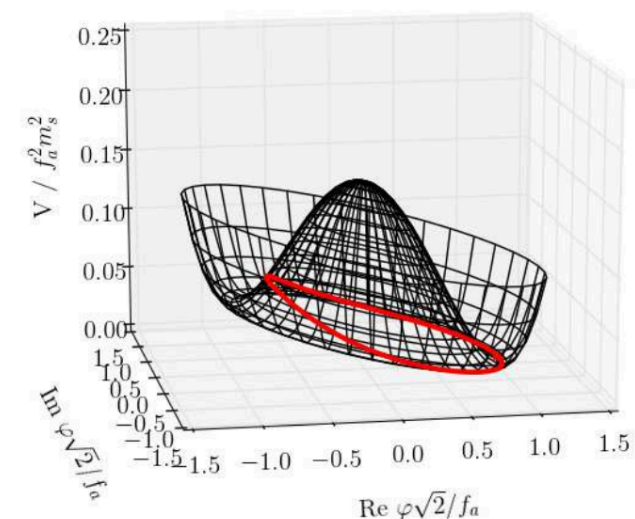
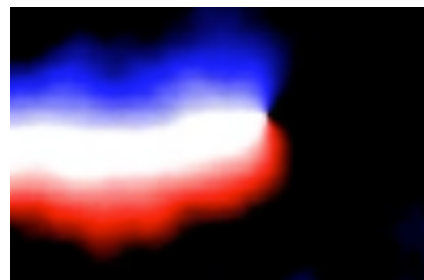


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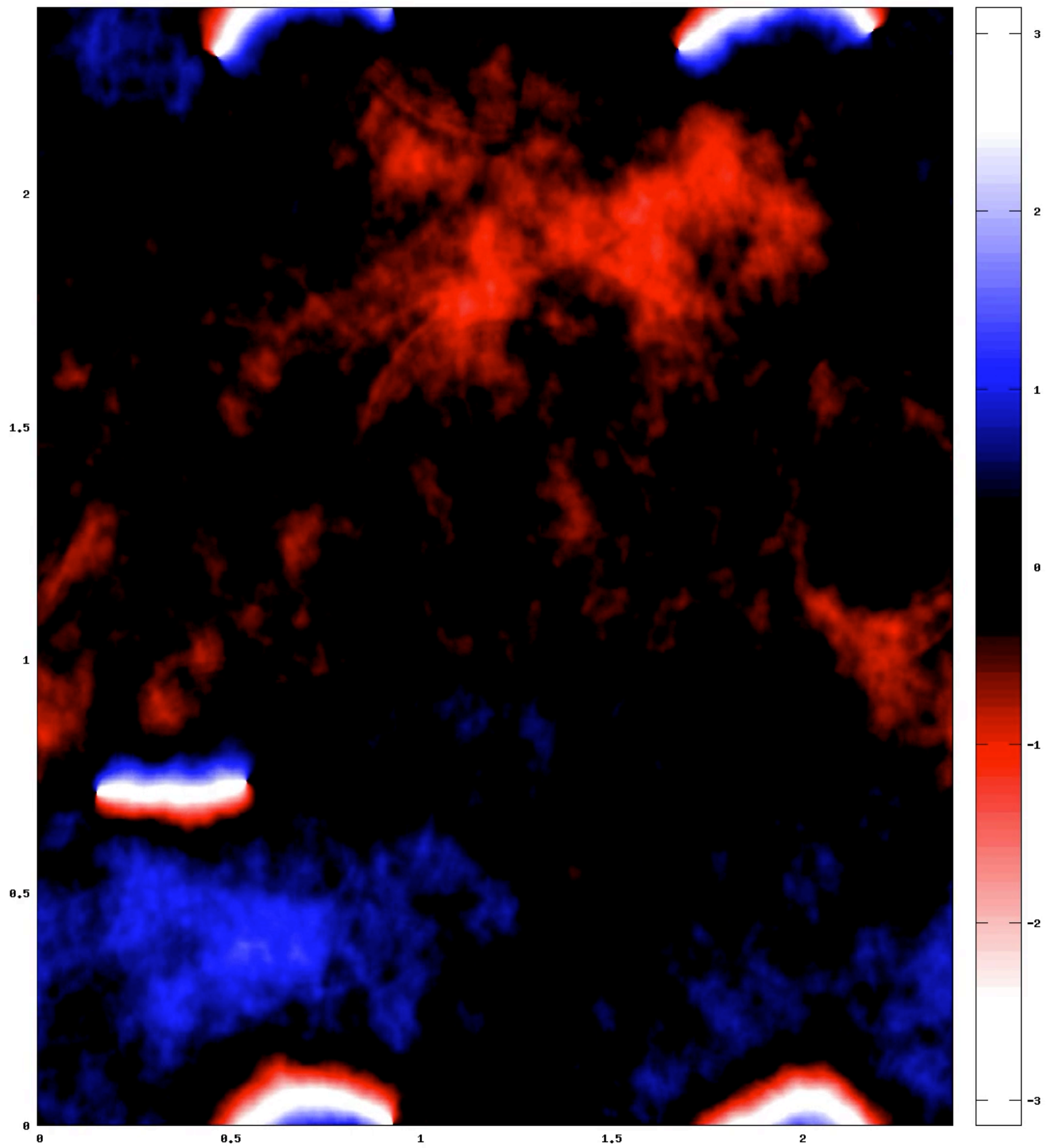
Volume $L/L_1 \gtrsim 6$

Around $\tau \sim 2$ strings are strongly pulled by axionic domain walls to collapse in loops

String tension : unphysical destruction of domain walls



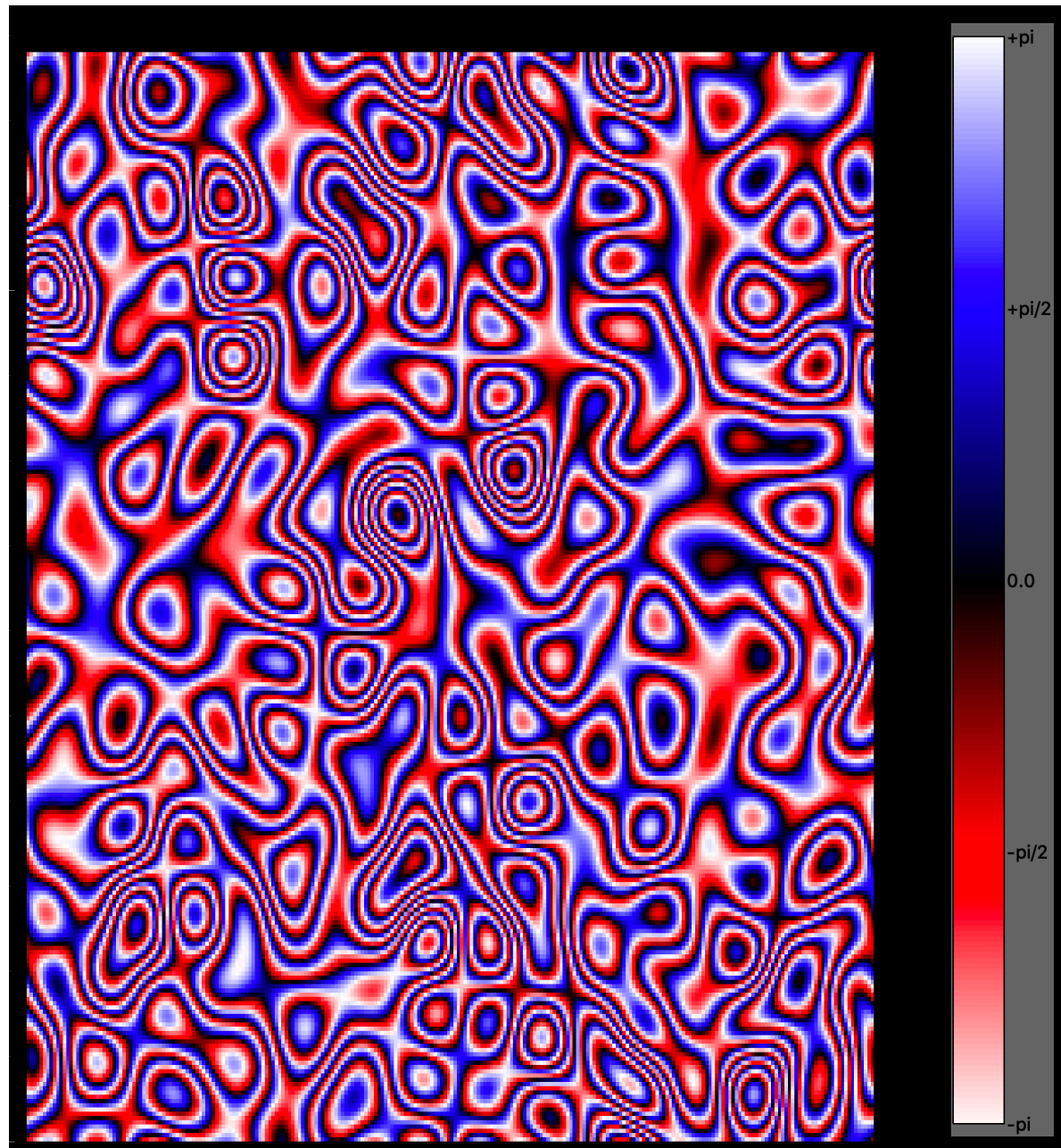
slice of theta

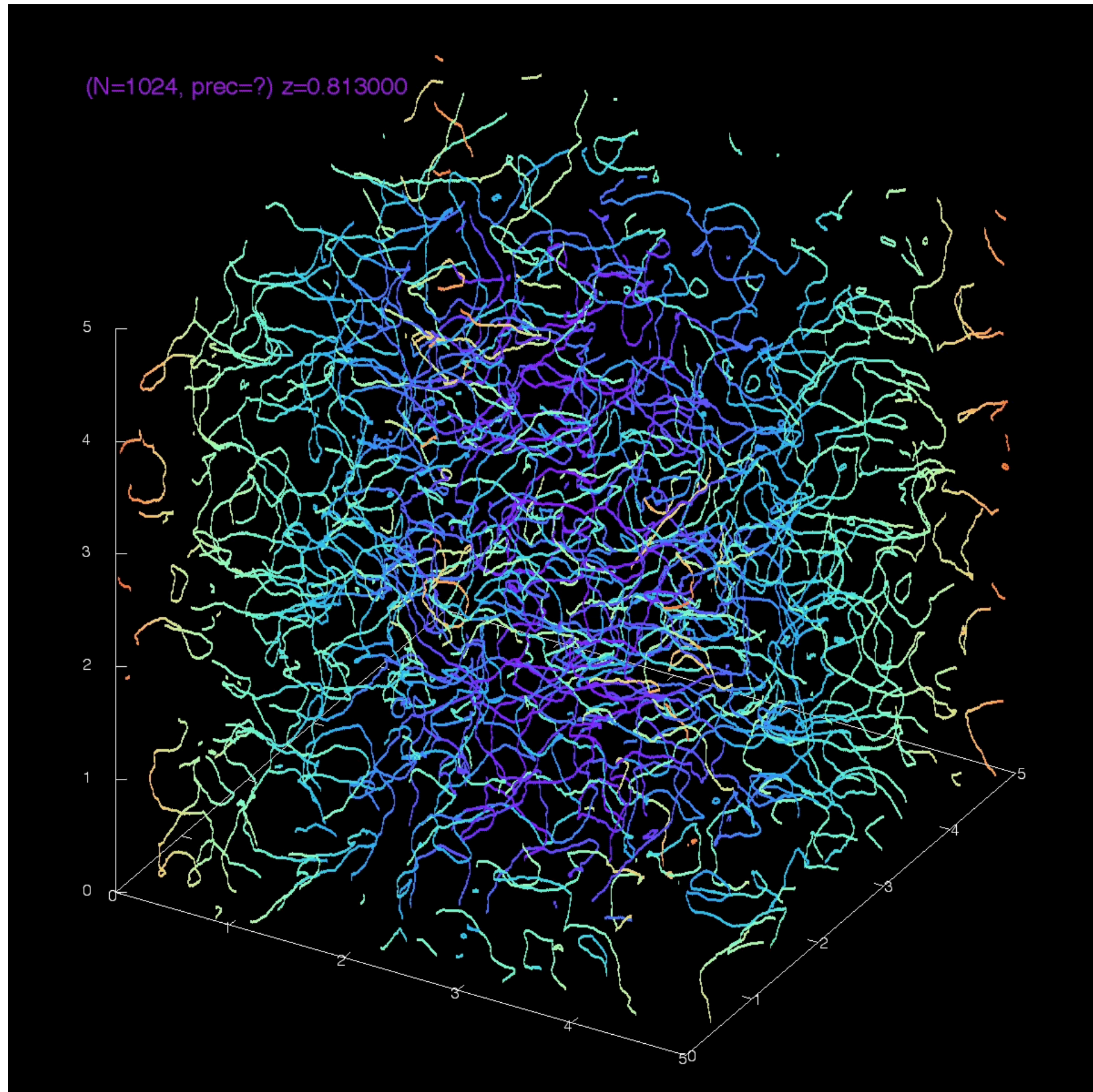


Tkachev Initial conditions

$$\theta = A \sum_{k=1, \dots, 6/L} \sin(k_x x) \sin(k_y y) \sin(k_z z)$$

White noise in theta angle





string evolution

Final density is highly inhomogenous

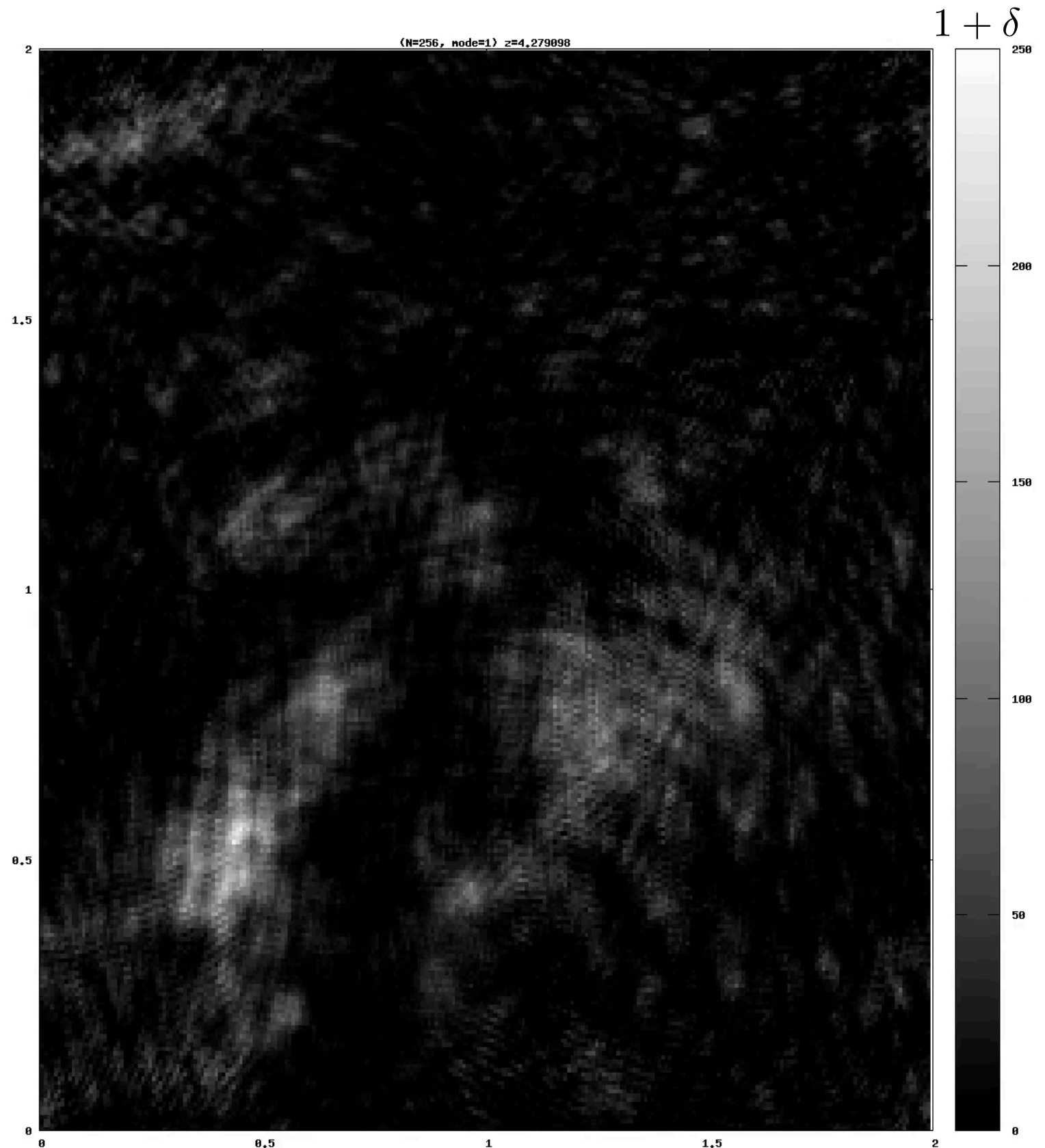
Axion overdensity contrast

$$\delta = \frac{\rho - \bar{\rho}}{\bar{\rho}}$$

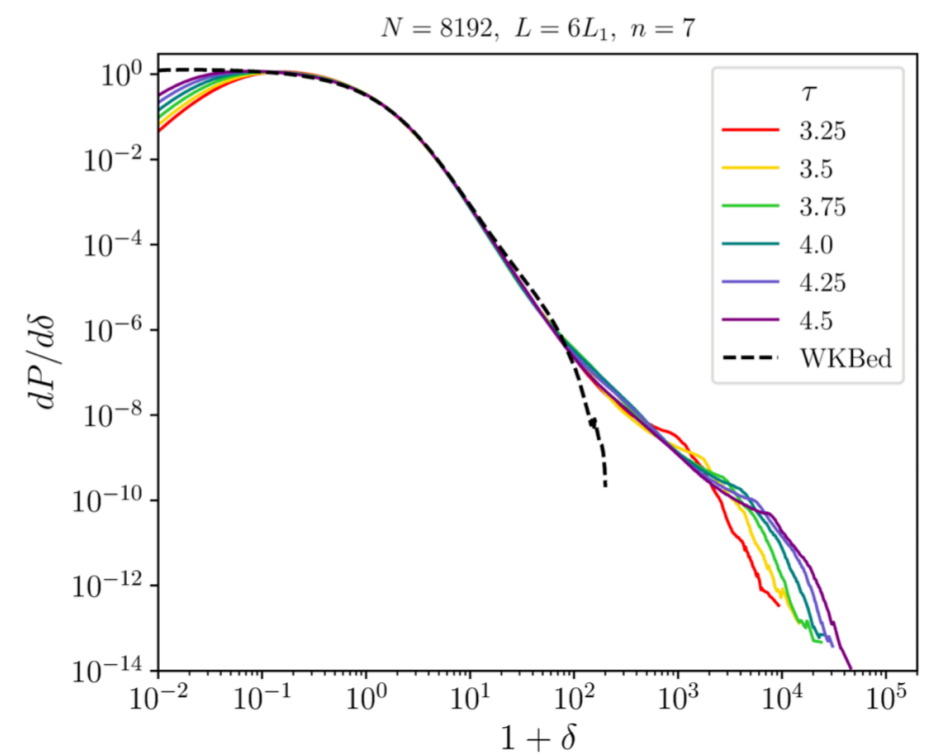
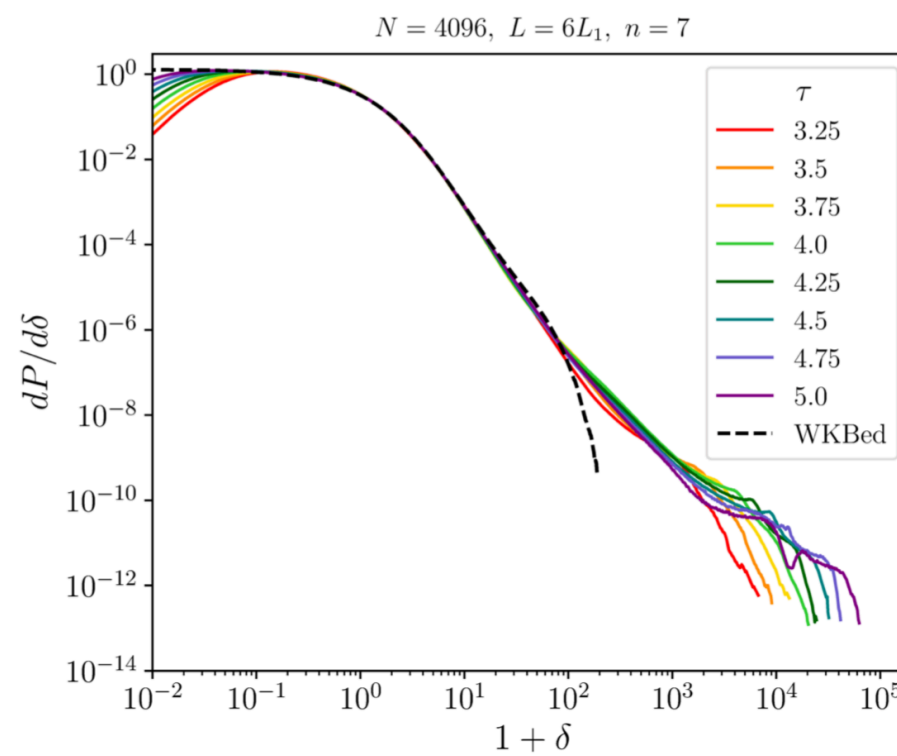
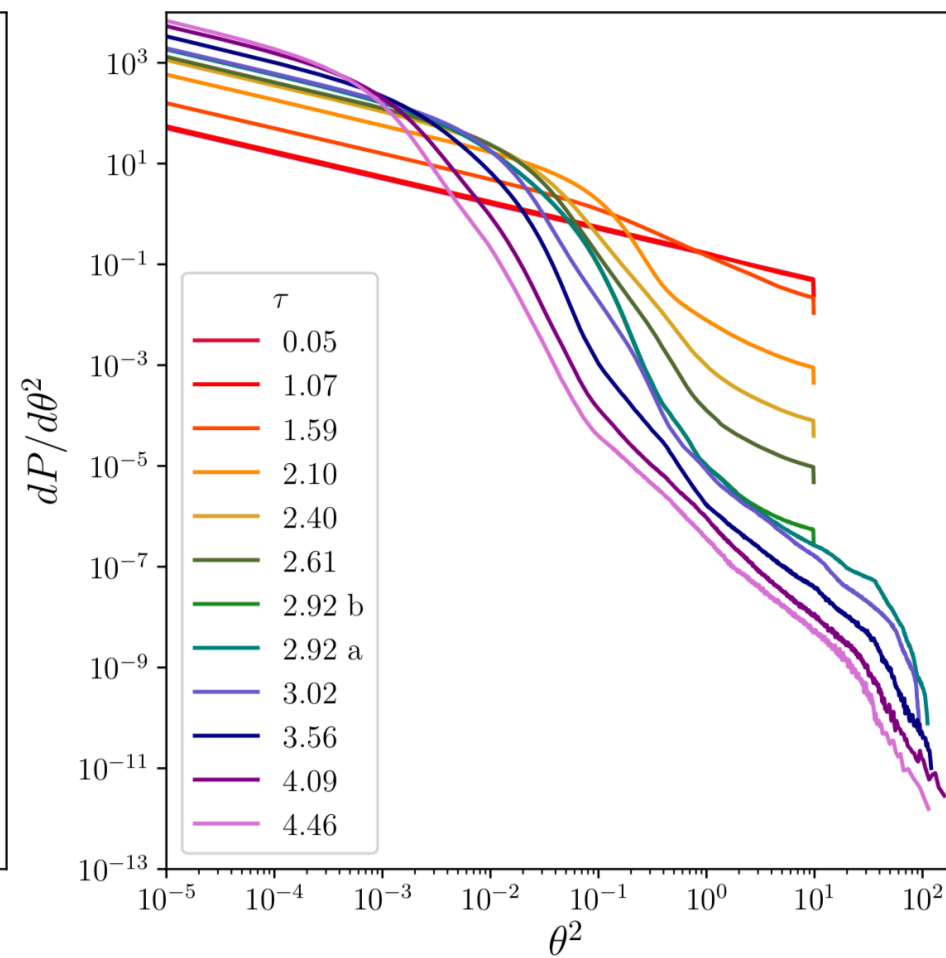
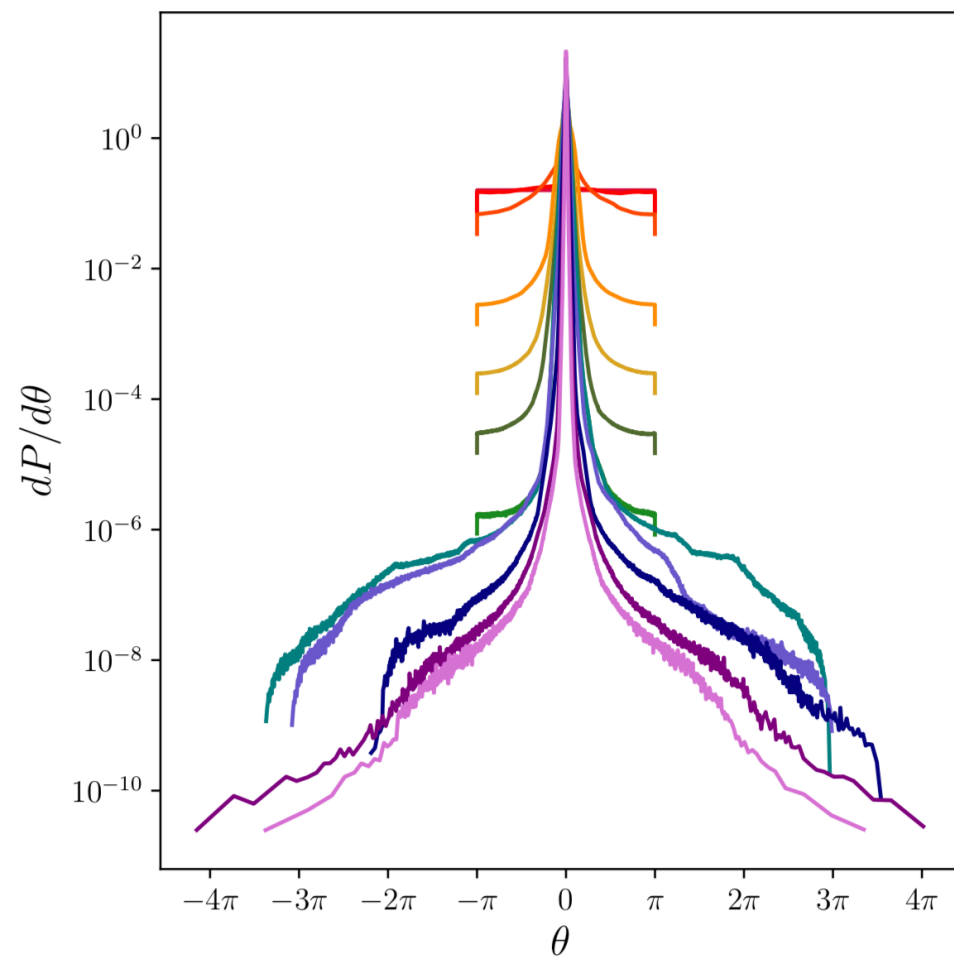
Shown is a 2D slice of $1 + \delta$

- Starts after last string-domain-wall collapses
- quickly axions become non-relativistic
- long wavelengths become frozen
- small scales very visible
- interference patterns not washed out

Low resolution example



Distribution of theta, density



Density contrast evolution

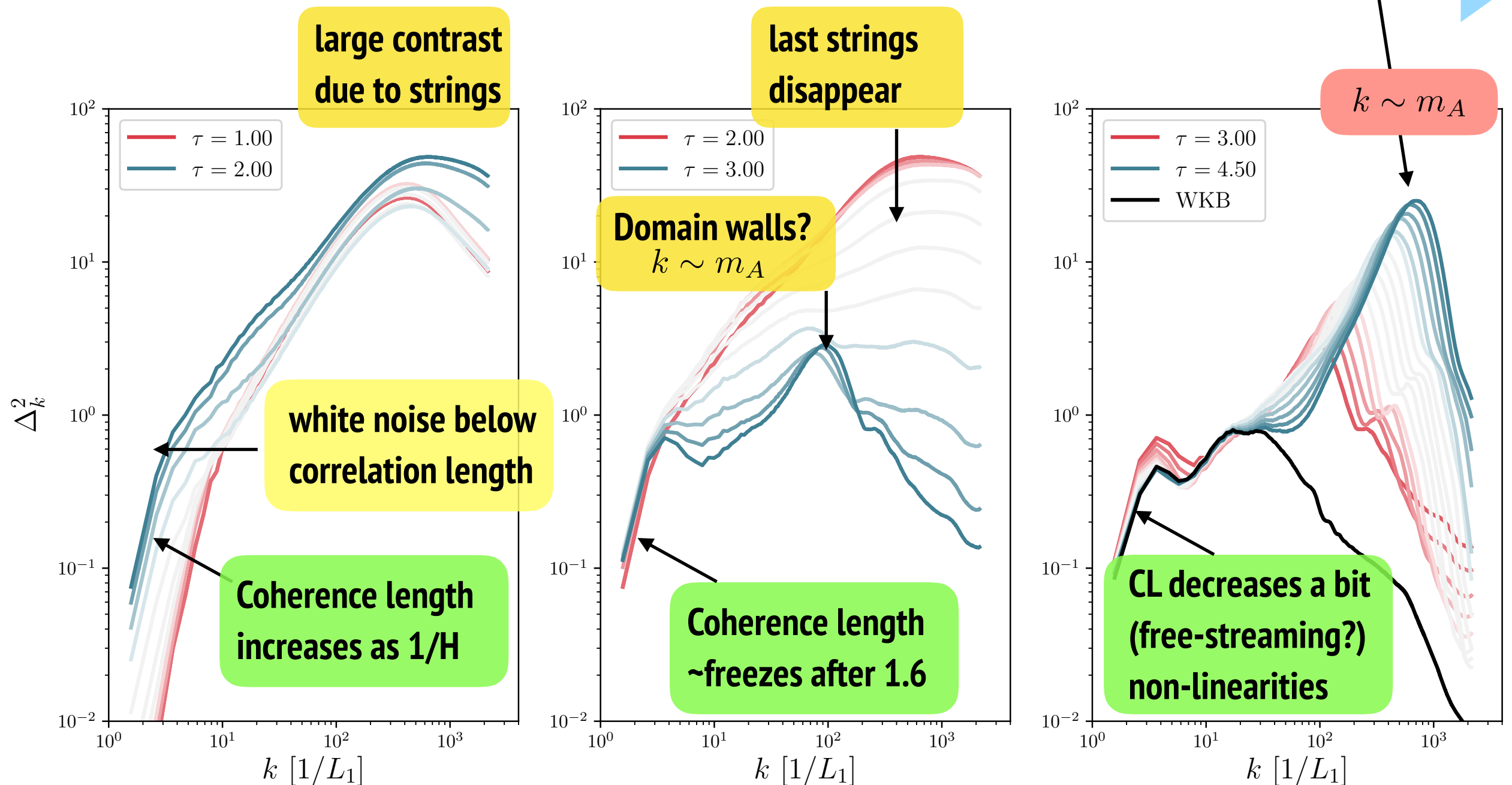
L=6, N=8192

Dimensionless-variance $\Delta_k^2 = \frac{k^3}{2\pi^2} \frac{1}{V} \langle |\tilde{\delta}(k)|^2 \rangle$

Early times, strings

Domain walls, axion mass peak

freeze out, axiton peak τ

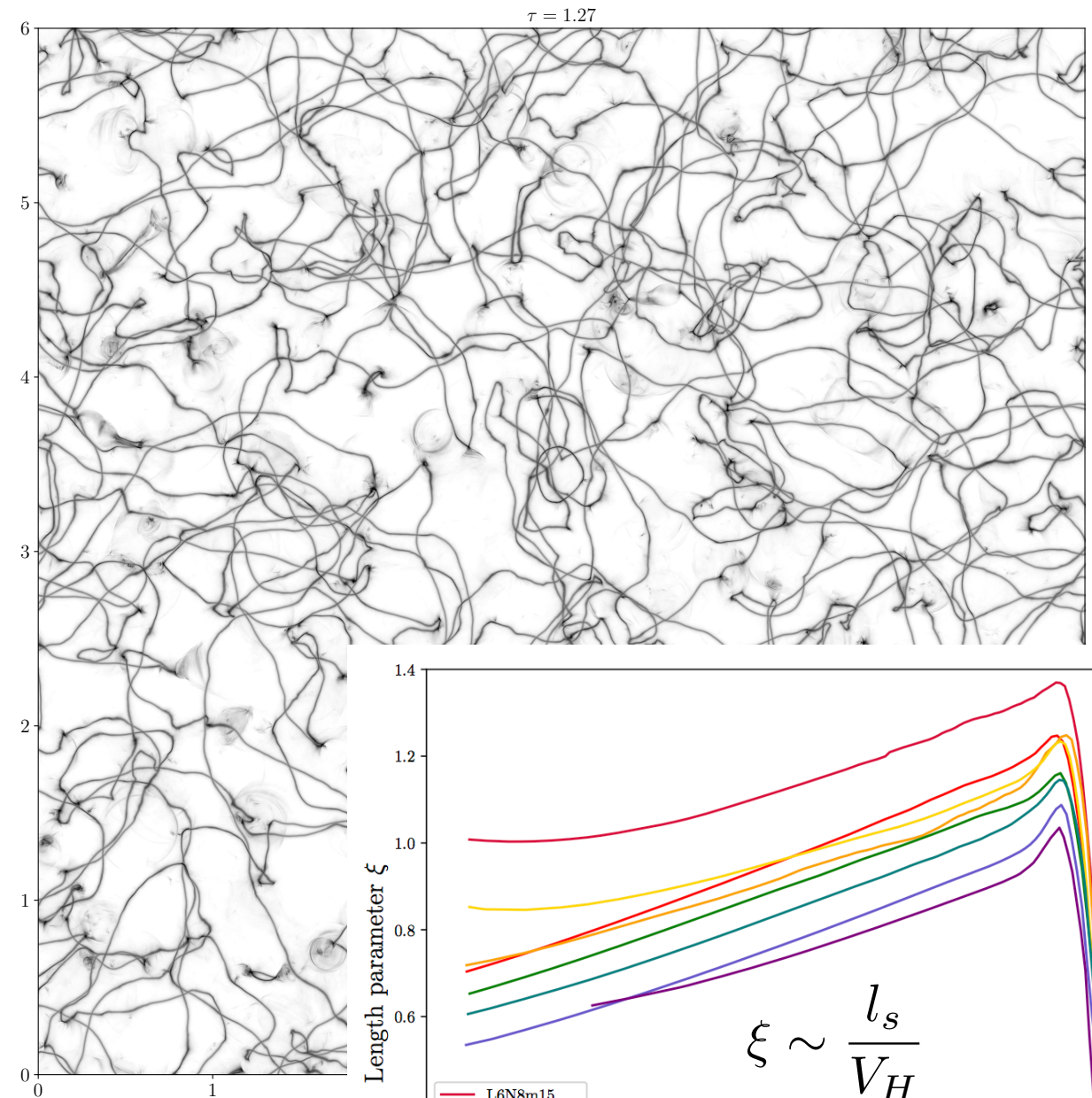
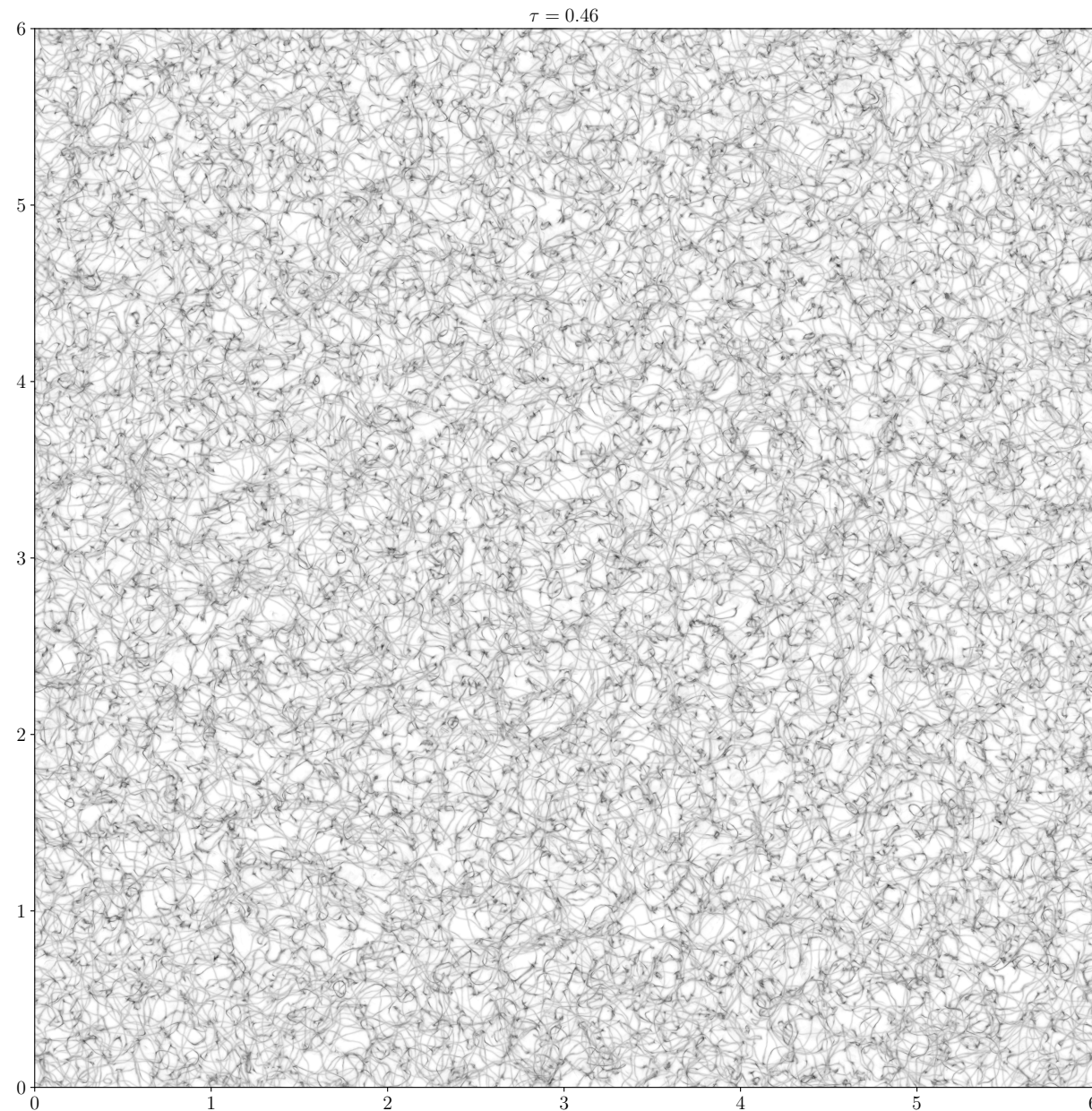


Density contrast evolution in conf. space

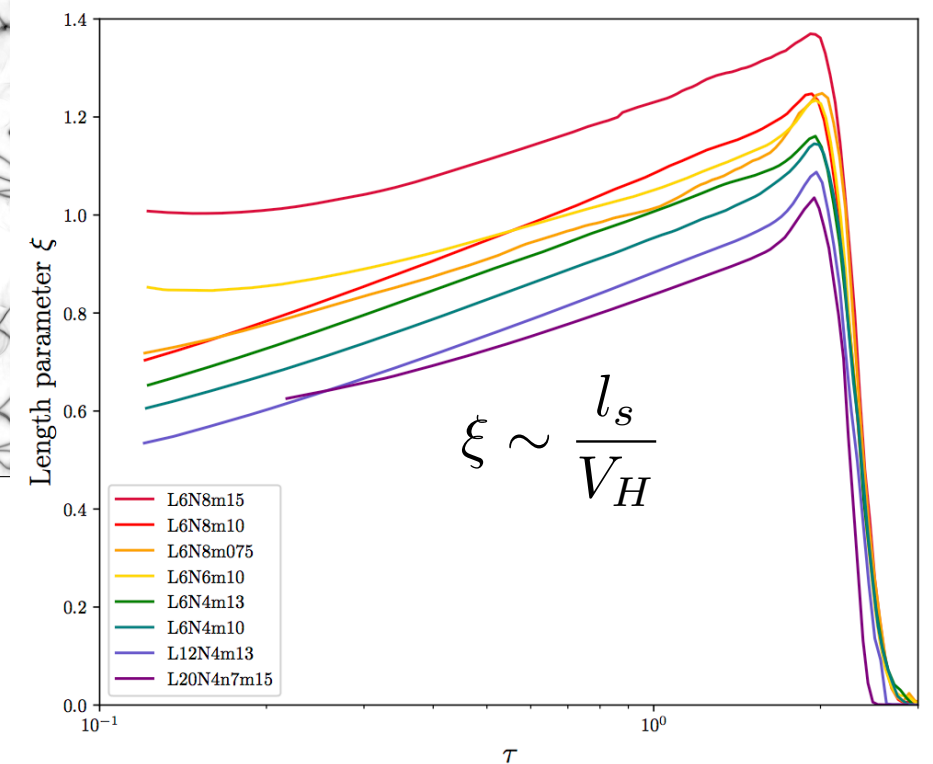
L=6, N=8192

Early times, strings

scaling solution with O(1) string/Hubble volume ... (scaling violations*)



projection plots of density² (3D→2D)



Density contrast evolution in conf. space

$L=6, N=8192$

Early times, strings

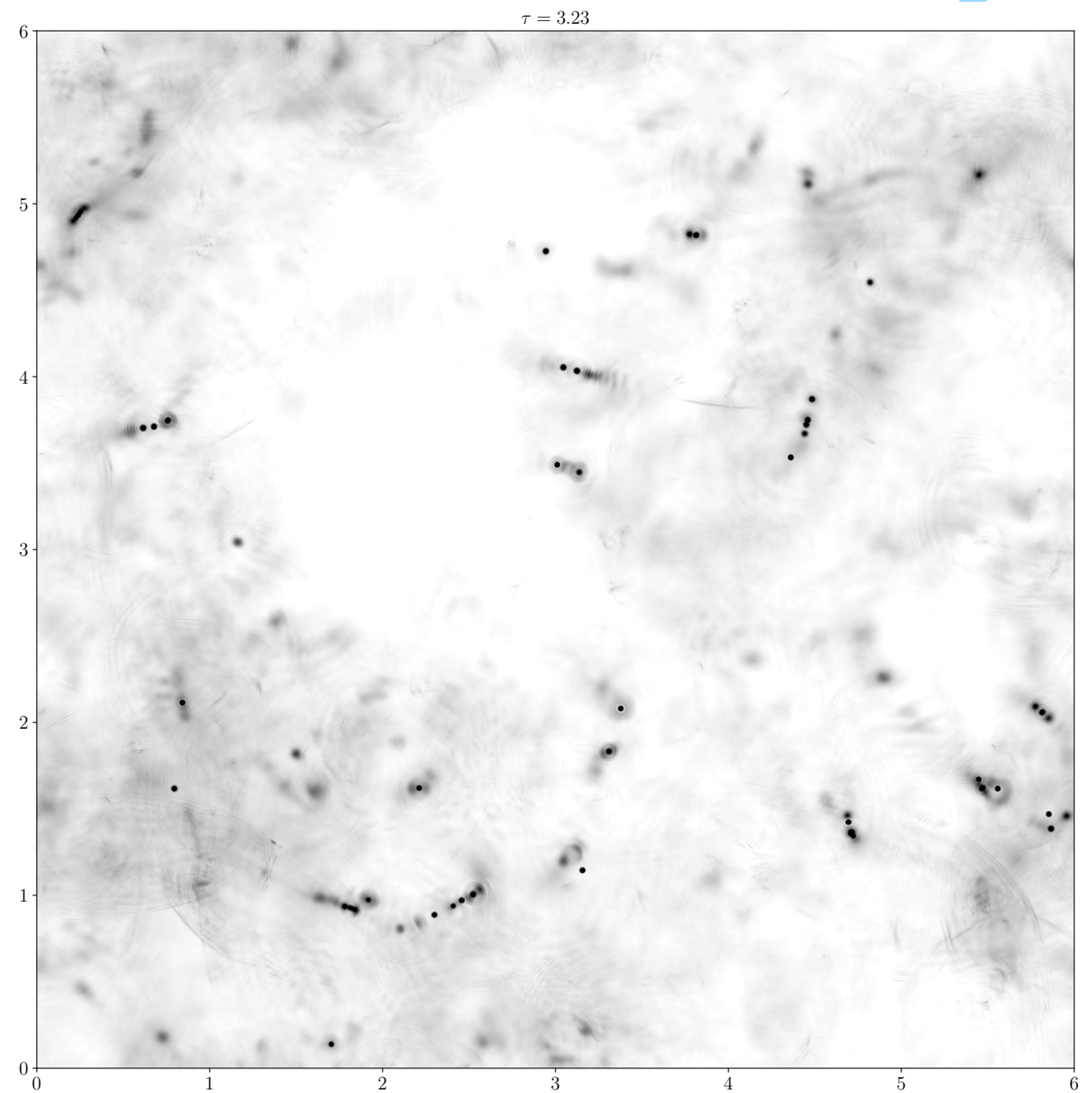
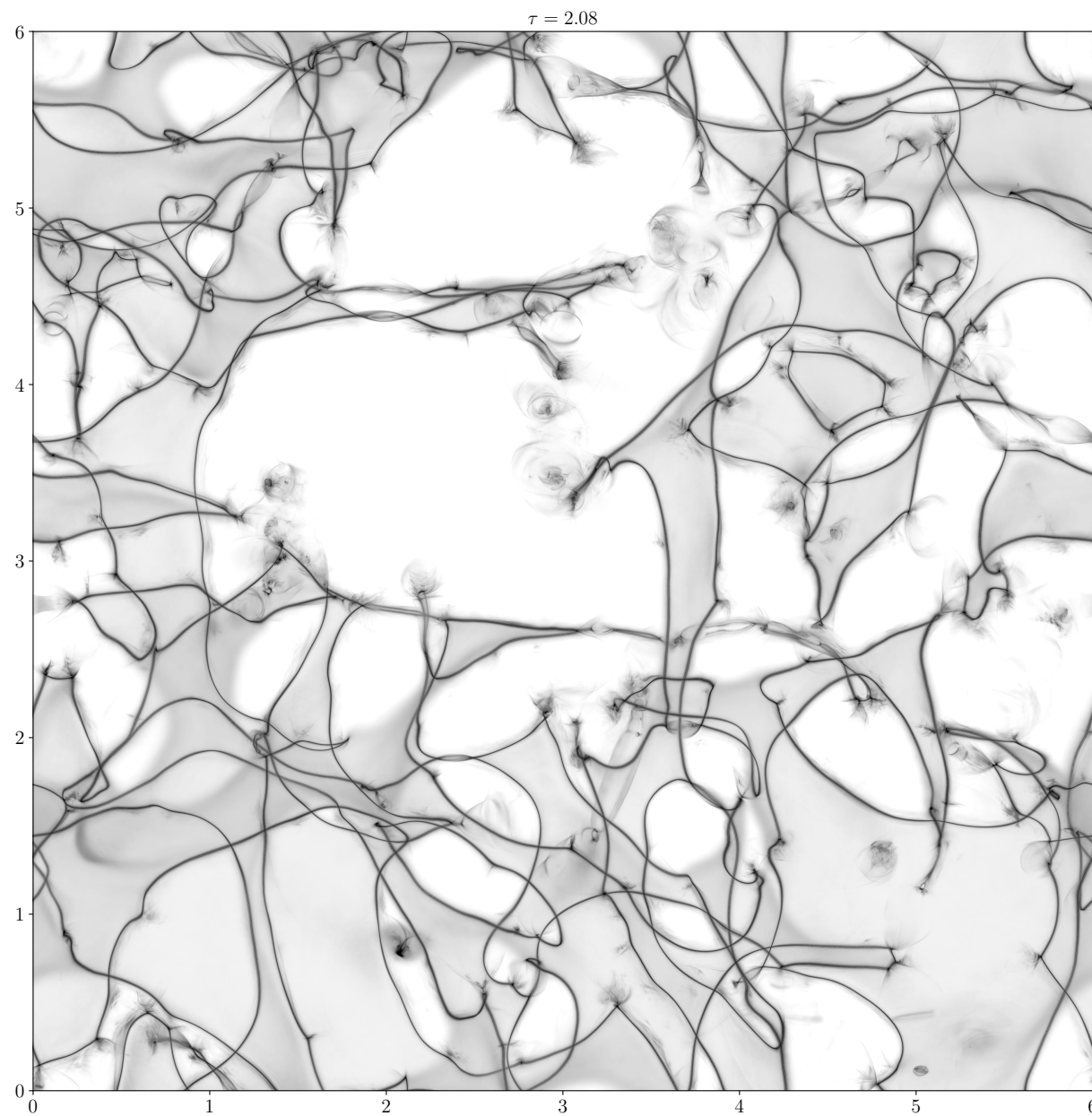
scaling solution with $O(1)$ string/Hubble volume ... (scaling violations*)

Reconnection hard emission, string cores, hard emission from loop collapse

Density contrast evolution in conf. space

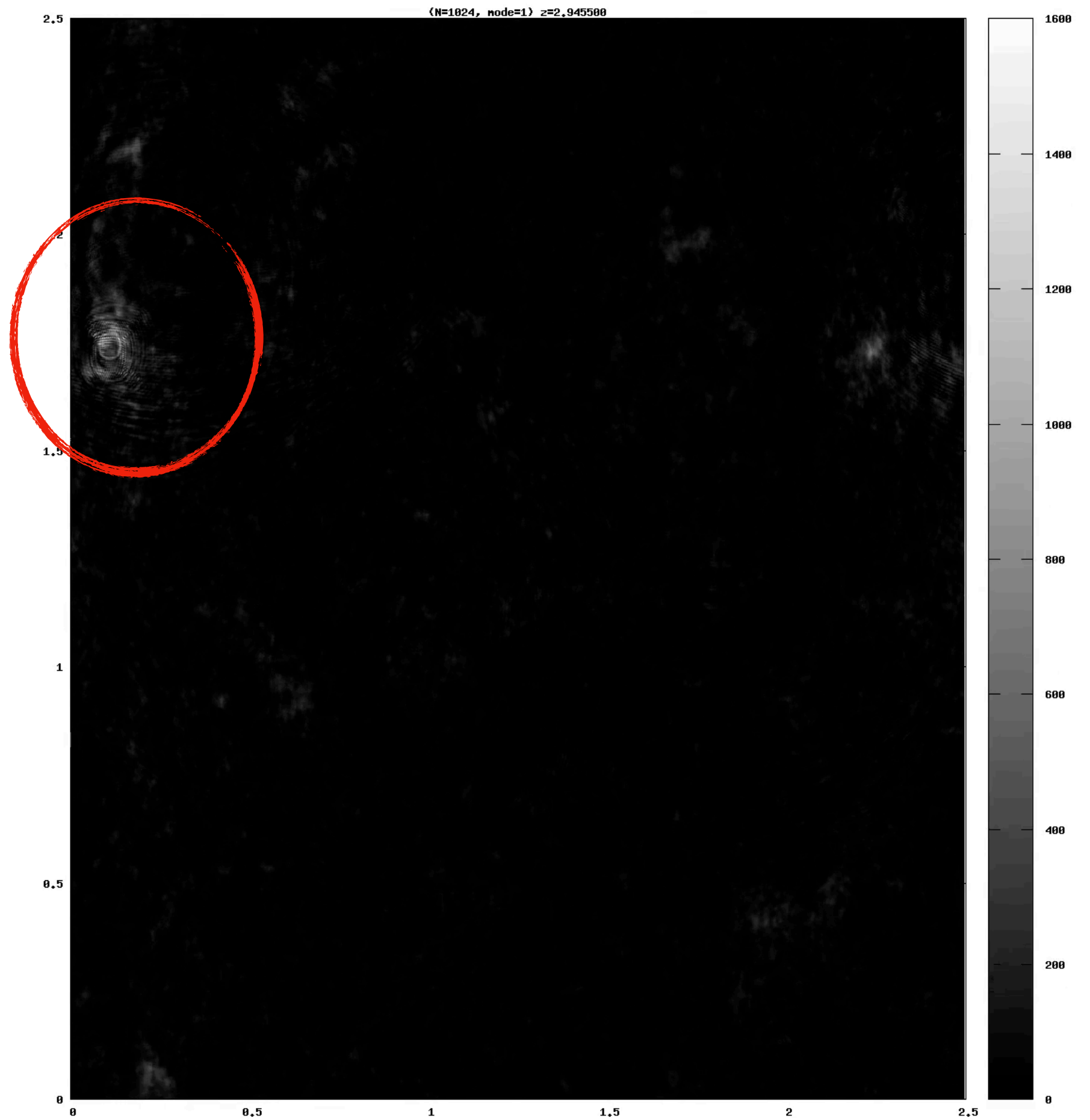
L=6, N=8192

Domain walls, string network collapse axitons



projection plots of density² (3D- $\rightarrow$ 2D)

axitons



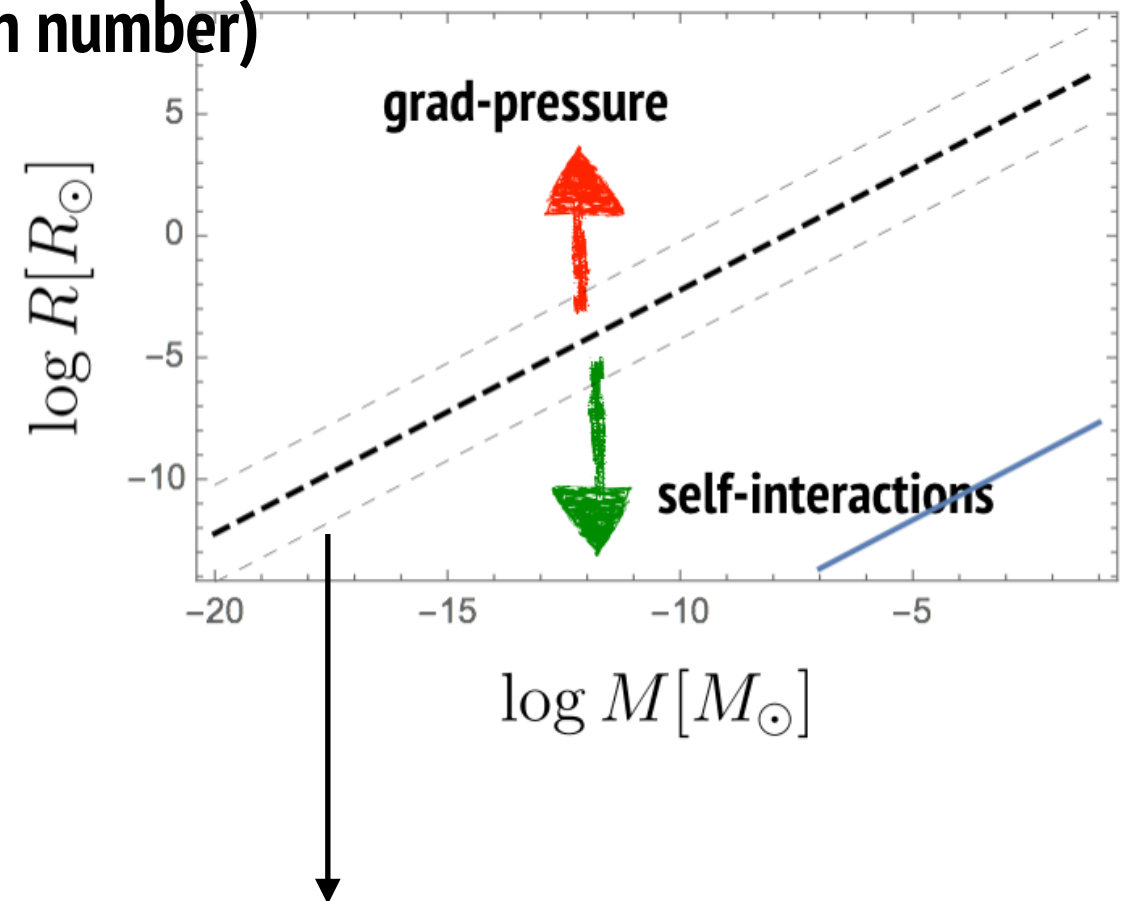
- The axion equation (Sine-Gordon) has a NR instability (**self interactions are attractive**)
- Energy of a axion Gaussian lump of size R (fixed axion number)

$$U = \int dV \left(\frac{1}{2} \dot{a}^2 + \frac{1}{2} m^2 a^2 + \frac{1}{2} (\nabla a)^2 - \text{grav} - \lambda a^4 + \dots \right)$$

$$U \sim M + \frac{M}{m^2 R^2} - \frac{GM^2}{R} - \lambda \frac{M^2}{m^4 R^3}$$

gradient pressure decreases energy expanding
gravity decreases energy contracting
self-interactions decrease energy contracting
FASTER THAN GRAD-PRESSURE

[sometimes called quantum pressure]



- Axitons start as **dense lumps below the critical line**
- They contract until $R \sim m_A$ and SI saturate
- They become pseudo-breathers
- They breathe emitting relativistic axions and finally relax
- In expanding Universe, they are fuelled by increasing axion masss they are resilient until axion mass saturates $R_{\text{end}} \sim m_A(\tau \sim 16) \ll H$

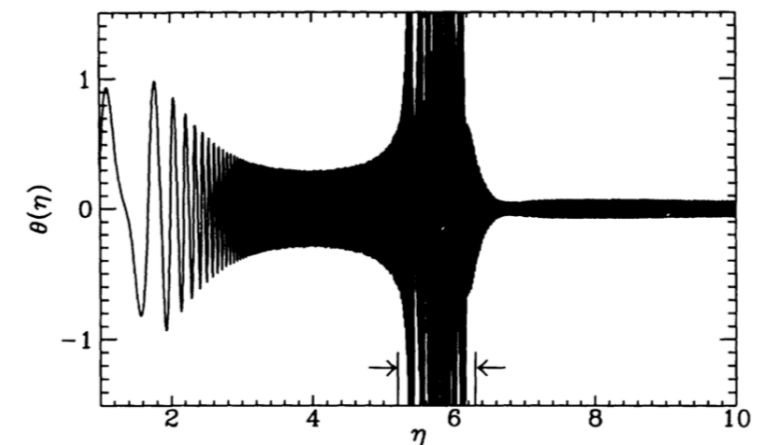


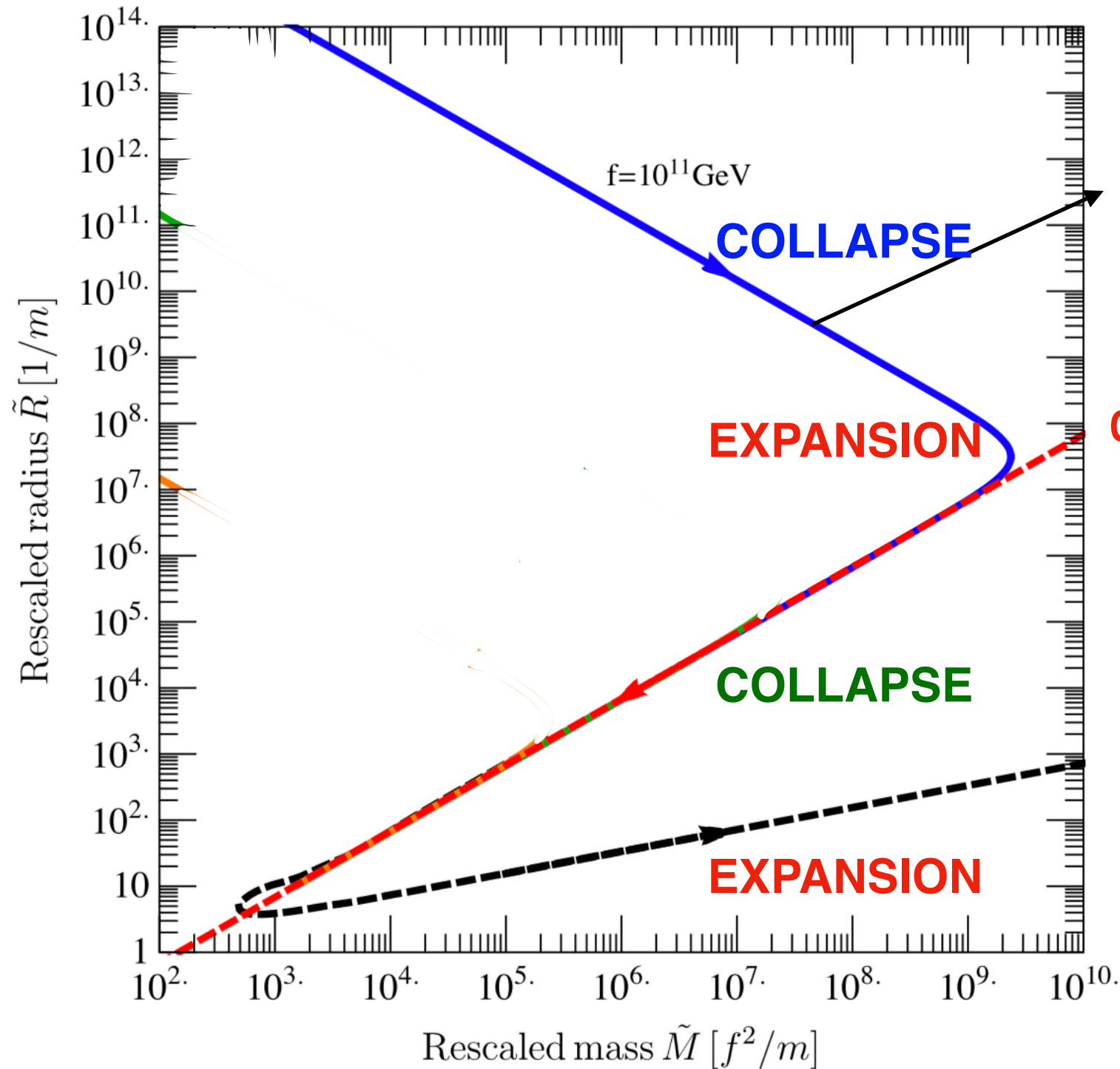
FIG. 8. The time dependence of θ in the center of an axiton in the (1+1)-dimensional calculation. The axiton was generated by the choice $A=0.77$.

Dilute and dense axion stars

Visinelli et al 2017

Axion star radius vs mass

$$\frac{1}{m} = 3 \times 10^{-11} R_{\odot} \left(\frac{10^{-5} \text{ eV}}{m} \right),$$



DILUTE axion-stars

Equilibrium between gravity and quantum pressure

Kaup 68, Ruffini 69, Tkachev 91

DENSE axion-stars

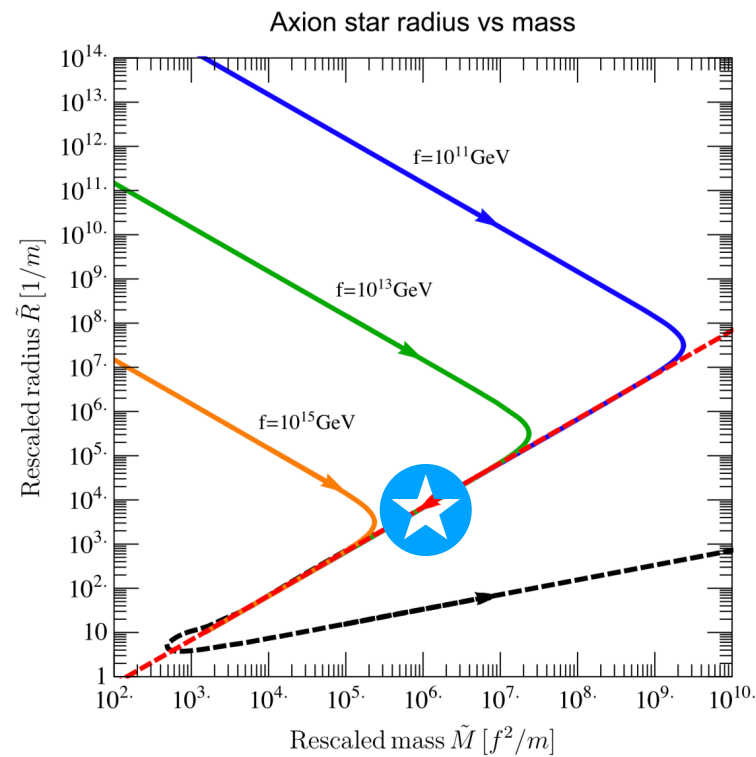
Equilibrium between Si and quantum pressure?
nope! lumps decay emitting relativistic axions!
relativistic + non-perturbative effects required
lifetimes $\sim 10^3\text{-}10^4 \text{ 1/mass}$

Braaten 2015 vs Visinelli 2017

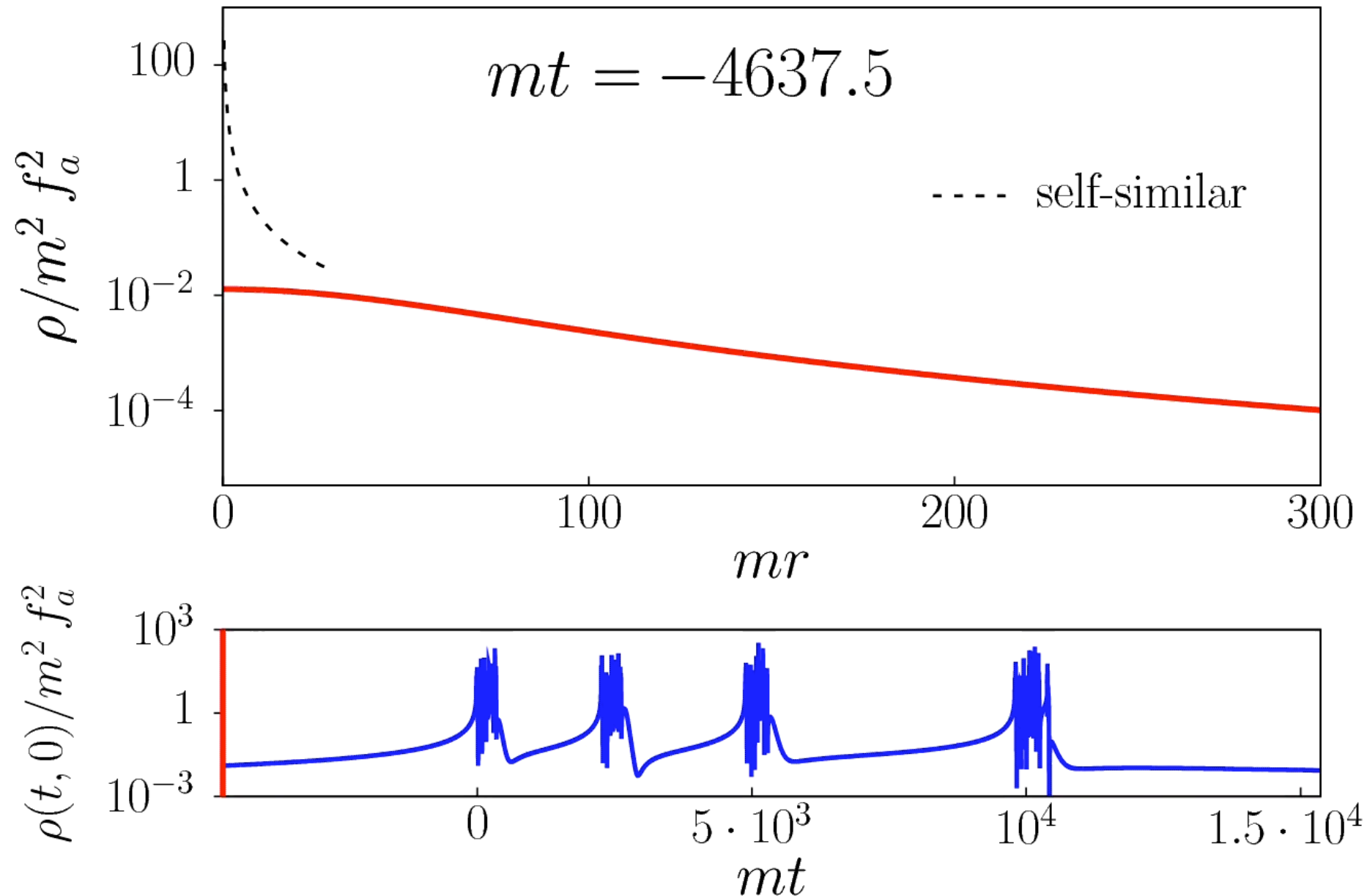
$$\frac{f^2}{m} = 3 \times 10^{-20} M_{\odot} \left(\frac{10^{-5} \text{ eV}}{m} \right)^3,$$

Collapse of a dilute axion star

Tkachev et al 2016

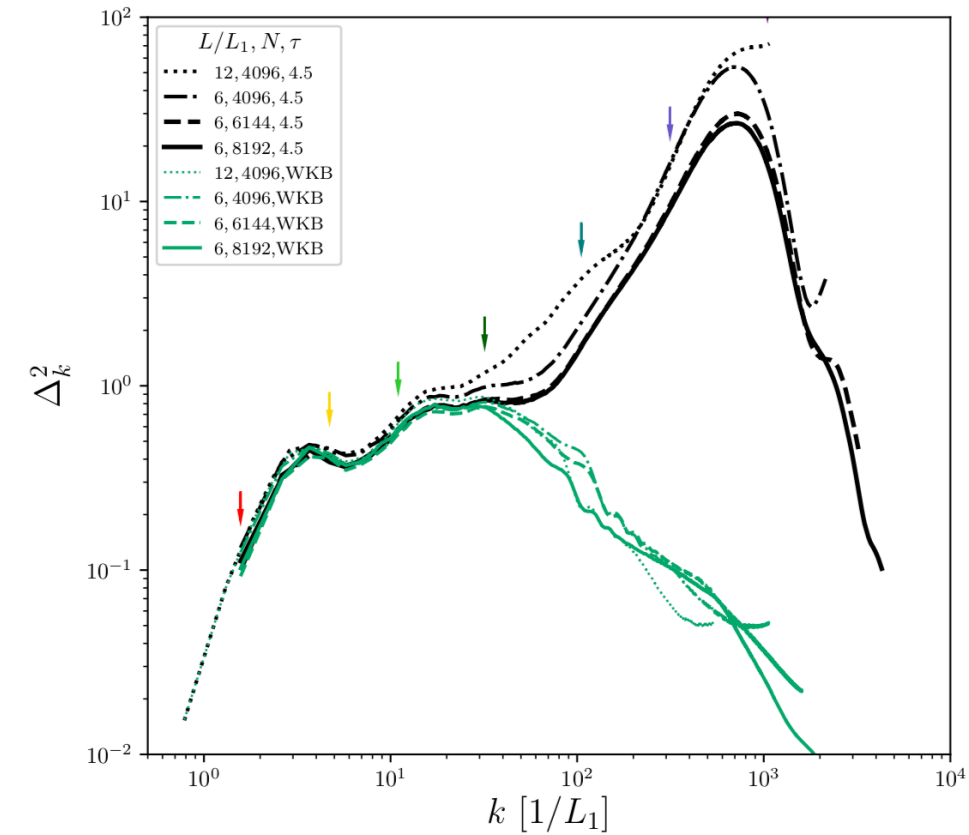
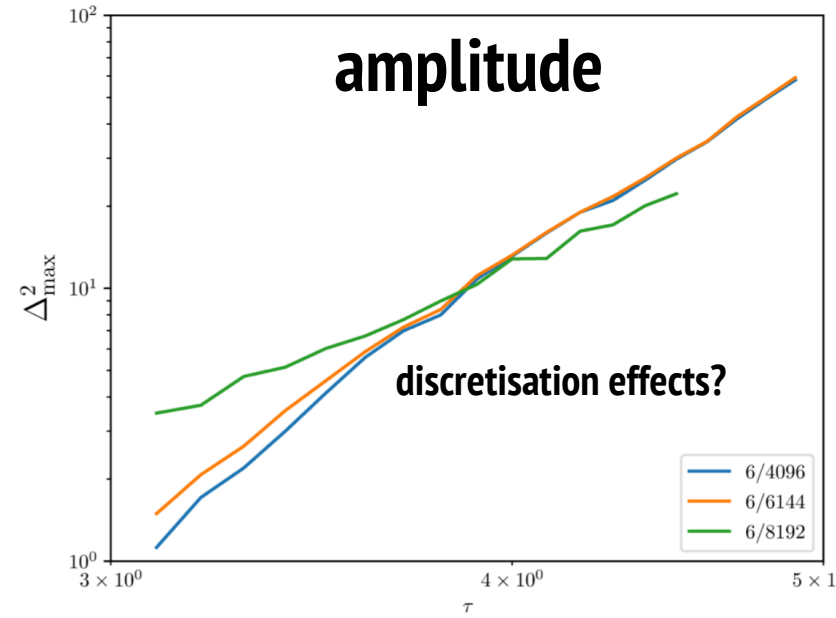
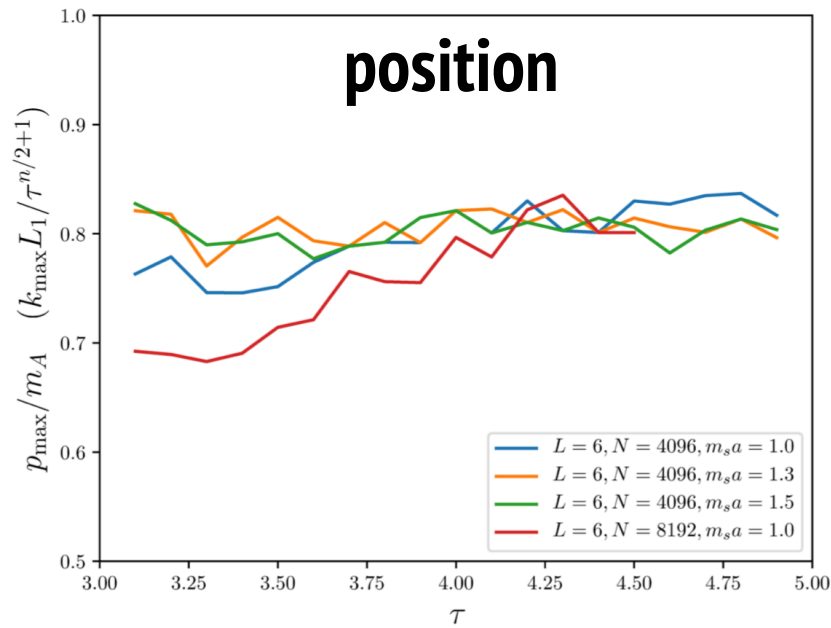


- Initial conditions slightly above critical mass
- Emission of relativistic axions



Axions in our simulations

Axion peak in the power spectrum

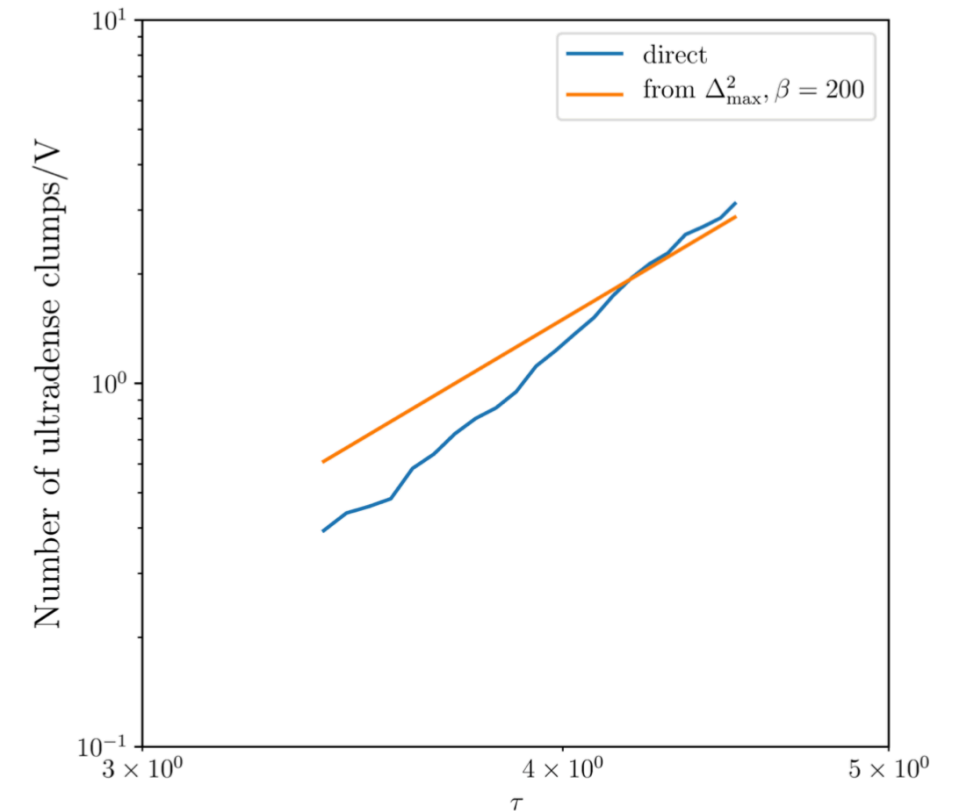


Number of axions increases tremendously

- Assuming uncorrelated positions ...

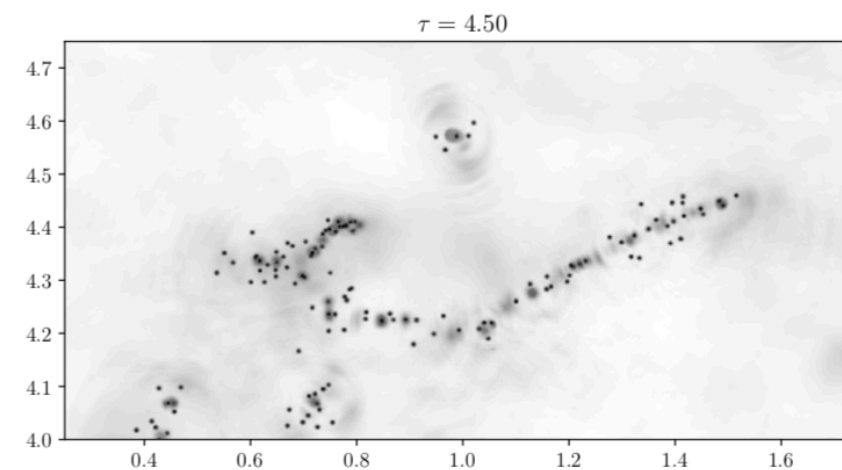
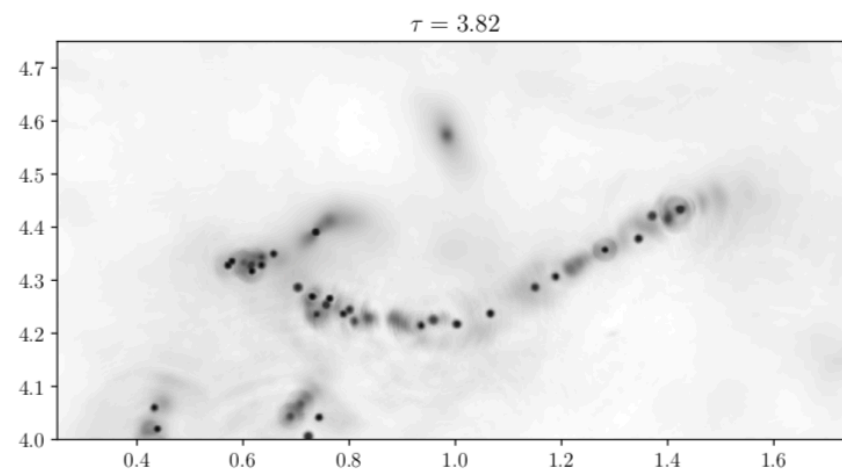
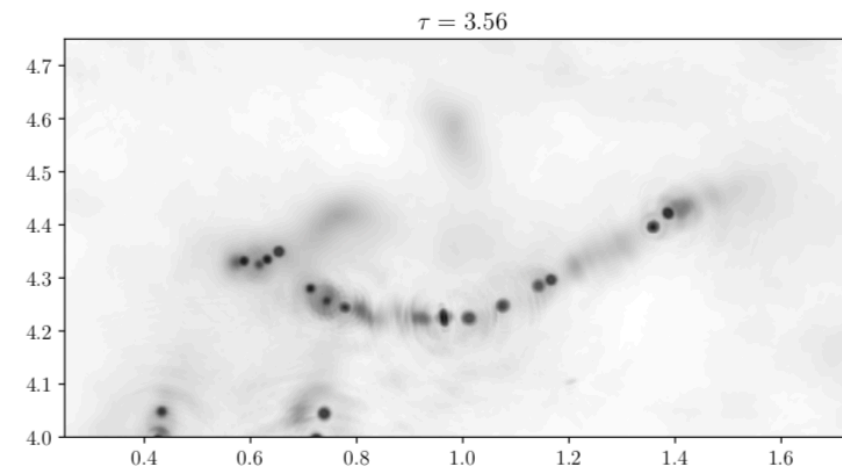
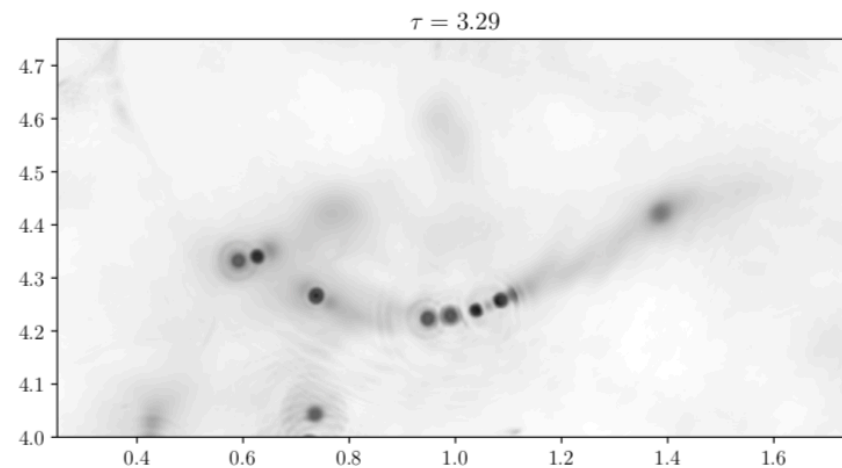
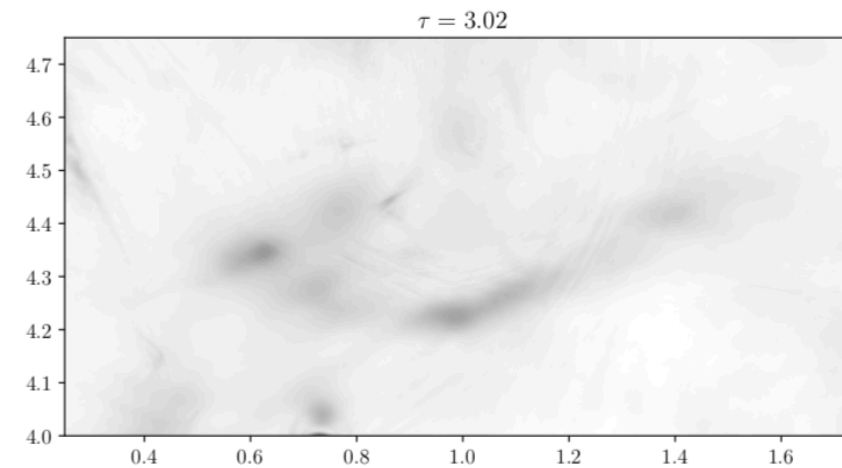
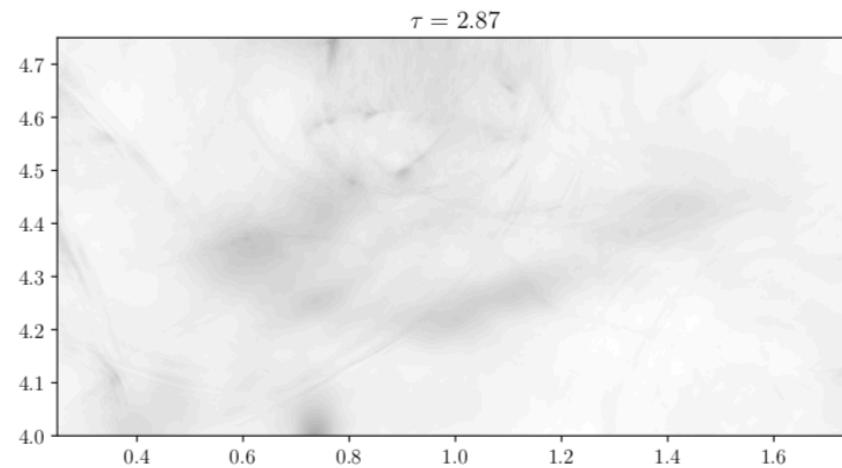
$$\frac{N_{\odot}}{V} \sim 2\pi^2 \Delta_{\odot}^2 \frac{125m_A^4}{k_{\odot}^3} \frac{1}{H_1 L_1^3} \sim 2.5 \times 10^3 \Delta_{\odot}^2 \tau^{n/2-3} \frac{1}{L_1^3}.$$

- Direct measurement



Axions are family people

Highly correlated, they appear in regions of large theta ... close to the last domain-walls collapsed?



Axions under control?

Axions convert NR axions into relativistic axions >



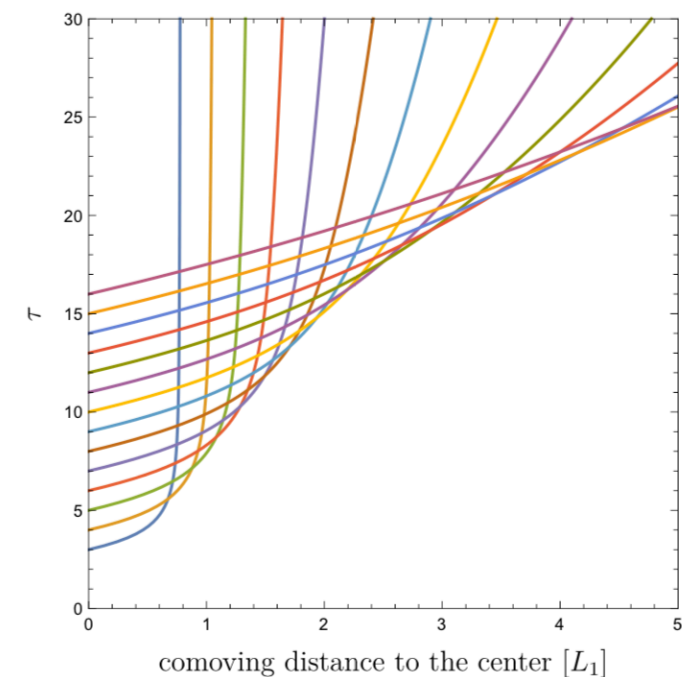
As time evolves, radius $\sim 1/m_A$ decreases (Volume and power too) and emitted energy $\gg H$

$$\frac{dN_e}{dt_e} \sim \frac{V_\odot \varrho_\odot \Gamma_\odot}{\omega_k} \sim \frac{m_A^{-3} (m_A^2 f_A^2) m_A \beta}{m_A},$$

$$\frac{dN_e}{d\tau_e} \sim \frac{f_A^2 \beta}{H_1^2} \frac{\tau_e}{\tau_e^{n/2}} \propto \tau_e^{1-n/2},$$

First emitted axions are most important

(are more abundant and free-stream less)



More on axion stars and axitons ...

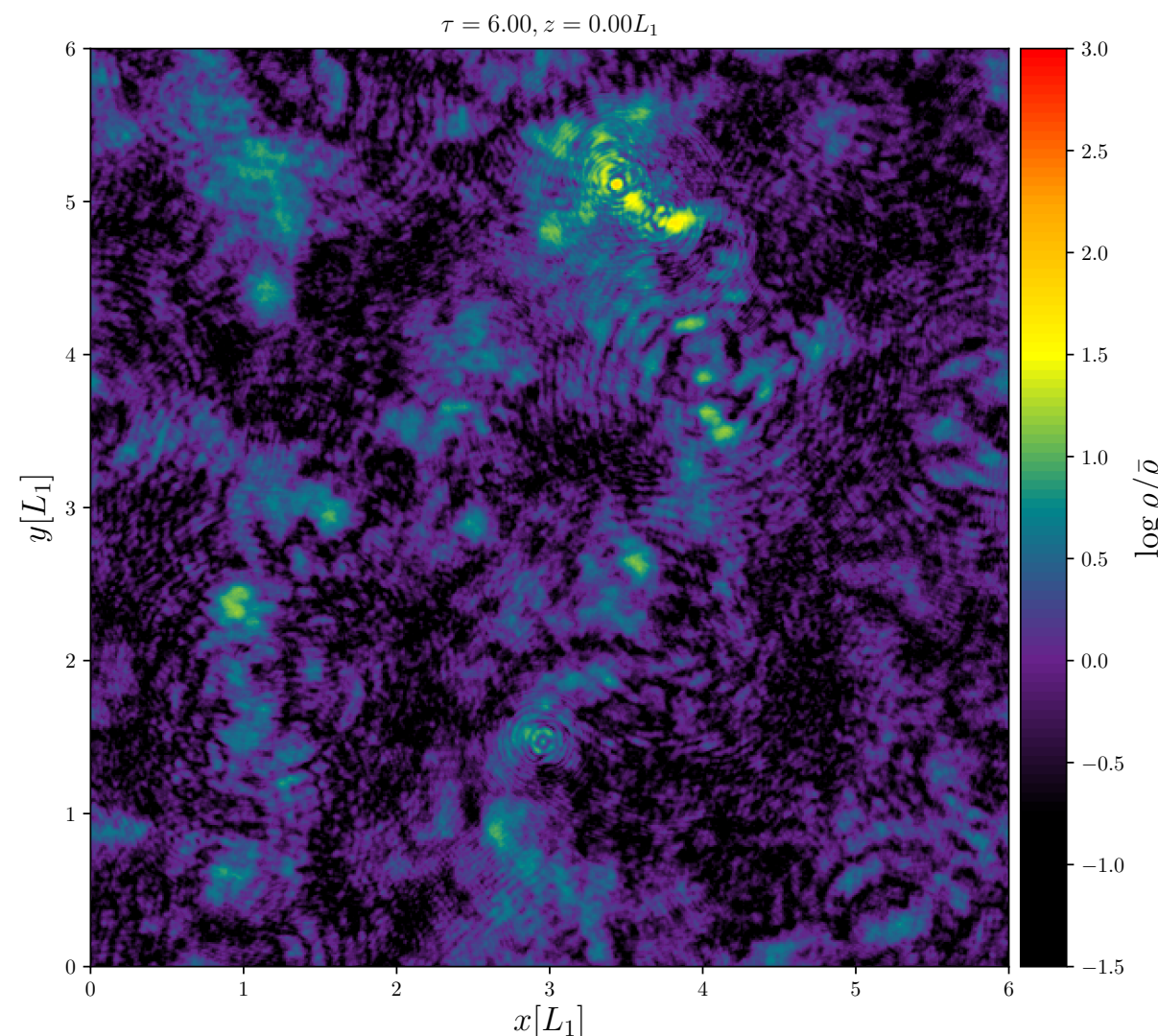
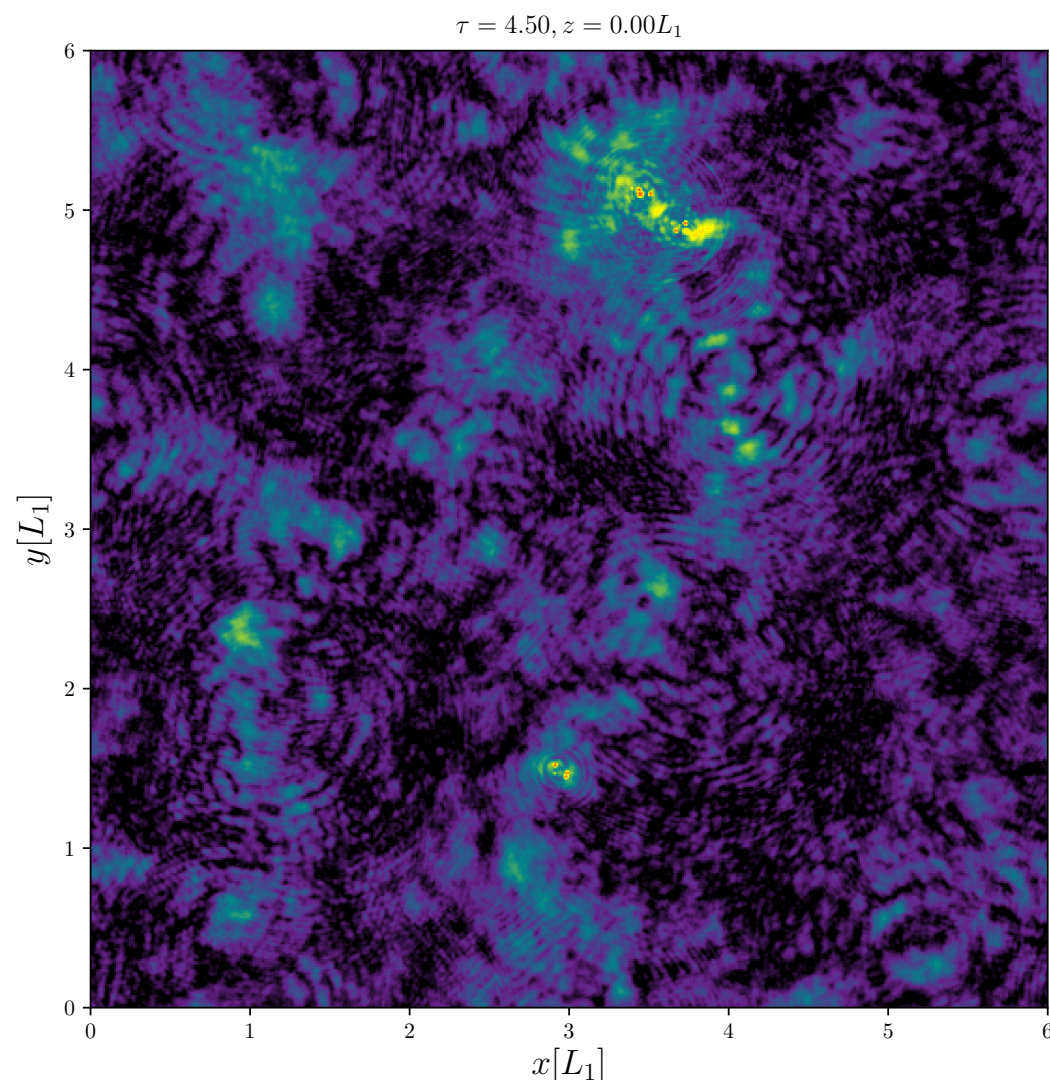
- **Huge overdensities at small scales -> largely diffuse away** *Vaquero, Stadler, JR 2018* **but some remnants...**
- **New studies to come** *Buschman, Safdi 2018?*

- **Relativistic axions from bose-star collapse** *Tkachev 2016*
- **Formation of bose stars in axion/ALP miniclusters** *Tkachev 2018, Niemeyer 2018*
- **Some astrophysical implications**
- **Lasing photons** *Hertzberg 2018*
- **Fast radio bursts** *Iwazaki 14, Raby 16*
-

WKBing the axitons away

- Axitons do not seem to alter large scales much after time ~ 4
- New axitons are small and relatively unimportant (although many could be produced)
- Axiton cores shrink in our simulations and eventually cannot be resolved $R_c \sim 1/m_A$
- Axions in axiton remnants will free-stream a long distance)

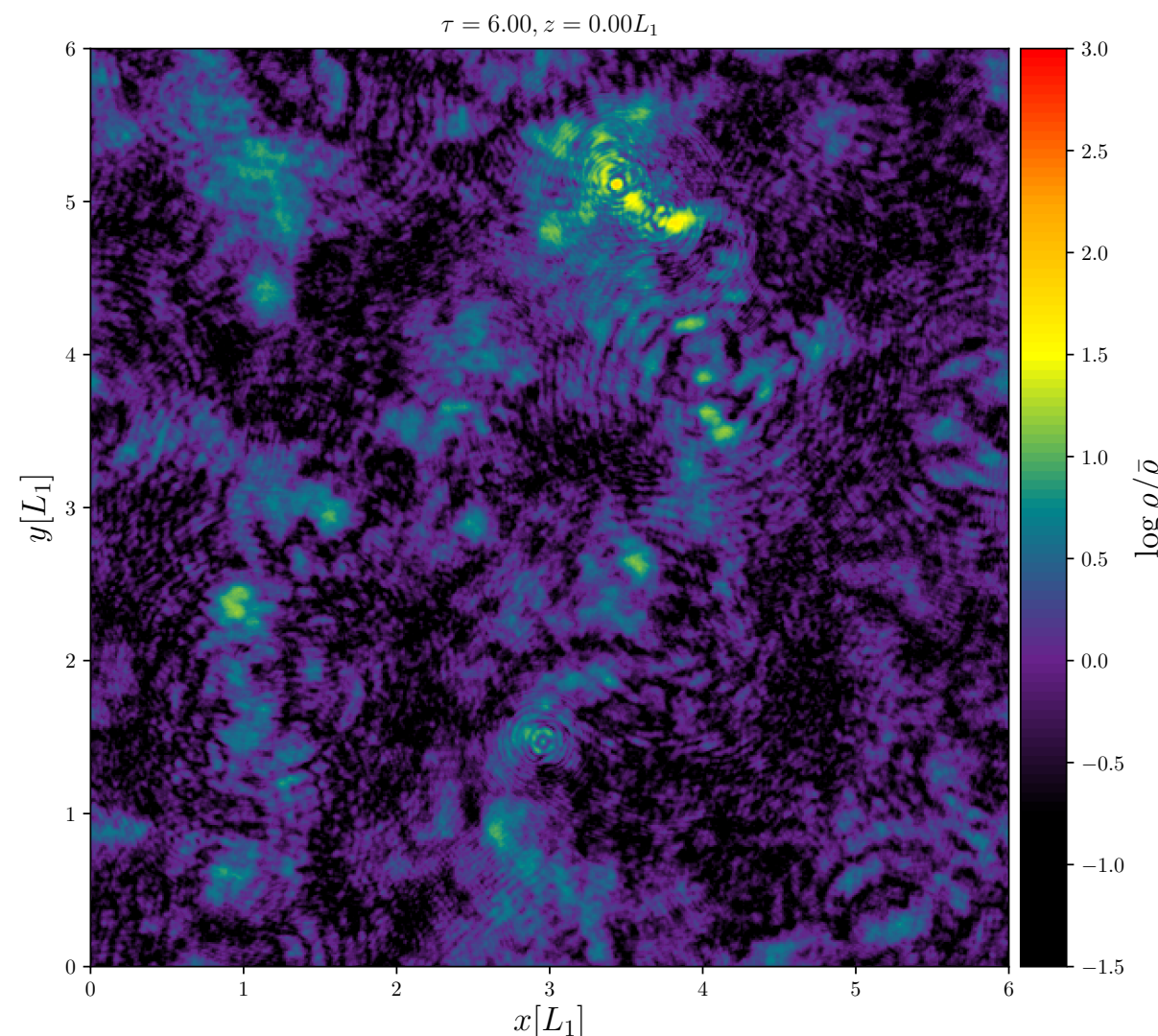
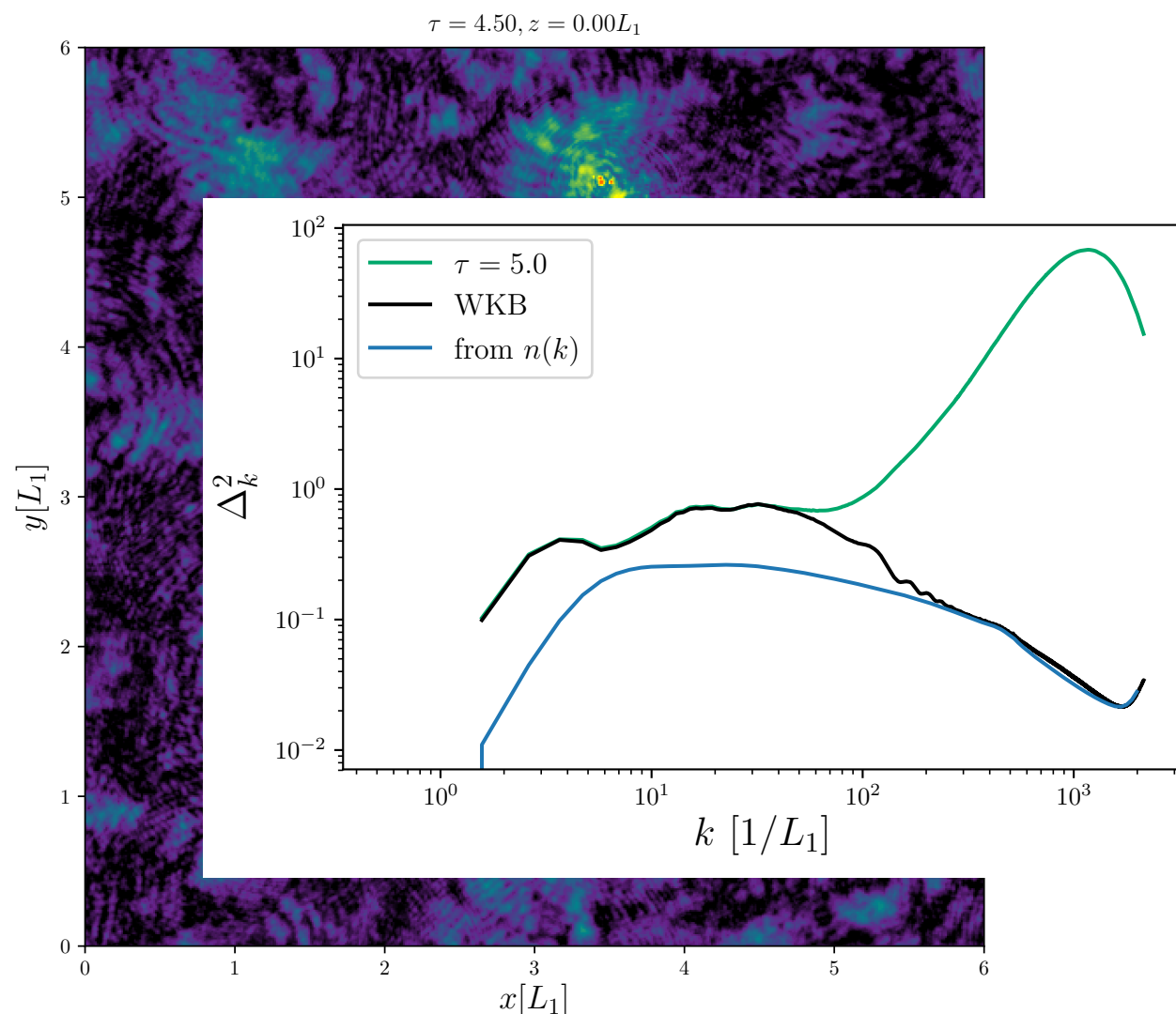
>>> we force them to free-stream at the end of our simulations (only impact at very small scales)



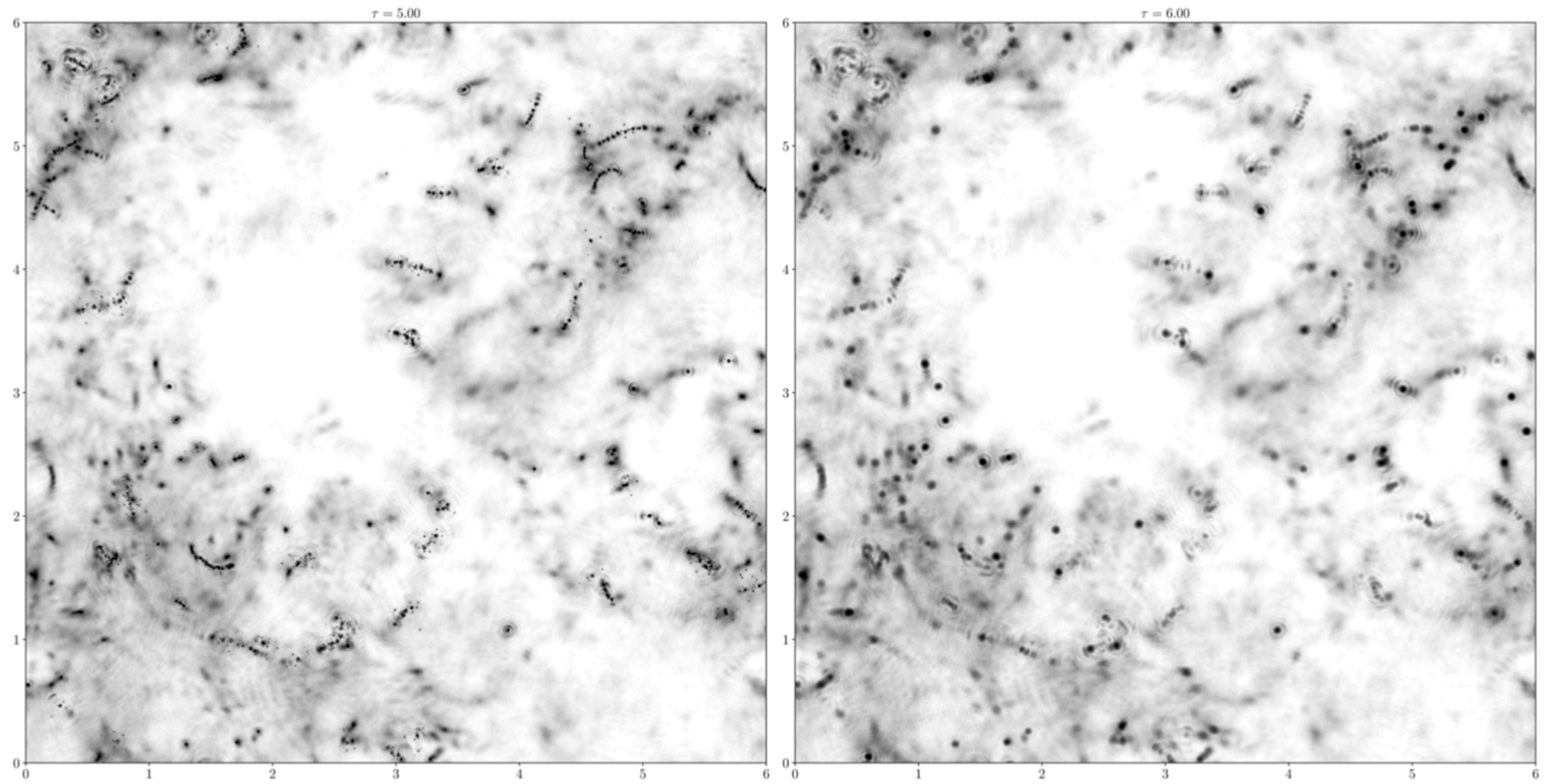
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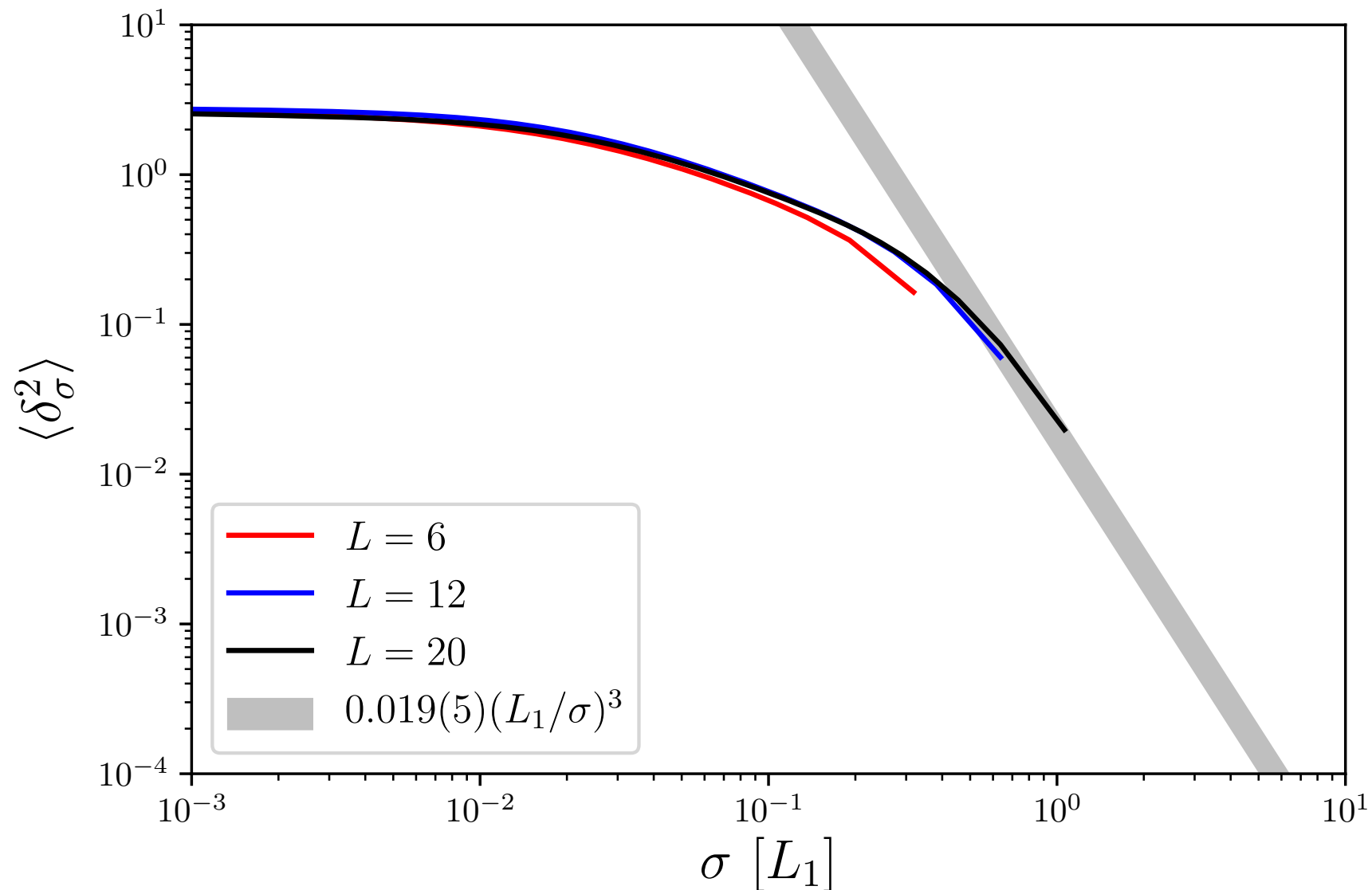


WKB

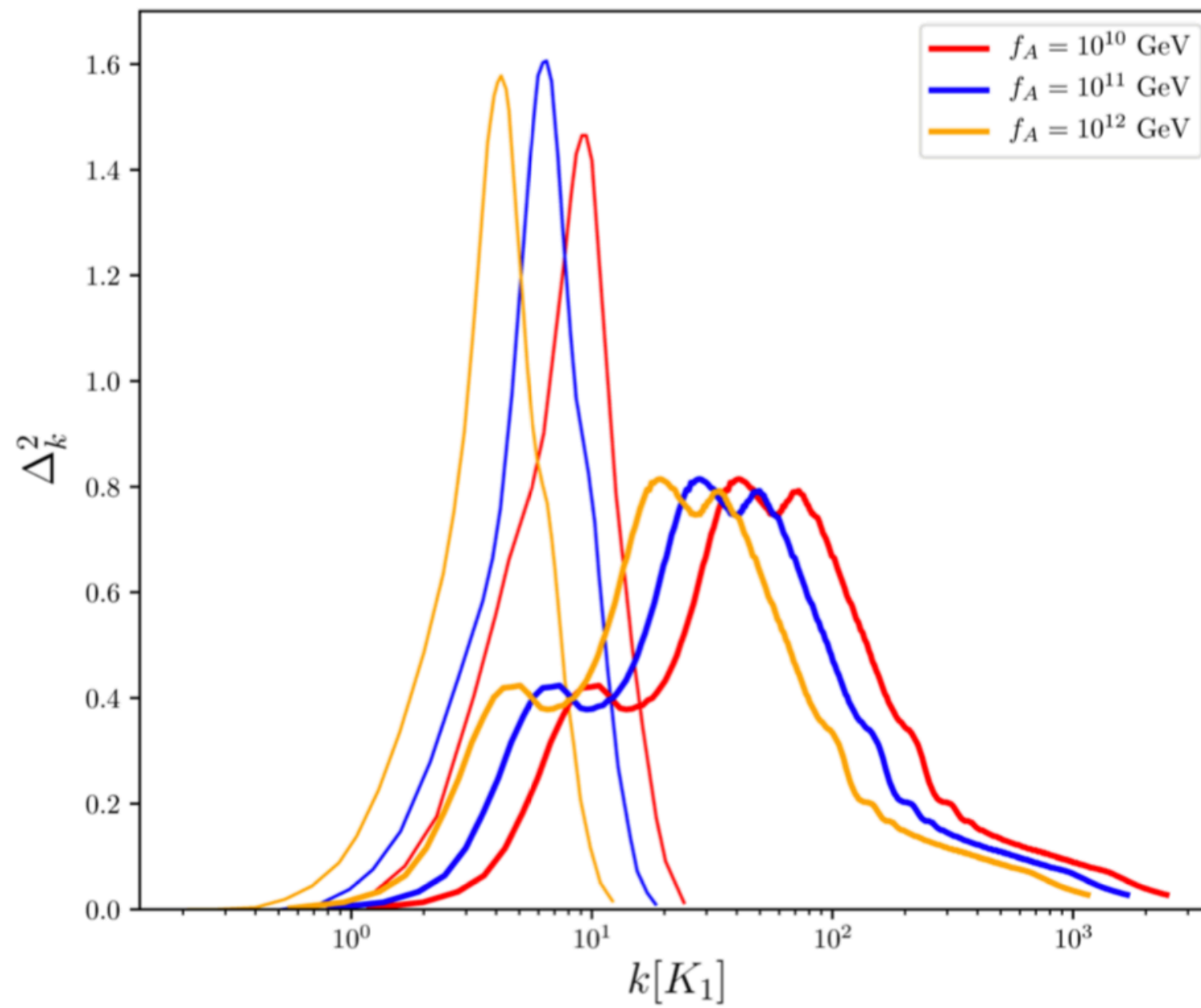


Typical fluctuation

- Density contrast averaged over a Gaussian window function of a given sigma
- Around $\sigma \sim L_1$, already in the white noise regime, very small "overdensities" at large scales
- Few high-density high-mass miniclusters expected
- Loads of high-density small-radius (small mass) Mcs!



Comparison to Tkachev-

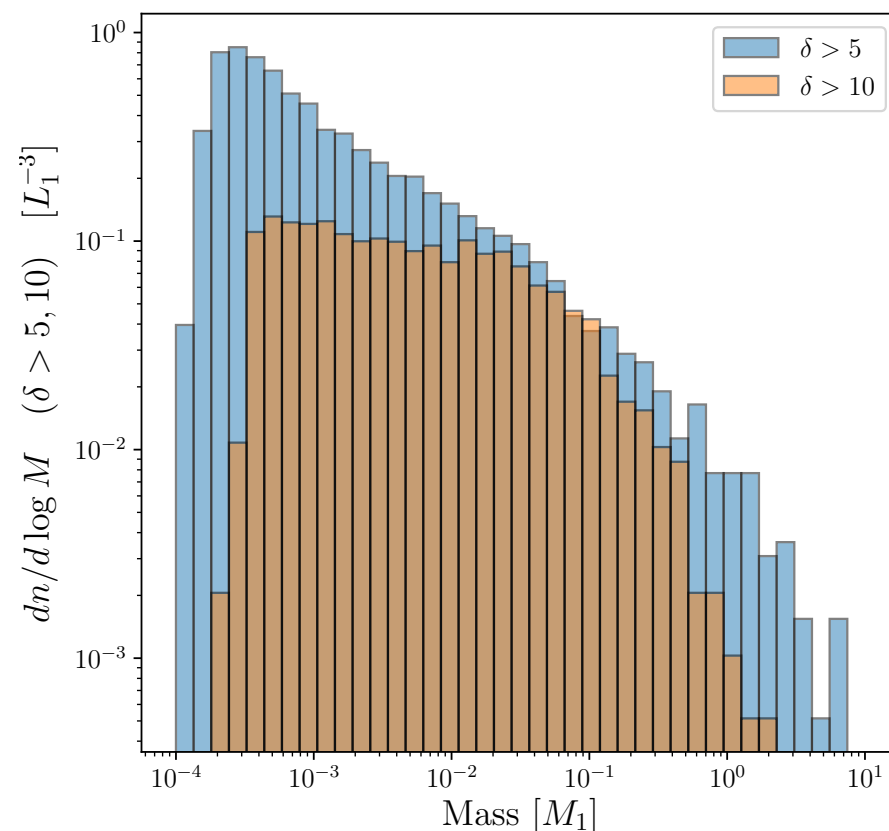


Distribution of Minicluster seeds

- If we want to talk about mass, we need to specify the amount of DM mass in L1
- It is output by our numerical simulations (function of m_a itself)
- Expressed as function of the axion DM fraction, it is

$$M_1 = 2.1 \times 10^{-12} M_{\odot} \frac{\Omega_{Ac} h^2}{0.12} \left(\frac{50 \mu\text{eV}}{m_a} \right)^{0.49}$$

- Distribution of seeds with all points more dense than 5, or 10



very few dense & large mass seeds

- Halo mass function needs the gravitational evolution

Conclusions and more

- New simulations of the axion dark matter field
- Study of the evolution of density perturbations at extremely small scales > non-trivial
- **Role of axitons** at high-k unhappily avoided > ultradense clumps?*
- Final density at **large scales** seems little affected by uncertainties (the ones we can simulate!)
- First estimates of minicluster mass and distribution with **"correct" initial conditions!**
- Study of minicluster seeds > many small seeds, large seeds are not very dense
- Gravitational evolution (N-body) with Enzo and Gadget
- Confirms estimates of typical minicluster mass
- $O(1)$ DM mass unbound
- HMF steeper than $1/M^{0.5}$
- Many low mass miniclusters not previously considered (dominate number, but not mass)
- Smallest and densest clusters (presumably cores of large MCs) require wave-evolution