

Topical Seminar on Frontiers of Particle Physics 2002: Neutrinos and Cosmology  
Yun Hu Holiday Resort of Mi Yun, Beijing, China (20-25 August 2002)

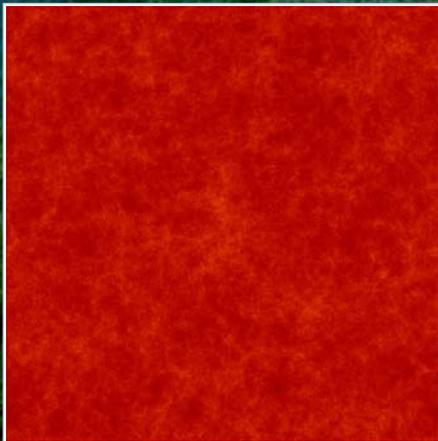
# Neutrino Astrophysics

Georg G. Raffelt

Max-Planck-Institut für Physik, München, Germany



**Lecture I:  
Physics with Supernovae**



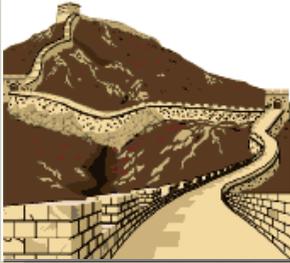
**Lecture II:  
Cosmological Neutrinos**

# Status of Evidence for Neutrino Oscillations

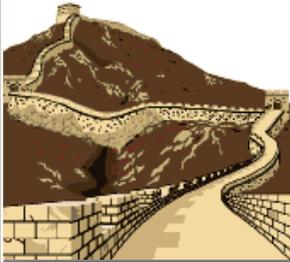
System	Atmospheric	Solar	LSND
Channel	$\nu_\mu \rightarrow \nu_\tau$	$\nu_e \rightarrow \nu_{\mu\tau}$	$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$
$\delta m^2 / eV^2$	$(1.5 - 4) \times 10^{-3}$	LMA $(0.2 - 2) \times 10^{-4}$	0.2-2
$\sin^2 2\theta$	0.9-1	0.2-0.6	0.001-0.03
Status	Established	Established	Unconfirmed
Mutually inconsistent with 3 mass eigenstates			
Test	Long Baseline (K2K)	KamLAND 2002 ?	MiniBooNE 2004 ?
Simplest interpretation	Three mass eigenstates with $m_1 \ll m_2 \ll m_3 \sim 50 \text{ meV}$ (hierarchical) $m_1 \sim m_2 \sim m_3 \gg 50 \text{ meV}$ (degenerate)		Experimental Fluke

**What is the absolute neutrino mass scale  $m_\nu$ ?**

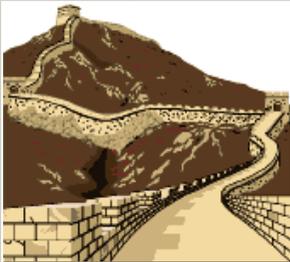
# Lecture II: Cosmological Neutrinos



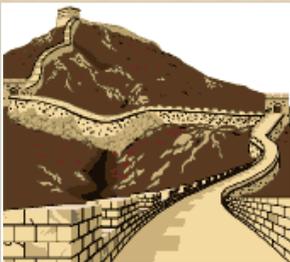
**Neutrino Dark Matter and  
Cosmic Structure Formation**



**Neutrino Chemical Potentials,  
Big-Bang Nucleosynthesis,  
and Flavor Oscillations**



**Highest-Energy Cosmic Rays  
and the Cosmic Neutrino Sea**



**Massive Neutrinos and the  
Cosmic Baryon Asymmetry**

# Cosmological Limit on Neutrino Masses

Cosmic neutrino "sea"  $\sim 112 \text{ cm}^{-3}$  neutrinos + anti-neutrinos per flavor

$$\Omega_\nu h^2 = \sum \frac{m_\nu}{94 \text{ eV}} < 0.4$$

$$m_\nu < 40 \text{ eV}$$

For all  
stable flavors

## REST MASS OF MUONIC NEUTRINO AND COSMOLOGY

S. S. Gershtein and Ya. B. Zel'dovich

Submitted 4 June 1966

ZhETF Pis'ma 4, No. 5, 174-177, 1 September 1966

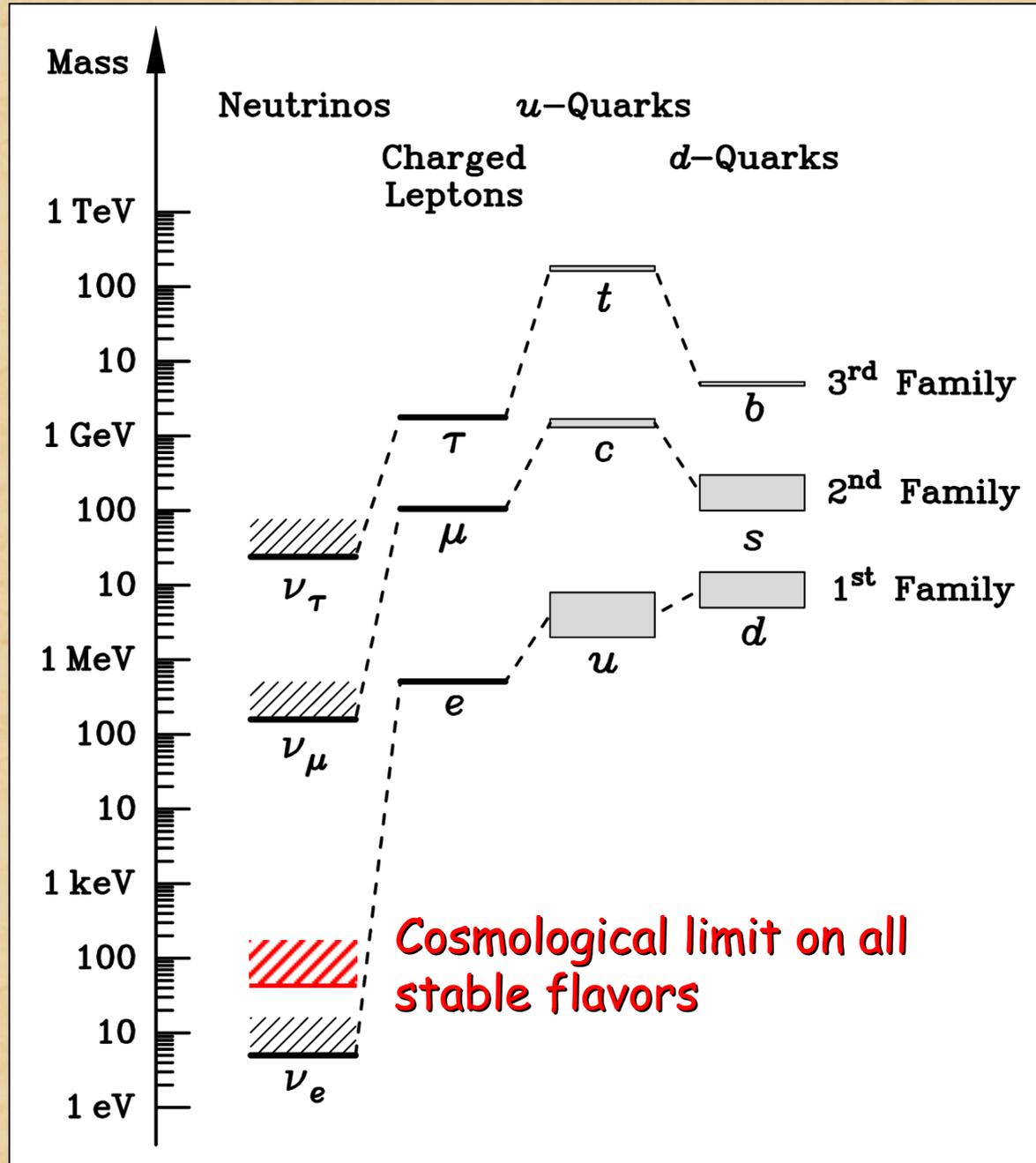
Low-accuracy experimental estimates of the rest mass of the neutrino [1] yield  $m(\nu_e) < 200 \text{ eV}/c^2$  for the electronic neutrino and  $m(\nu_\mu) < 2.5 \times 10^6 \text{ eV}/c^2$  for the muonic neutrino.

Cosmological considerations connected with the hot model of the Universe [2] make it possible to strengthen greatly the second inequality. Just as in the paper by Ya. B. Zel'dovich and Ya. A. Smorodinskii [3], let us consider the gravitational effect of the neutrinos on the dynamics of the expanding Universe. The age of the known astronomical objects is not smaller than  $5 \times 10^9$  years, and Hubble's constant  $H$  is not smaller than  $75 \text{ km/sec-Mparsec} = (13 \times 10^9 \text{ years})^{-1}$ . It follows therefore that the density of all types of matter in the Universe is at the present time <sup>1)</sup>

$$\rho < 2 \times 10^{-28} \text{ g/cm}^3.$$

A classic paper:  
Gershtein & Zeldovich  
JETP Lett. 4 (1966) 120

# Fermion Mass Spectrum



# Weakly Interacting Particles as Dark Matter

THE ASTROPHYSICAL JOURNAL, 180: 7-10, 1973 February 15  
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## GRAVITY OF NEUTRINOS OF NONZERO MASS IN ASTROPHYSICS

R. COWSIK\* AND J. MCCLELLAND  
Department of Physics, University of California, Berkeley  
Received 1972 July 24

### ABSTRACT

If neutrinos have a rest mass of a few eV/c<sup>2</sup>, then they would dominate the gravitational dynamics of the large clusters of galaxies and of the Universe. A simple model to understand the virial mass discrepancy in the Coma cluster on this basis is outlined.

*Subject headings:* cosmology — galaxies, clusters of — neutrinos

The possibility of a finite rest mass for the neutrinos has fascinated astrophysicists (Kuchowicz 1969). A recent discussion of such a possibility has been in the context of the solar-neutrino experiments (Bahcall, Cabibbo, and Yahil 1972). Here we wish to point out some interesting consequences of the gravitational interactions of such neutrinos. These considerations become particularly relevant in the framework of big-bang cosmologies which we assume to be valid in our discussion here.

In the early phase of such a Universe when the temperature was ~1 MeV, several processes of neutrino production (Ruderman 1969) would have led to copious production of neutrinos and antineutrinos (Steigman 1972; Cowsik and McClelland 1972). Conditions of thermal equilibrium allow an easy estimate of their number densities (Landau and Lifshitz 1969):

$$n_{\nu i} = \frac{1}{\pi^2 \hbar^3} \int_0^\infty \frac{p^2 dp}{\exp [E/kT(z_{\text{eq}})] + 1} \quad (1)$$

Here  $n_{\nu i}$  = number density of neutrinos of the  $i$ th kind (notice that in writing this expression we have assumed that both the helicity states are allowed for the neutrinos because of finite rest mass);  $E = c(p^2 + m^2 c^2)^{1/2}$ ;  $k$  = Boltzmann's constant;  $T(z_{\text{eq}}) = T_r(z_{\text{eq}}) = T_e(z_{\text{eq}}) = T_\nu(z_{\text{eq}}) \dots$  = the common temperature of radiation, neutrinos, electrons, etc., at the latest epoch characterized by redshift  $z_{\text{eq}}$  when they may be assumed to have been in thermal equilibrium;  $kT(z_{\text{eq}}) \simeq 1$  MeV.

Since the masses of the neutrinos are expected to be small,  $kT(z_{\text{eq}}) \gg m_{\nu i} c^2$ , in the extreme-relativistic limit equation (1) reduces to

$$n_{\nu i}(z_{\text{eq}}) \simeq 0.183 [T(z_{\text{eq}})/hc]^3 \quad (2)$$

As the Universe expands, only the neutrinos (in contrast to all other known particles) survive annihilation because of extremely low cross-sections (deGraff and Tolhock 1966), and their number density decreases with increasing volume of the Universe, simply as  $\sim V(z_{\text{eq}})/V(z) = [(1+z)/(1+z_{\text{eq}})]^3$ . Noting that  $(1+z_{\text{eq}})/(1+z) = T_r(z_{\text{eq}})/T_r(z)$ , the number density at the present epoch ( $z = 0$ ) is given by

$$n_{\nu i}(0) = n_{\nu i}(z_{\text{eq}})/(1+z_{\text{eq}})^3 \simeq 0.183 [T_r(0)/hc]^3 \simeq 300 \text{ cm}^{-3} \quad (3)$$

\* On leave from the Tata Institute of Fundamental Research, Bombay, India.

Almost 30 years ago,  
beginnings of the idea of  
weakly interacting particles  
(neutrinos) as dark matter

Massive neutrinos are no  
longer a good candidate  
(hot dark matter)

However, the idea of  
weakly interacting massive  
particles as dark matter  
is now standard

# What is wrong with neutrino dark matter?

## Galactic Phase Space ("Tremaine-Gunn-Limit")

Maximum mass density of a Fermi gas

$$\rho_{\max} = m_\nu n_{\max} = m_\nu p_{\max}^3 / 3\pi^2 = m_\nu (m_\nu v_{\text{escape}})^3 / 3\pi^2$$

$m_\nu > 20 - 40 \text{ eV}$       Spiral galaxies

More restrictive from dwarf galaxies  
 $m_\nu > 100 - 200 \text{ eV}$

## Neutrino Free Streaming (Collisionless Phase Mixing)

- At  $T < 1 \text{ MeV}$  neutrino scattering in early universe ineffective
- Stream freely until nonrelativistic
- Wash out density contrasts on small scales

Neutrinos

Neutrinos

Over-density

- Nus are "Hot Dark Matter"
- Ruled out by structure formation

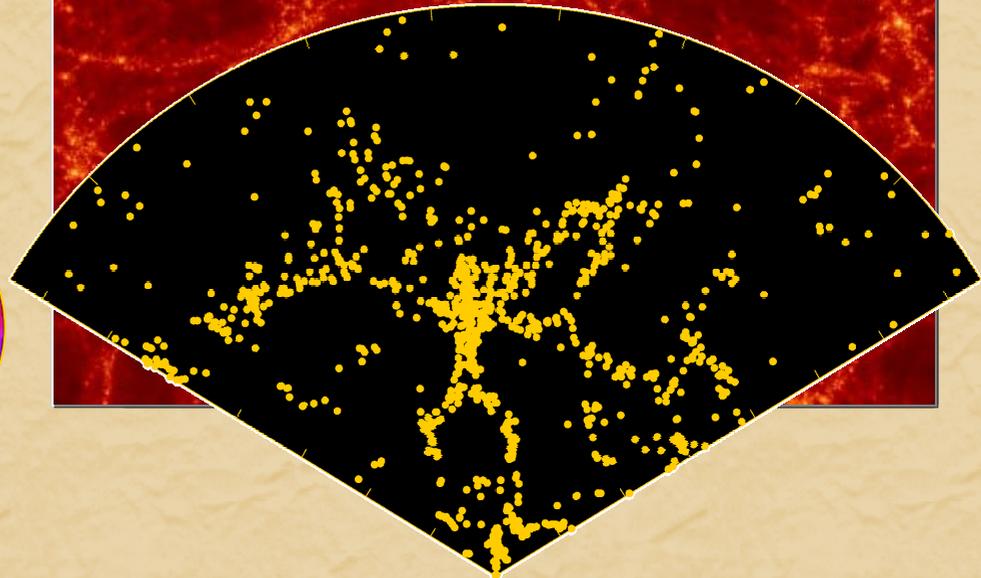
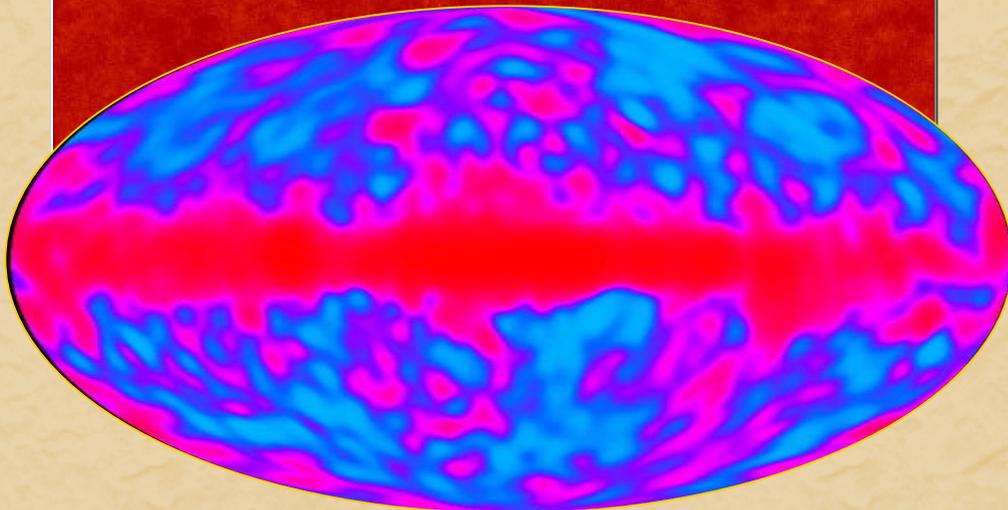
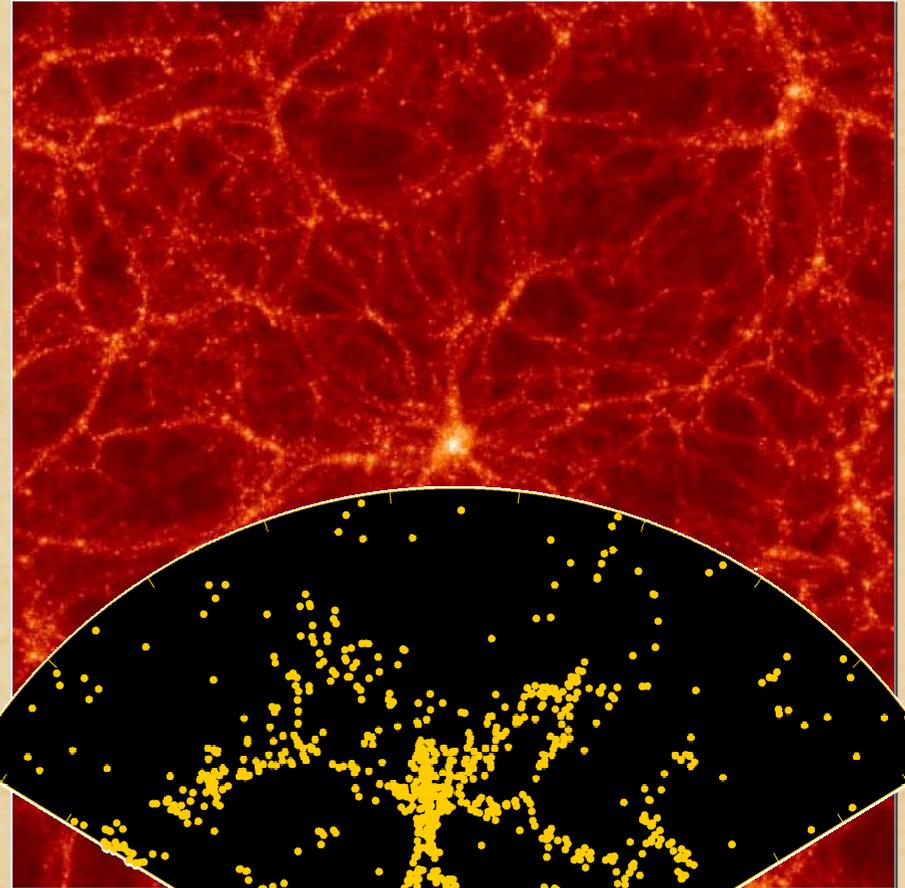
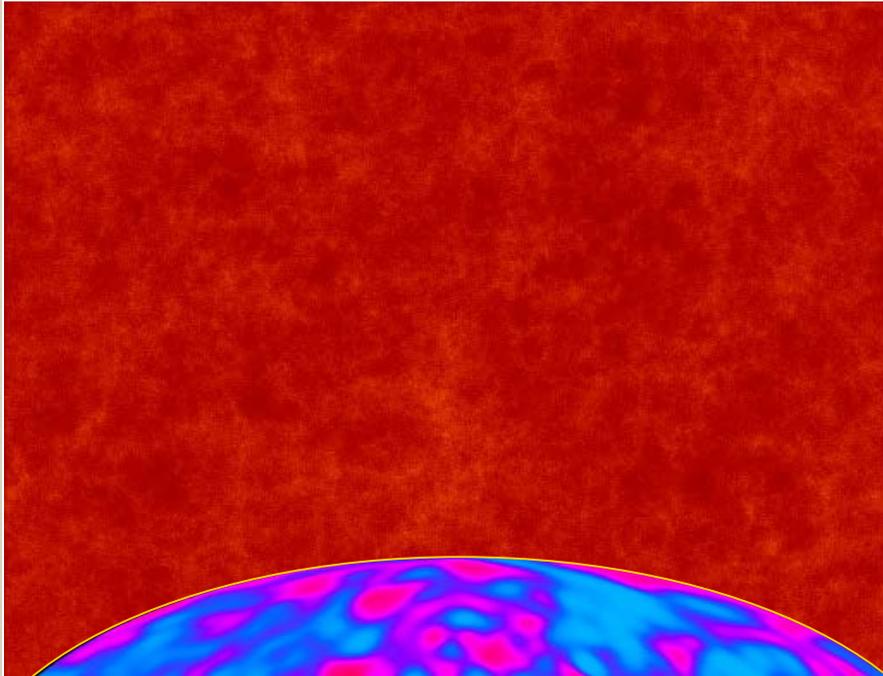
# Formation of Structure

Numerical Simulation Max-Planck-Institut für Astrophysik, Garching

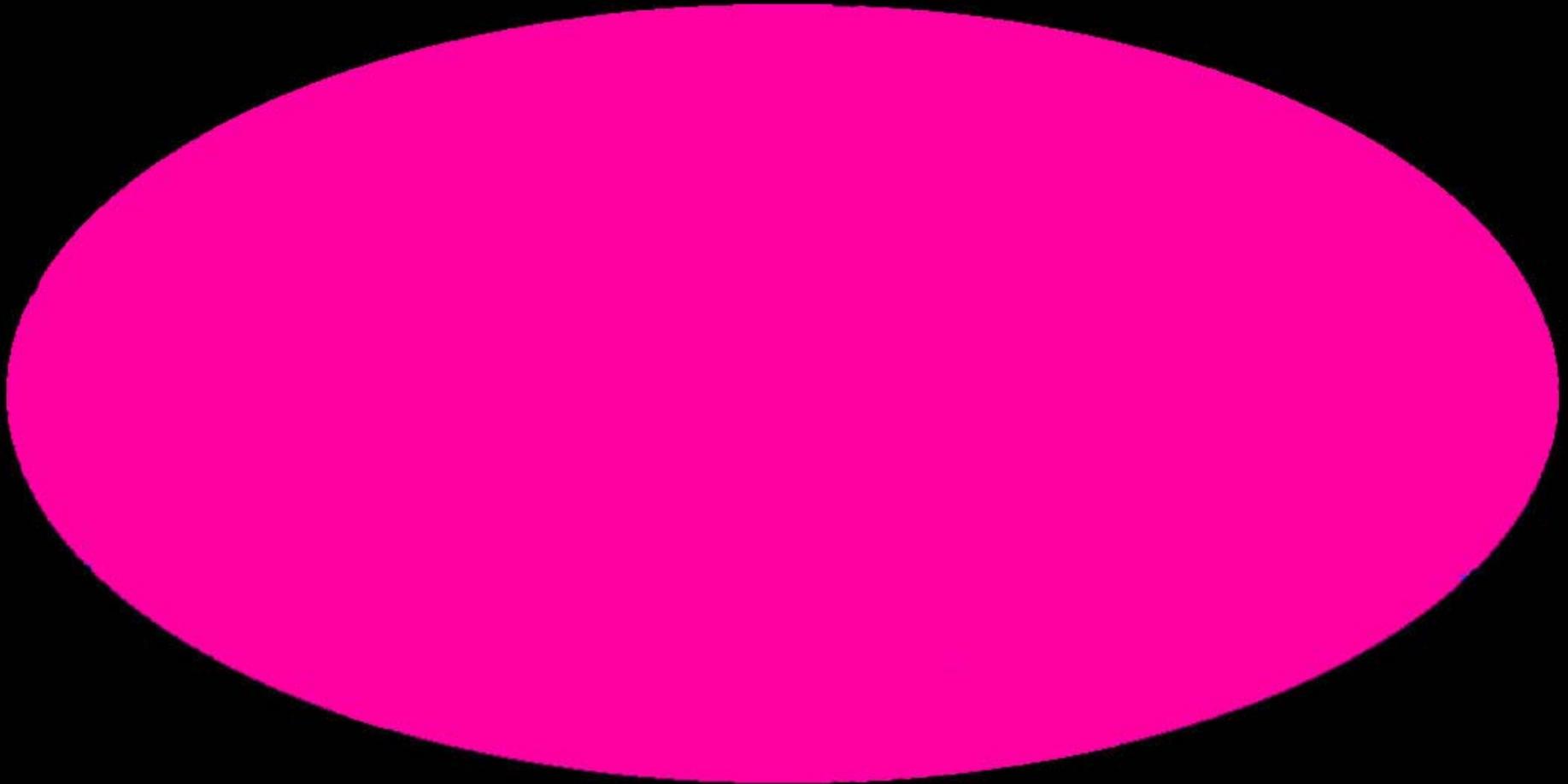
Smooth



Structured

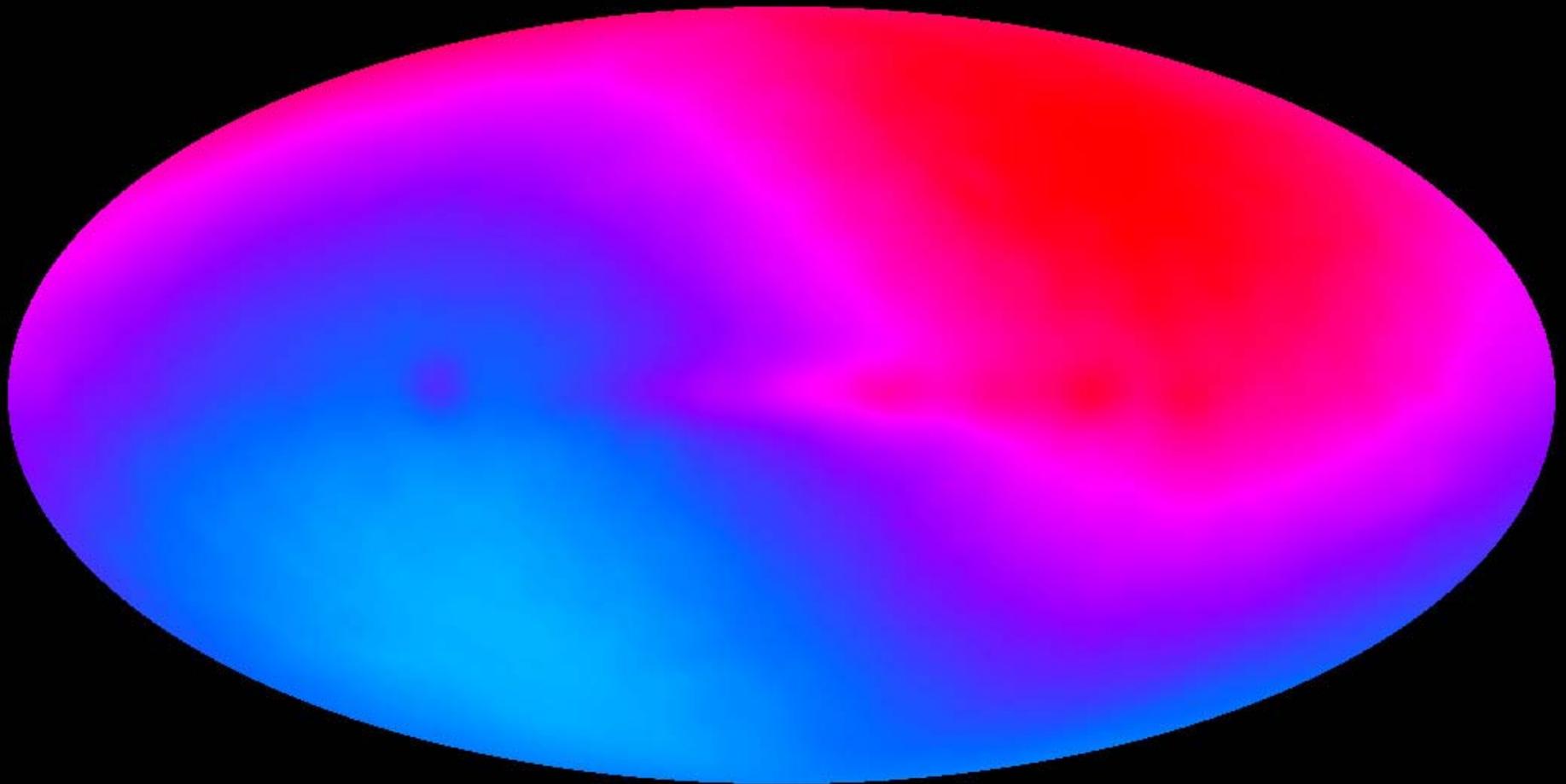


# COBE Sky Map of the CMBR Temperature



$T = 2.728 \text{ K}$  (uniform on the sky)

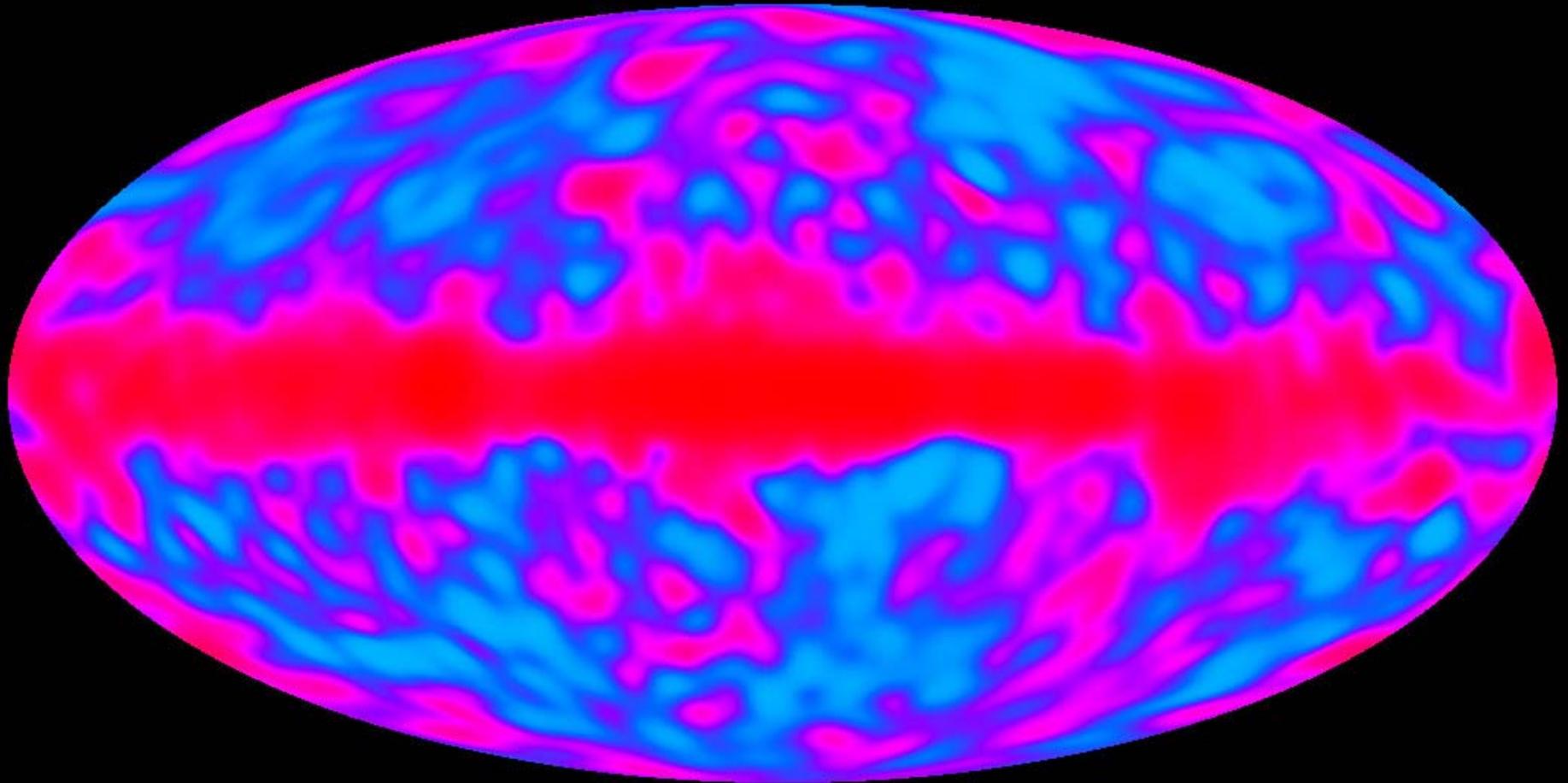
# COBE Sky Map of the CMBR Temperature



**Dynamical range  $\Delta T = 3.353$  mK**

**Dipole temperature distribution from Doppler effect due to our motion relative to the cosmic frame**

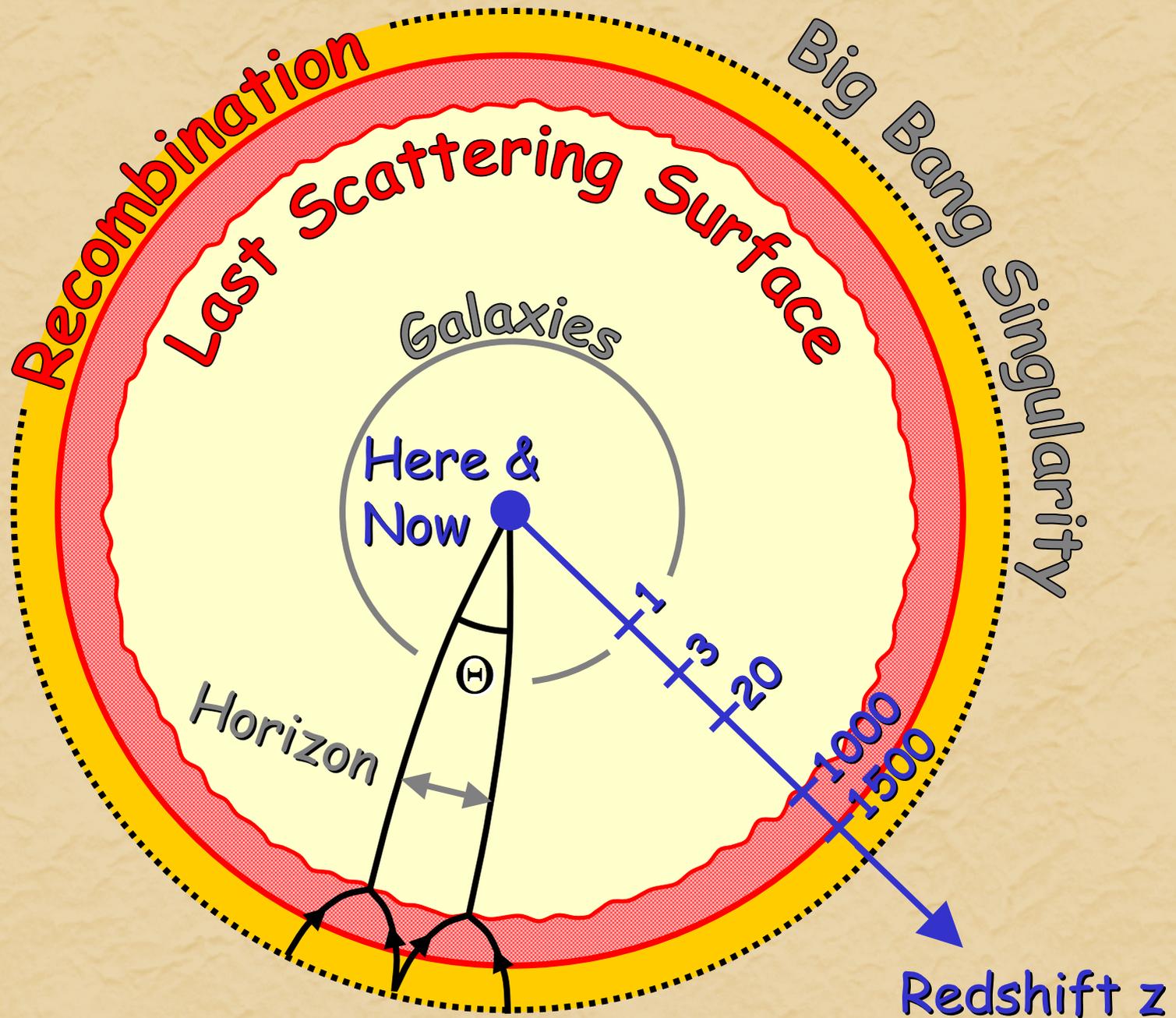
# COBE Sky Map of the CMBR Temperature



Dynamical range  $\Delta T = 18 \mu\text{K}$

**Primordial temperature fluctuations**  
our motion relative to the cosmic frame

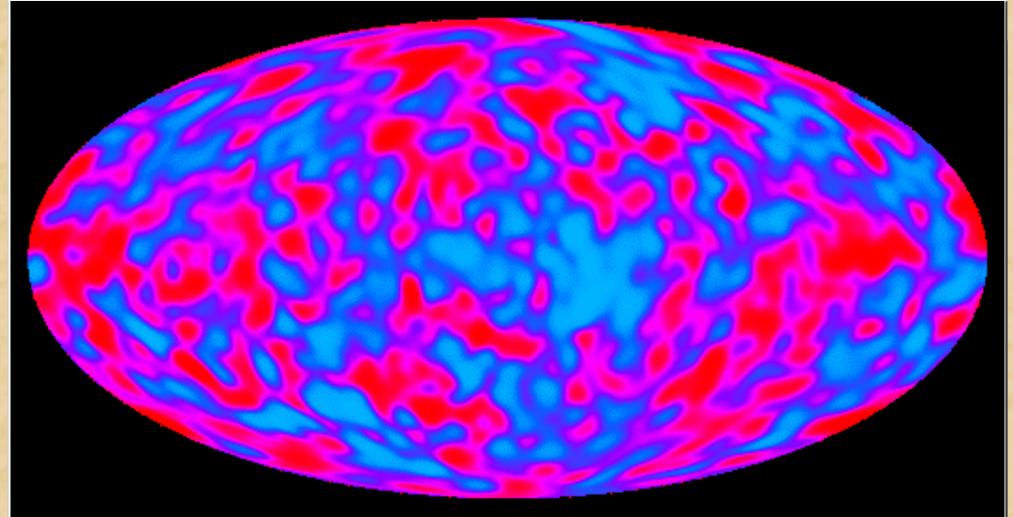
# Last Scattering Surface



# Power Spectrum of CMBR Temperature Fluctuations

Sky map of CMBR temperature fluctuations

$$\Delta(\theta, \varphi) = \frac{T(\theta, \varphi) - \langle T \rangle}{\langle T \rangle}$$

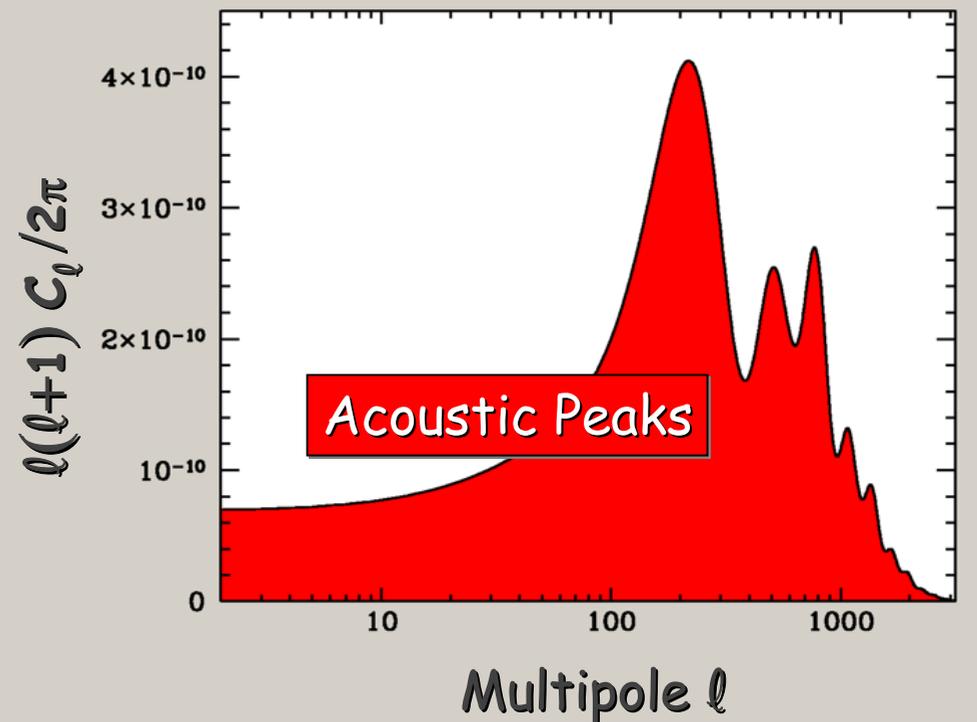


Multipole expansion

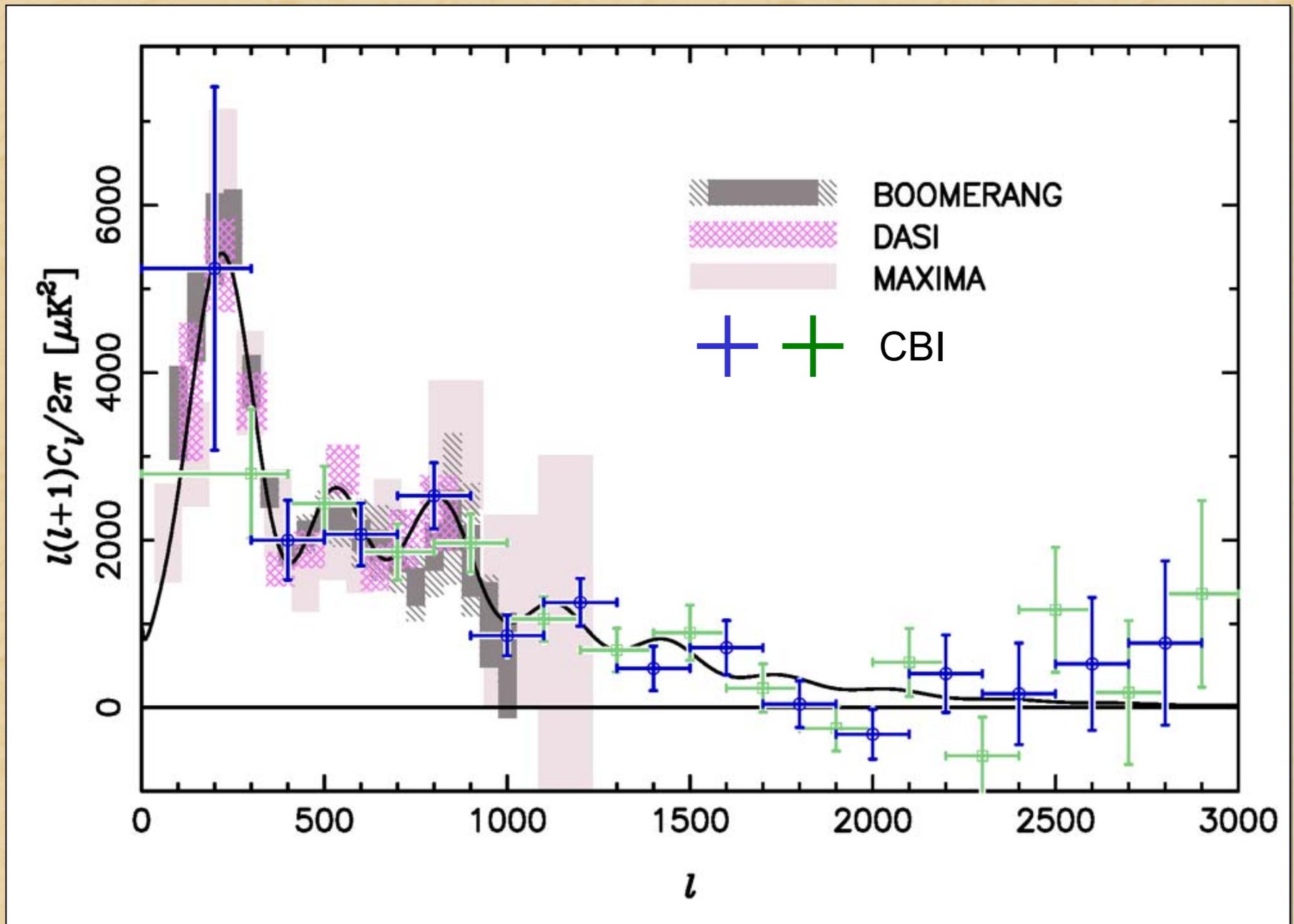
$$\Delta(\theta, \varphi) = \sum_{\ell=0}^{\infty} \sum_{m=-\ell}^{\ell} a_{\ell m} Y_{\ell m}(\theta, \varphi)$$

Angular power spectrum

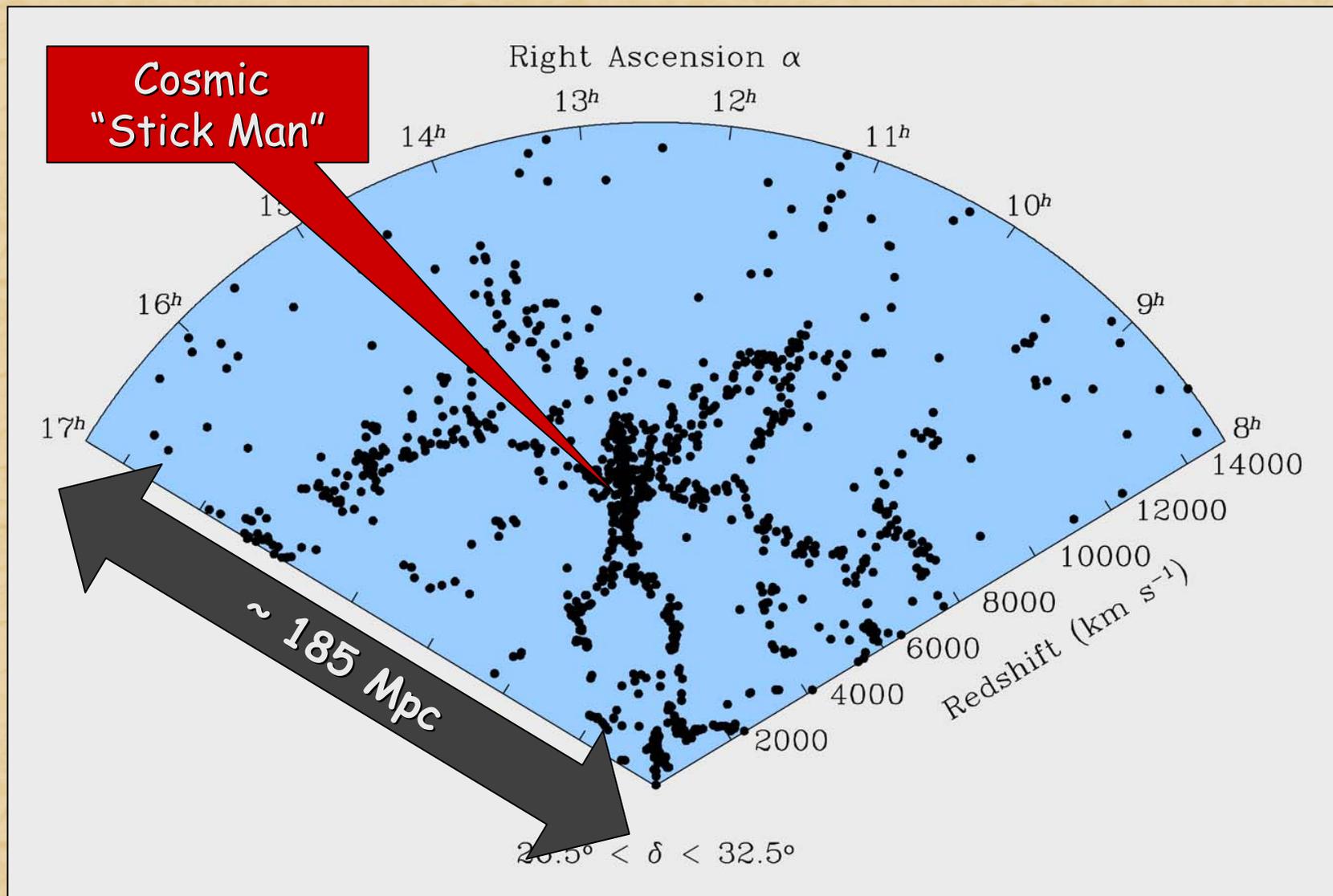
$$C_{\ell} = \langle a_{\ell m}^* a_{\ell m} \rangle = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} a_{\ell m}^* a_{\ell m}$$



# Multiple Peaks in CMBR Angular Power Spectrum

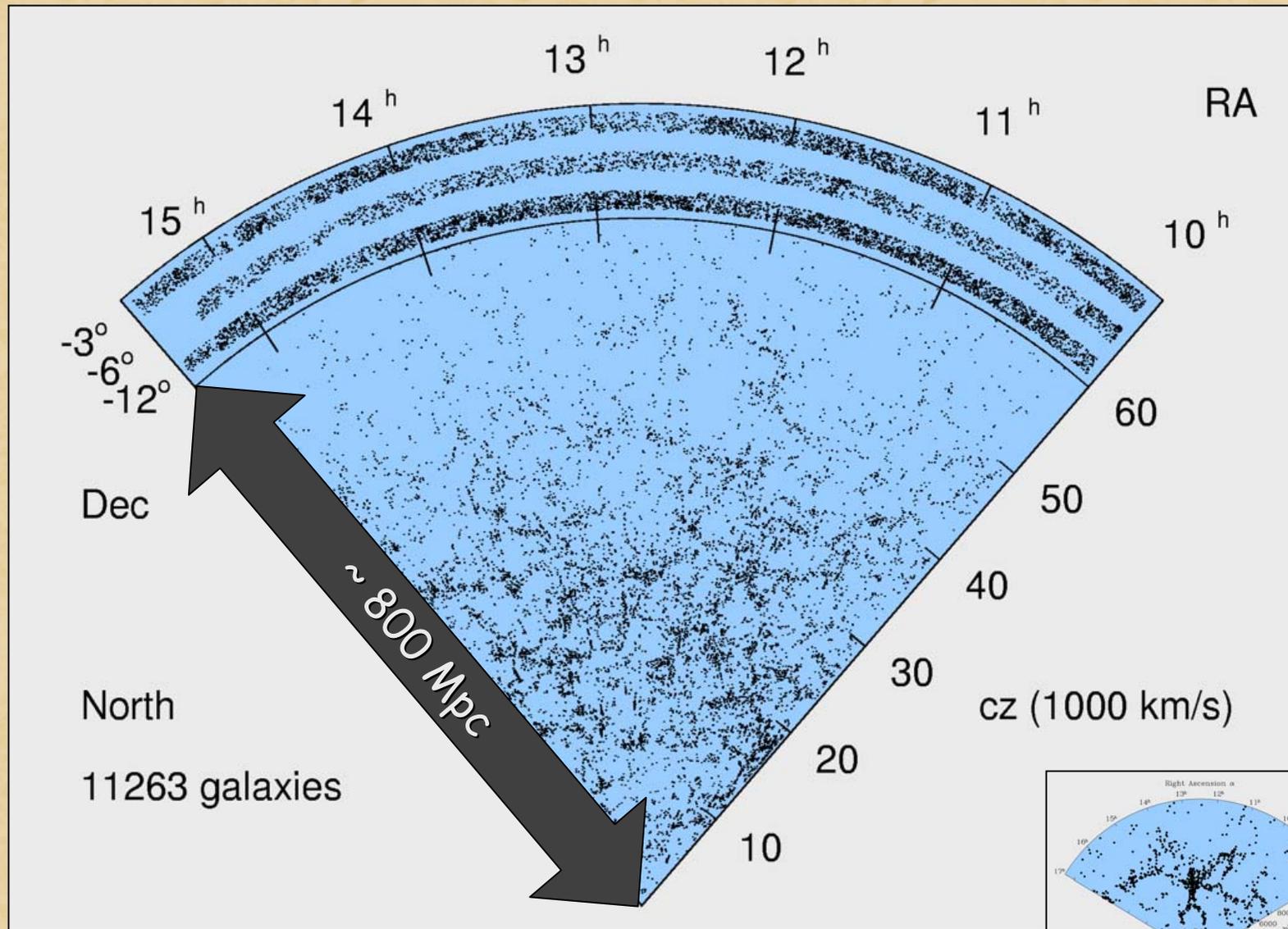


# A Slice of the Universe

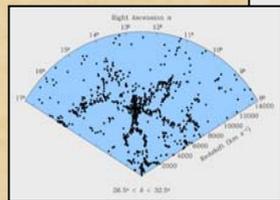
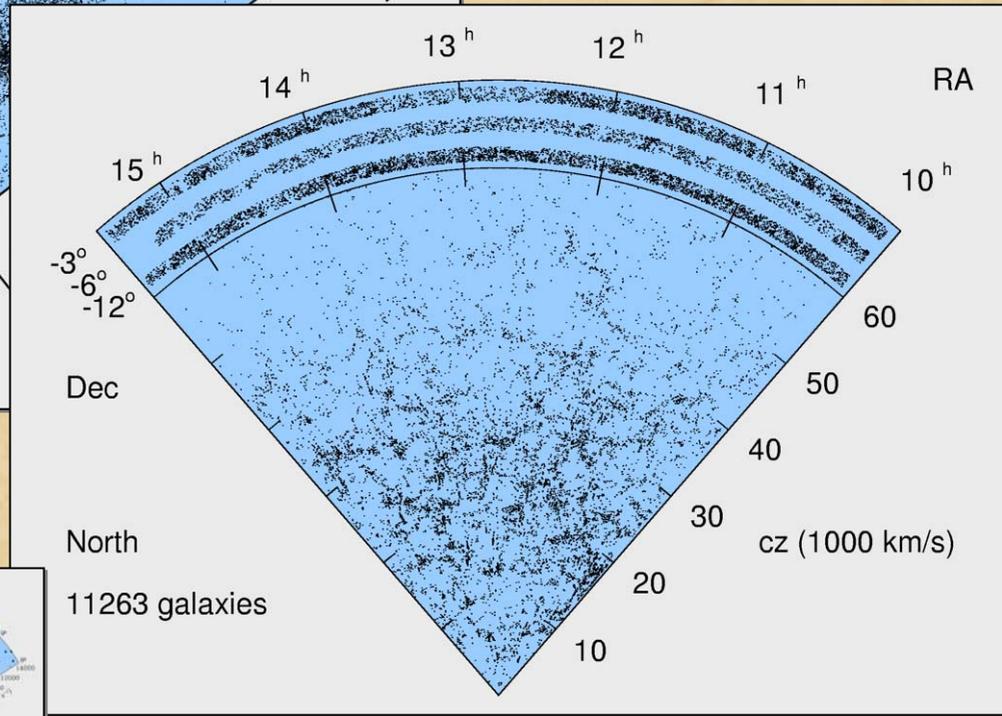
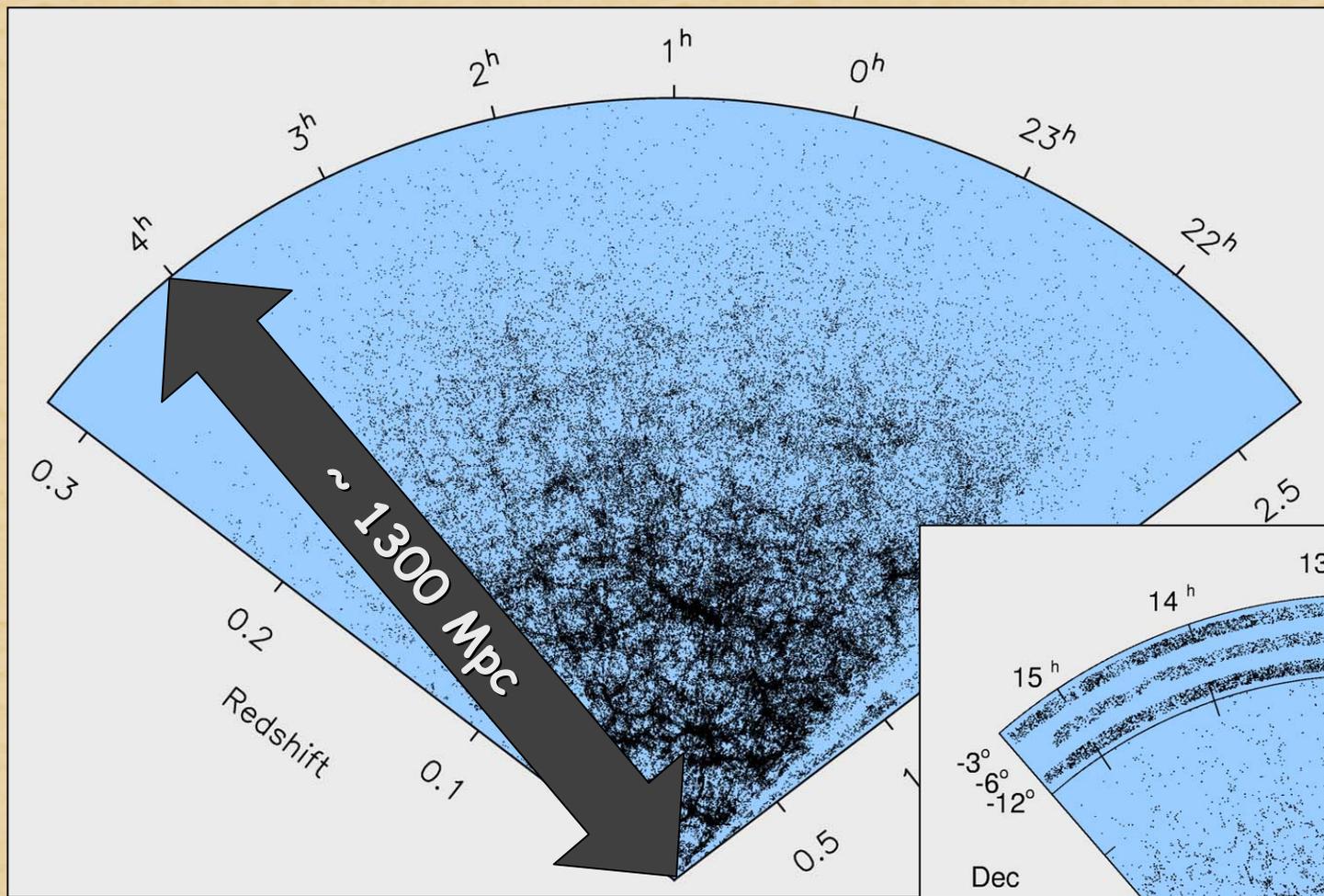


Galaxy distribution from the CfA redshift survey  
[ApJ 302 (1986) L1]

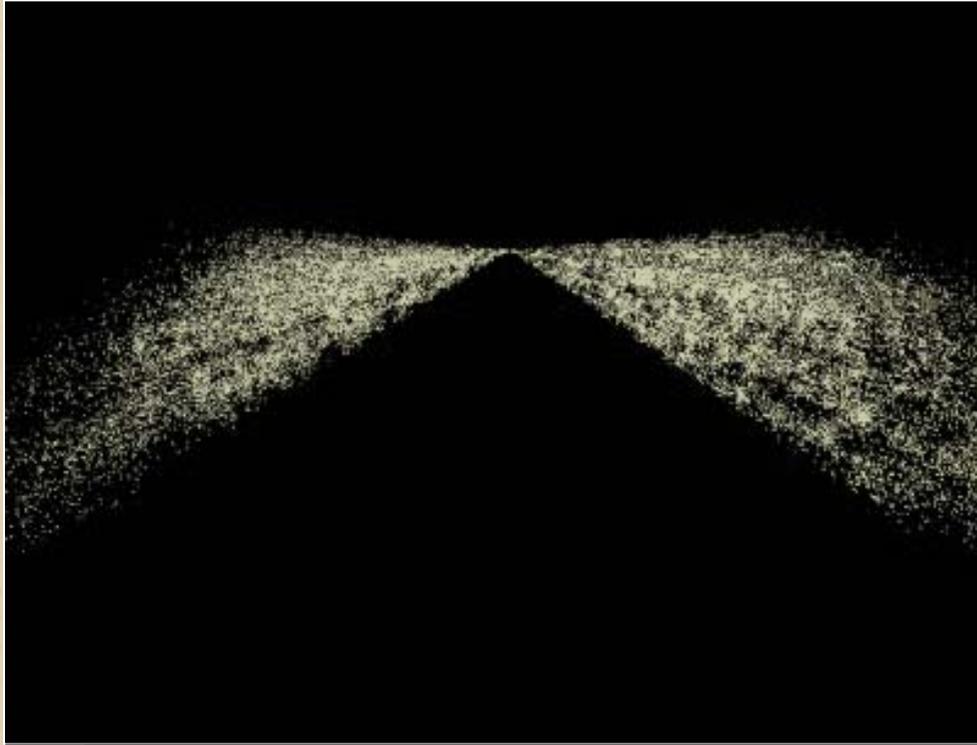
# Las Campanas Redshift Survey



# 2dF Galaxy Redshift Survey (15 May 2002)



# 2dF Galaxy Redshift Survey



Animations from 2dFGRS Homepage <http://www.mso.anu.edu.au/2dFGRS/>

# Power Spectrum of Density Fluctuations

Field of density fluctuations

$$\delta(\mathbf{x}) = \frac{\delta\rho(\mathbf{x})}{\bar{\rho}}$$

Fourier transform

$$\delta(\mathbf{k}) = \int d^3\mathbf{x} e^{-i\mathbf{k}\cdot\mathbf{x}} \delta(\mathbf{x})$$

Power spectrum essentially square of Fourier transform

$$\langle \delta(\mathbf{k})\delta(\mathbf{k}') \rangle = (2\pi)^3 \hat{\delta}(\mathbf{k} - \mathbf{k}') P(\mathbf{k})$$

with  $\hat{\delta}$  the delta function

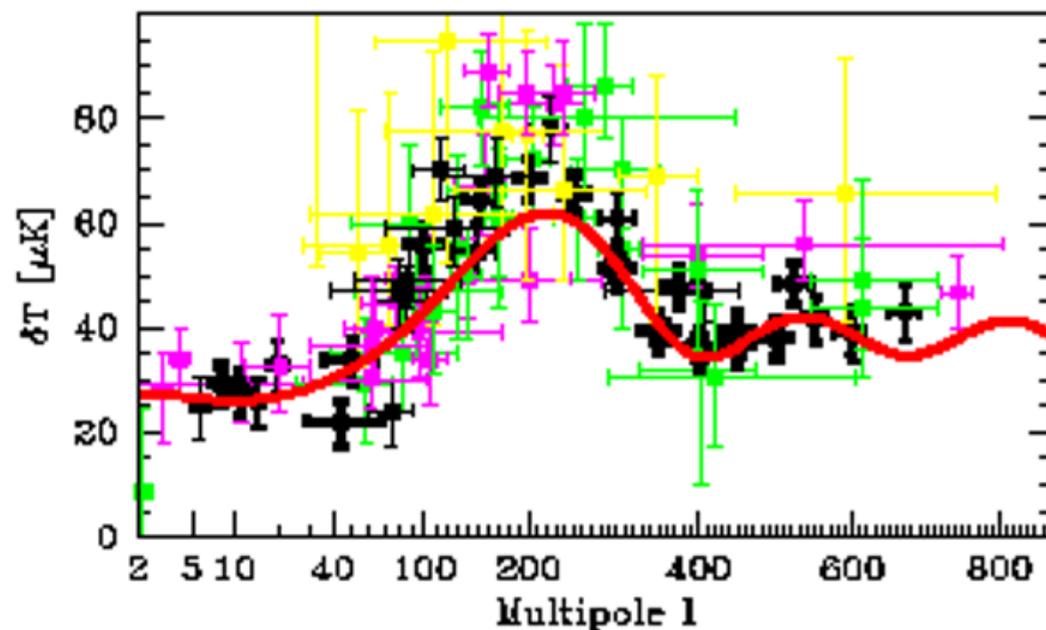
Power spectrum is Fourier transform of two-point correlation function

$$\xi(\mathbf{x}) = \langle \delta(\mathbf{x}_2)\delta(\mathbf{x}_1) \rangle = \int \frac{d^3\mathbf{k}}{(2\pi)^3} e^{i\mathbf{k}\cdot\mathbf{x}} P(\mathbf{k})$$

where  $\mathbf{x} = \mathbf{x}_2 - \mathbf{x}_1$

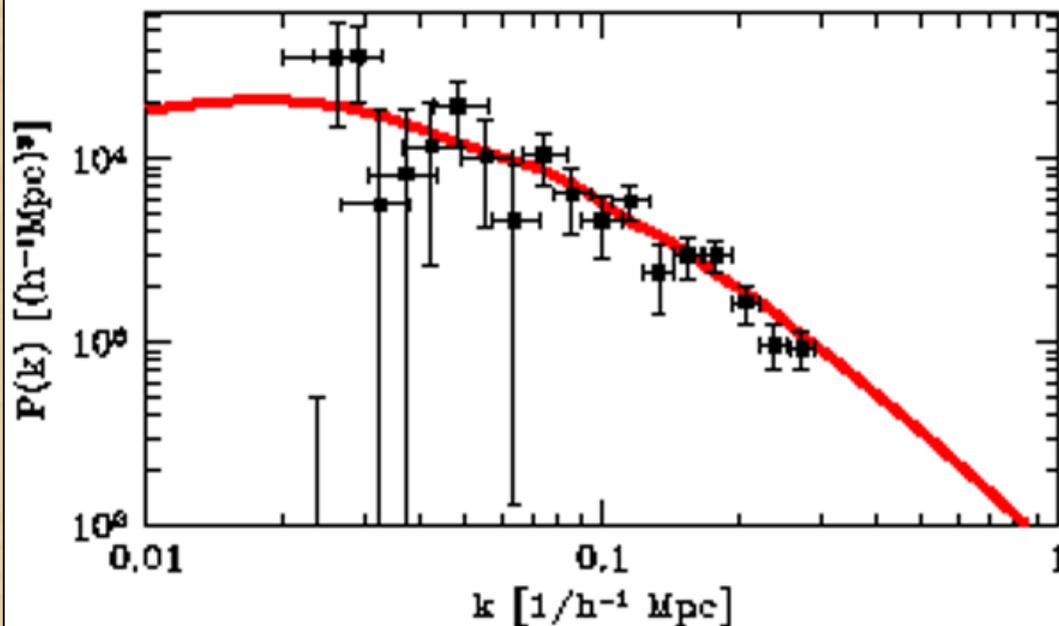
Gaussian random field  
fully characterized  
by power spectrum

# Fitting the Cosmological Model - Neutrinos

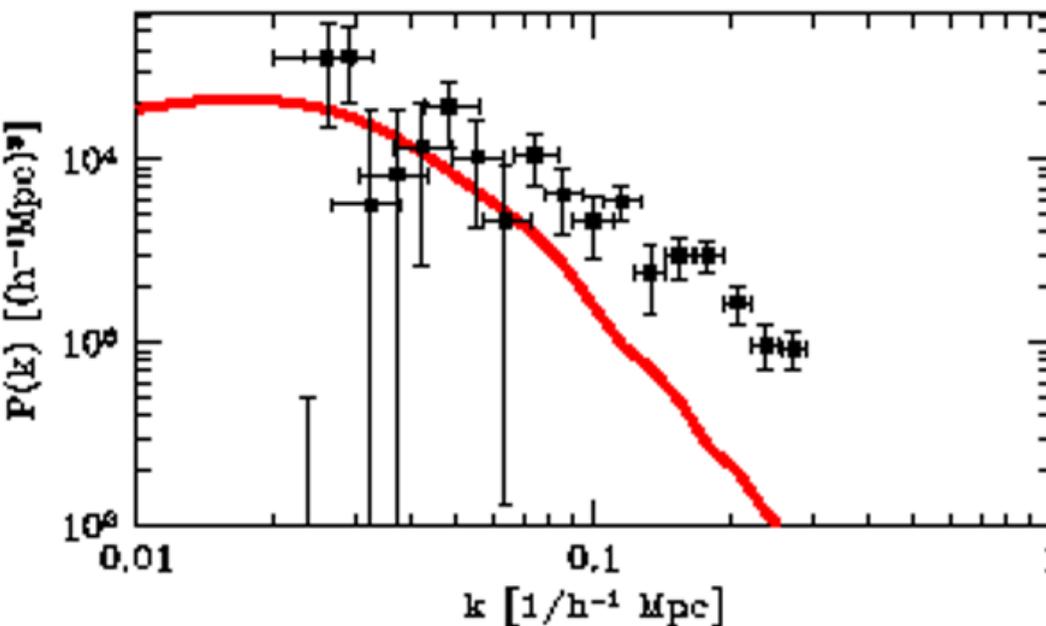
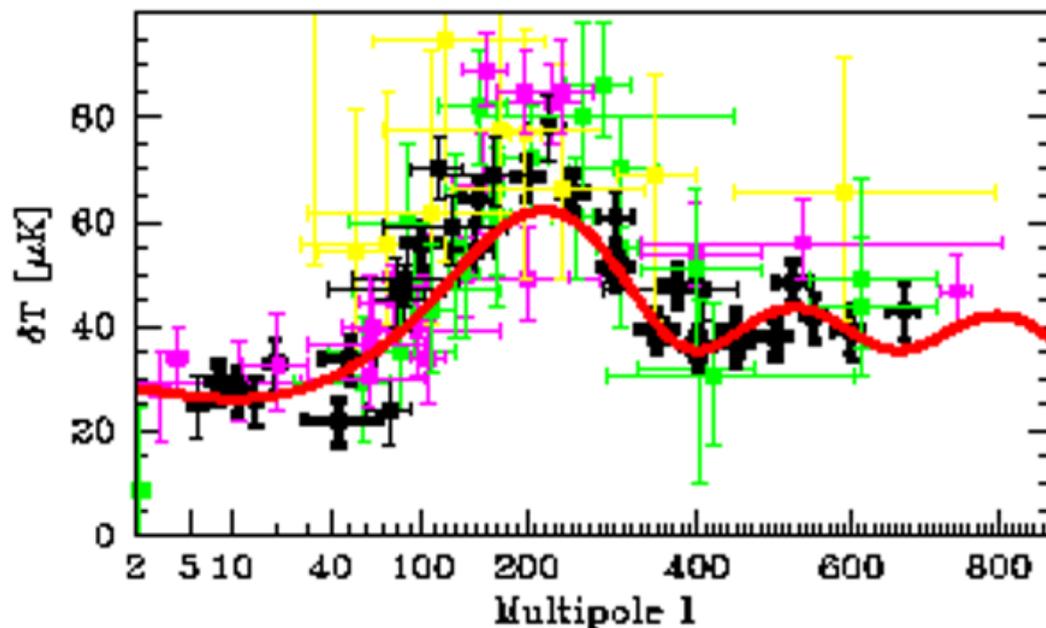


- $\tau = 0.000$
- $\Omega_k = 0.000$
- $\Omega_\Lambda = 0.61$
- $\omega_d = 0.13$
- $\omega_b = 0.020$
- $f_\nu = 0.000$
- $n_s = 0.90$
- $n_t = -1.000$
- $A_s = 0.44$
- $A_t = 0.000$
- $b = 1.2$
- $h = 0.62$
- $\chi^2 = 0.000$

- Ionization parameter
- Curvature
- Cosmological constant
- Dark Matter ( $\Omega_M h^2$ )
- Baryons ( $\Omega_B h^2$ )
- Neutrino DM fraction**
- Scalar power-law index
- Tensor power-law index
- Scalar Amplitude
- Tensor Amplitude
- Biasing parameter
- Hubble constant
- Max Tegmark,  
[www.hep.upenn.edu/~max/concordance.html](http://www.hep.upenn.edu/~max/concordance.html)



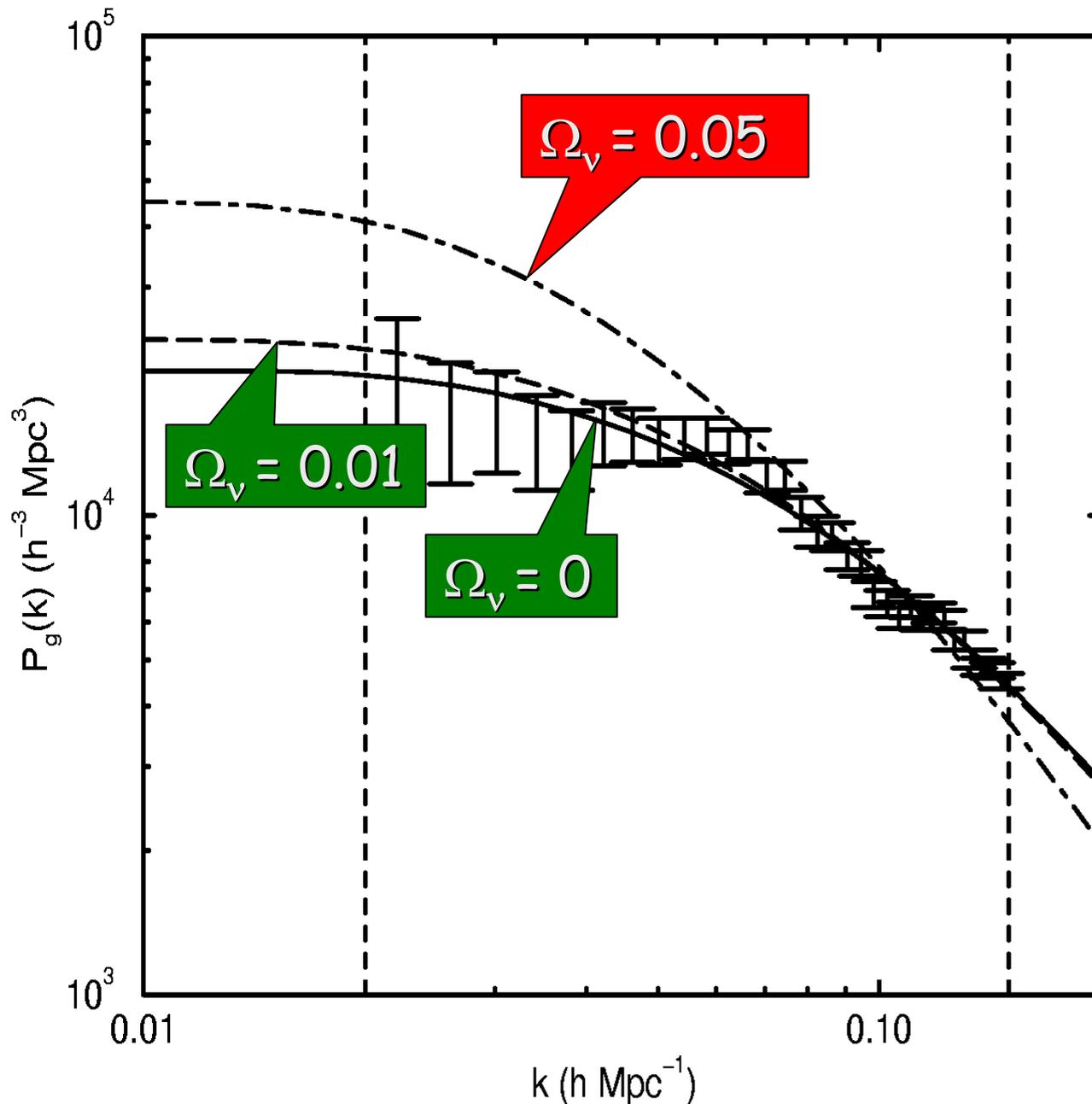
# Fitting the Cosmological Model - Neutrinos



- $\tau = 0.000$
- $\Omega_k = 0.000$
- $\Omega_\Lambda = 0.81$
- $\omega_d = 0.13$
- $\omega_b = 0.020$
- $f_\nu = 0.46$
- $n_s = 0.90$
- $n_t = -1.000$
- $A_s = 0.44$
- $A_t = 0.000$
- $b = 1.2$
- $h = 0.82$
- $\chi^2 = 0.000$

- Ionization parameter
- Curvature
- Cosmological constant
- Dark Matter ( $\Omega_M h^2$ )
- Baryons ( $\Omega_B h^2$ )
- Neutrino DM fraction**
- Scalar power-law index
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# Neutrino Mass Limit from 2dF Galaxy Survey



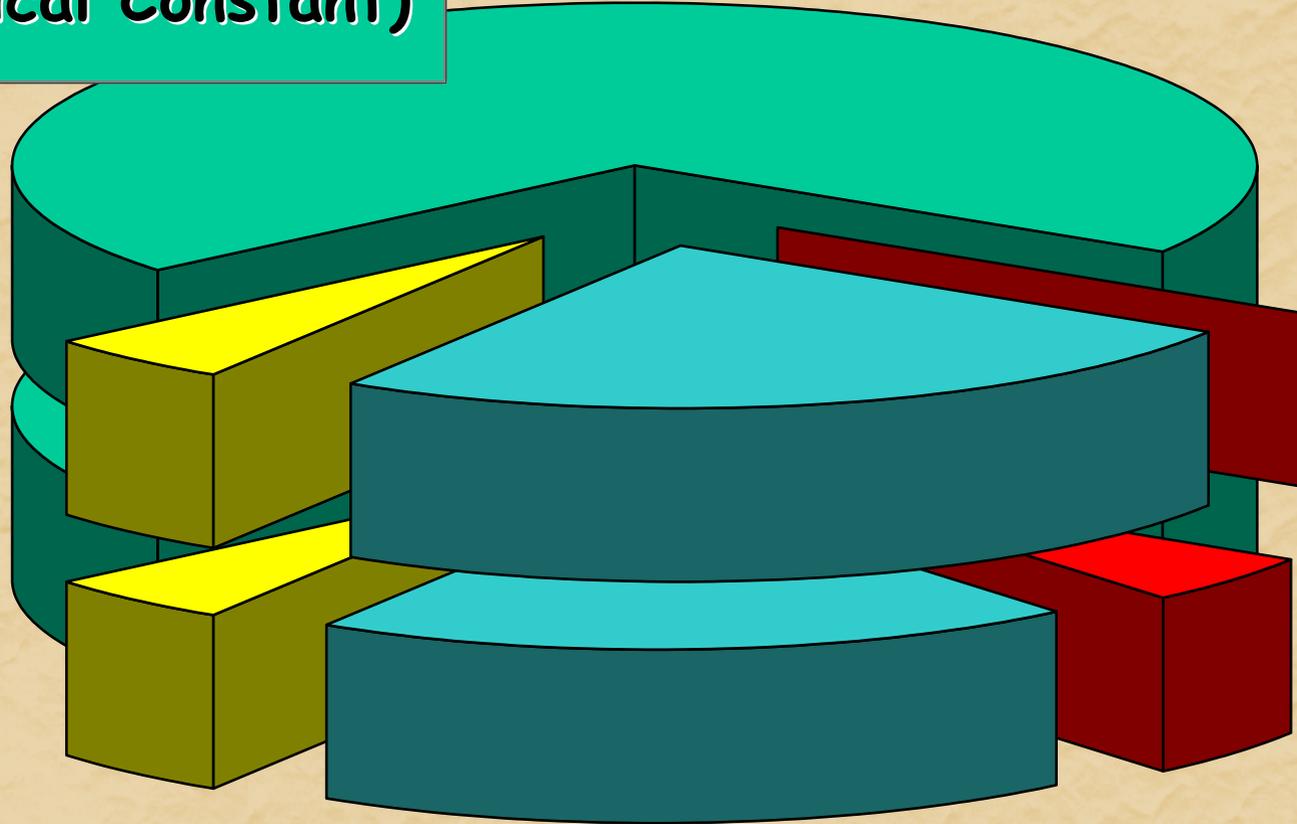
Elgaroy et al.,  
astro-ph/0204152

$\Sigma m_\nu < 2.2 \text{ eV}$   
at 95% CL

For a similar limit  
based on the 2dF  
data see Hannestad  
astro-ph/0205223

# Matter Inventory of the Universe

**Dark Energy ~ 70%**  
**(Cosmological Constant)**



**Baryonic Matter ~ 5%**  
**(~10% of this luminous)**

**Dark Matter**  
**~ 25%**

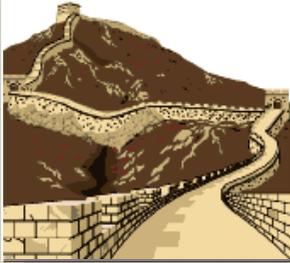
**Neutrinos**  
**min. 0.1%**  
**max. 6%**

# Neutrino Mass Limits and Future Sensitivity

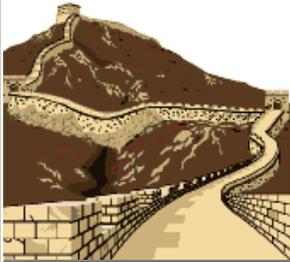
Tritium endpoint	Mainz/Troitsk	2.5 eV
	KATRIN	0.3 eV
Supernova Nus Time-of-flight	SN 1987A	20 eV
	Super-Kamiokande	3 eV
	with black hole	2 eV
	with gravity waves	1 eV
Cosmic structure	2dF Redshift Survey	0.8 eV
	Sloan Digital Sky Survey	0.3 eV

- Assume 3 mass eigenstates with very small mass differences as indicated by atmospheric and solar neutrinos
- The cosmological limit refers to  $m_\nu = \Sigma m_\nu / 3$

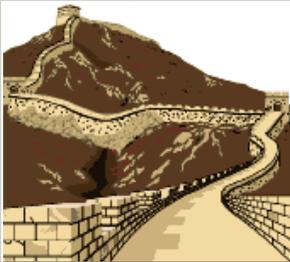
# Lecture II: Cosmological Neutrinos



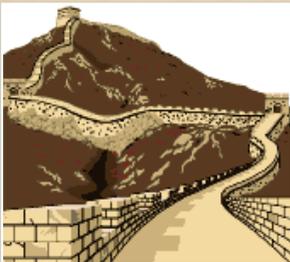
**Neutrino Dark Matter and  
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**Neutrino Chemical Potentials,  
Big-Bang Nucleosynthesis,  
and Flavor Oscillations**



**Highest-Energy Cosmic Rays  
and the Cosmic Neutrino Sea**



**Massive Neutrinos and the  
Cosmic Baryon Asymmetry**

# How Many Relic Neutrinos?

Standard thermal population in one flavor  $n_{\nu\bar{\nu}} = \frac{3}{11} n_\gamma \approx 112 \text{ cm}^{-3}$

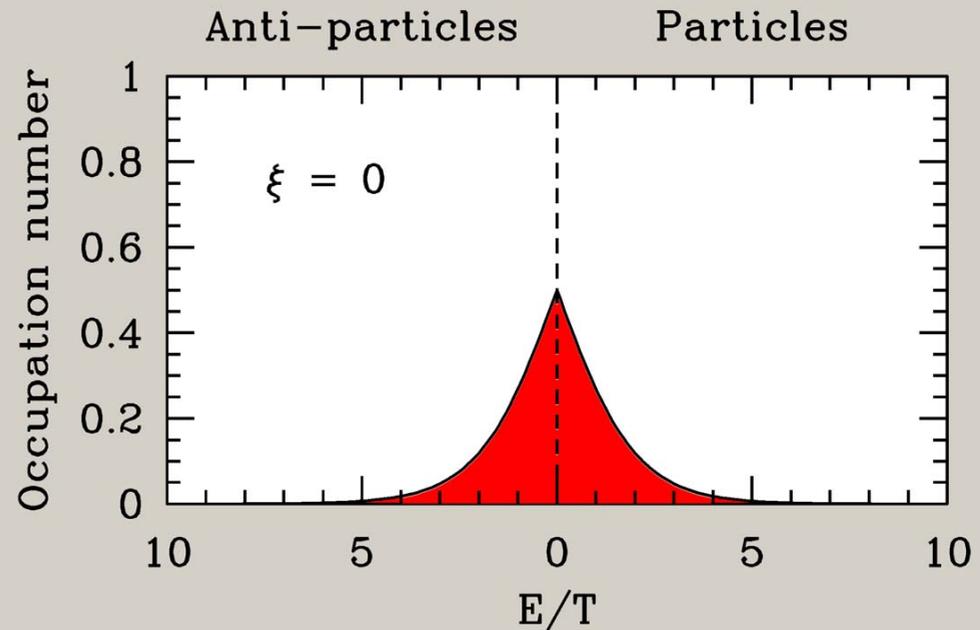
Additional active neutrinos beyond standard population of $\nu_e, \nu_\mu, \nu_\tau$	Additional families	Excluded by $Z^0$ width ( $N_\nu = 3$ )
	Chemical potentials for $\nu_e, \nu_\mu, \nu_\tau$	Possible
Sterile (right-handed) states  Populated by $\nu_L \rightarrow \nu_R$ transitions	Dirac mass	Not effective in eV range
	Right-handed currents	Excluded by energy loss of SN 1987A
	Electromagnetic dipole moments	Excluded by energy loss of globular cluster stars
	Oscillations/collisions	Hot/warm/cold DM possible

# Thermal Neutrino Distribution

## Fermi-Dirac distribution

- Temperature  $T$
- Chemical potential  $\mu$
- $+\mu$  Particles
- $-\mu$  Anti-particles

$$f_p = \frac{1}{\exp\left(\frac{E - \mu}{T}\right) + 1}$$



Degeneracy parameter  $\xi = \frac{\mu}{T}$  Invariant under cosmic expansion

Number density

$$n_{\nu\bar{\nu}} = \int dE \frac{4\pi}{(2\pi)^3} \left( \frac{E^2}{1 + \exp(E/T - \xi)} + \frac{E^2}{1 + \exp(E/T + \xi)} \right)$$

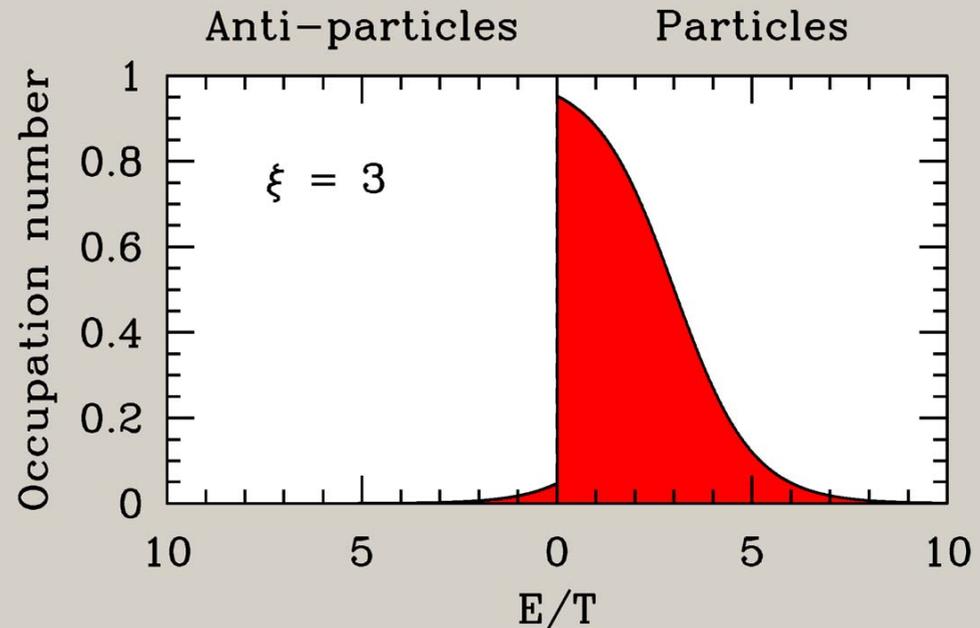
$$= \frac{3\zeta_3}{2\pi^2} T_\nu^3 \left[ 1 + \frac{2\ln(2)}{3\zeta_3} \xi^2 + \frac{1}{72\zeta_3} \xi^4 + \dots \right]$$

# Thermal Neutrino Distribution

## Fermi-Dirac distribution

- Temperature  $T$
- Chemical potential  $\mu$
- $+\mu$  Particles
- $-\mu$  Anti-particles

$$f_p = \frac{1}{\exp\left(\frac{E - \mu}{T}\right) + 1}$$



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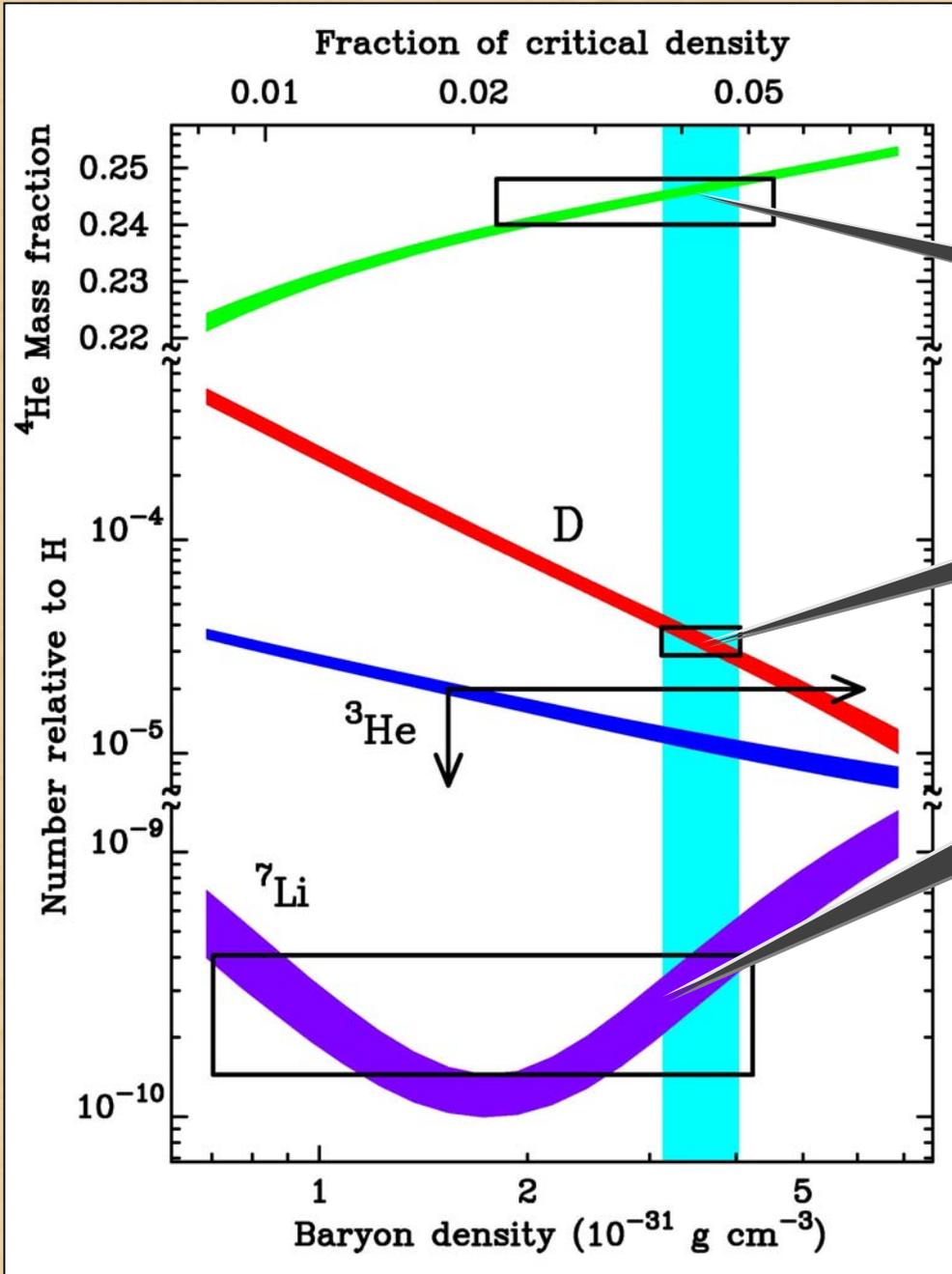
Number density

$$n_{\nu\bar{\nu}} = \int dE \frac{4\pi}{(2\pi)^3} \left( \frac{E^2}{1 + \exp(E/T - \xi)} + \frac{E^2}{1 + \exp(E/T + \xi)} \right)$$

$$= \frac{3\zeta_3}{2\pi^2} T_\nu^3 \left[ 1 + \frac{2\ln(2)}{3\zeta_3} \xi^2 + \frac{1}{72\zeta_3} \xi^4 + \dots \right]$$

# BBN Concordance

Burles, Nollett & Turner  
astro-ph/9903300



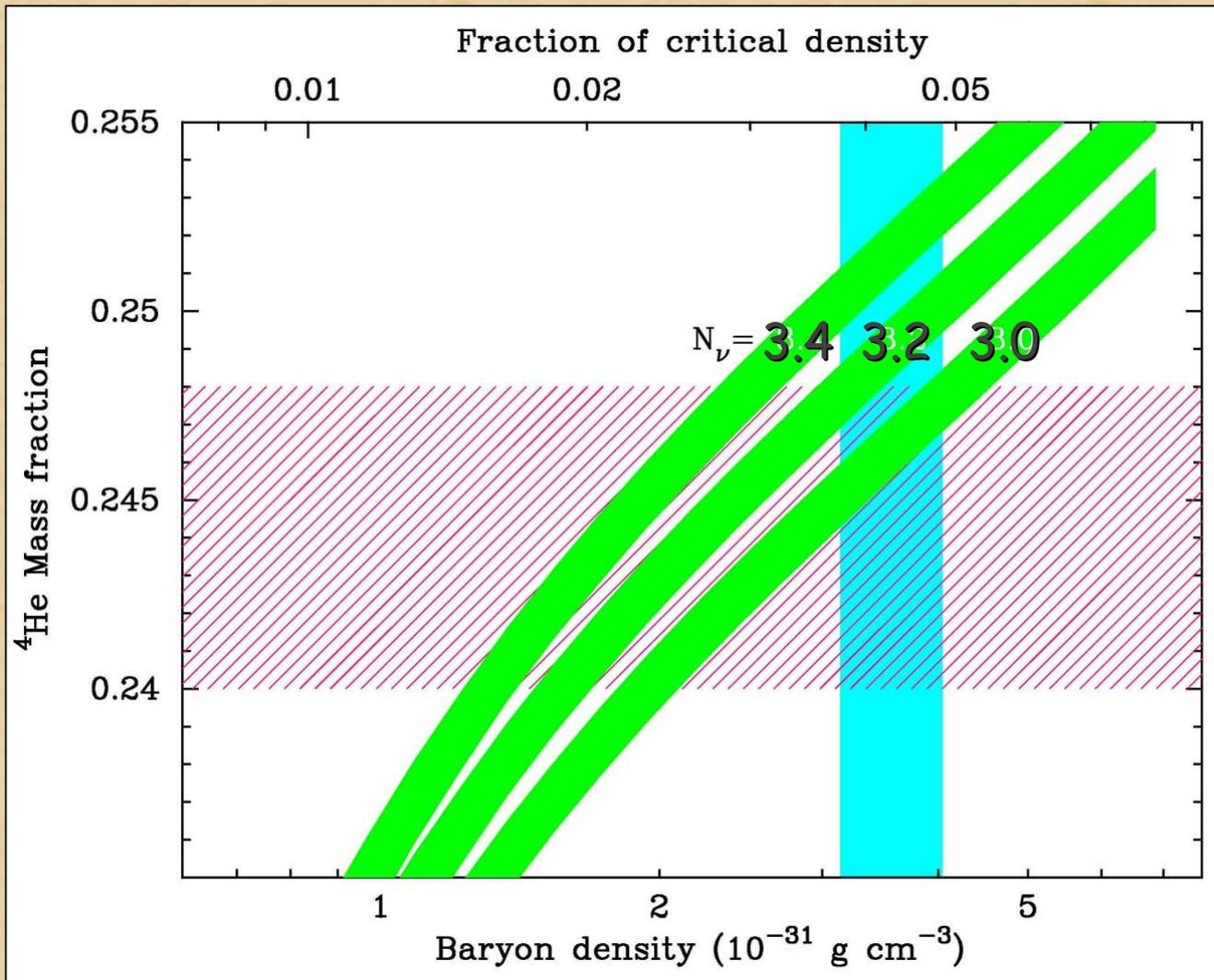
Helium 4

Deuterium

Lithium

Cosmic baryon density  
implied by deuterium  
 $\Omega_B h^2 = 0.019 \pm 0.0024$

# BBN Limits on Neutrino Flavors



- At BBN one flavor contributes about 16% to cosmic mass-energy density
- Extra flavors modify expansion parameter accordingly

Conservative limit  
 $|\Delta N_{\text{eff}}| < 1$

Burles, Nollett & Turner, astro-ph/9903300

# BBN and Neutrino Chemical Potentials

Expansion Rate  
Effect  
(all flavors)

Energy density in one neutrino flavor with degeneracy parameter  $\xi = \eta/T$

$$\rho_{\nu\bar{\nu}} = \frac{7\pi^2}{120} T_\nu^4 \left[ 1 + \underbrace{\frac{30}{7} \left(\frac{\xi}{\pi}\right)^2 + \frac{15}{7} \left(\frac{\xi}{\pi}\right)^4}_{\Delta N_{\text{eff}}} \right]$$

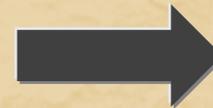
Beta equilibrium  
effect for  
electron flavor  
 $n + \nu_e \leftrightarrow p + e^-$

Helium abundance essentially fixed by  
 $n/p$  ratio at beta freeze-out

$$\frac{n}{p} = e^{-(m_n - m_p)/T - \xi_{\nu_e}}$$

Effect on helium equivalent to  $\Delta N_{\text{eff}} \sim -18 \xi_{\nu_e}$

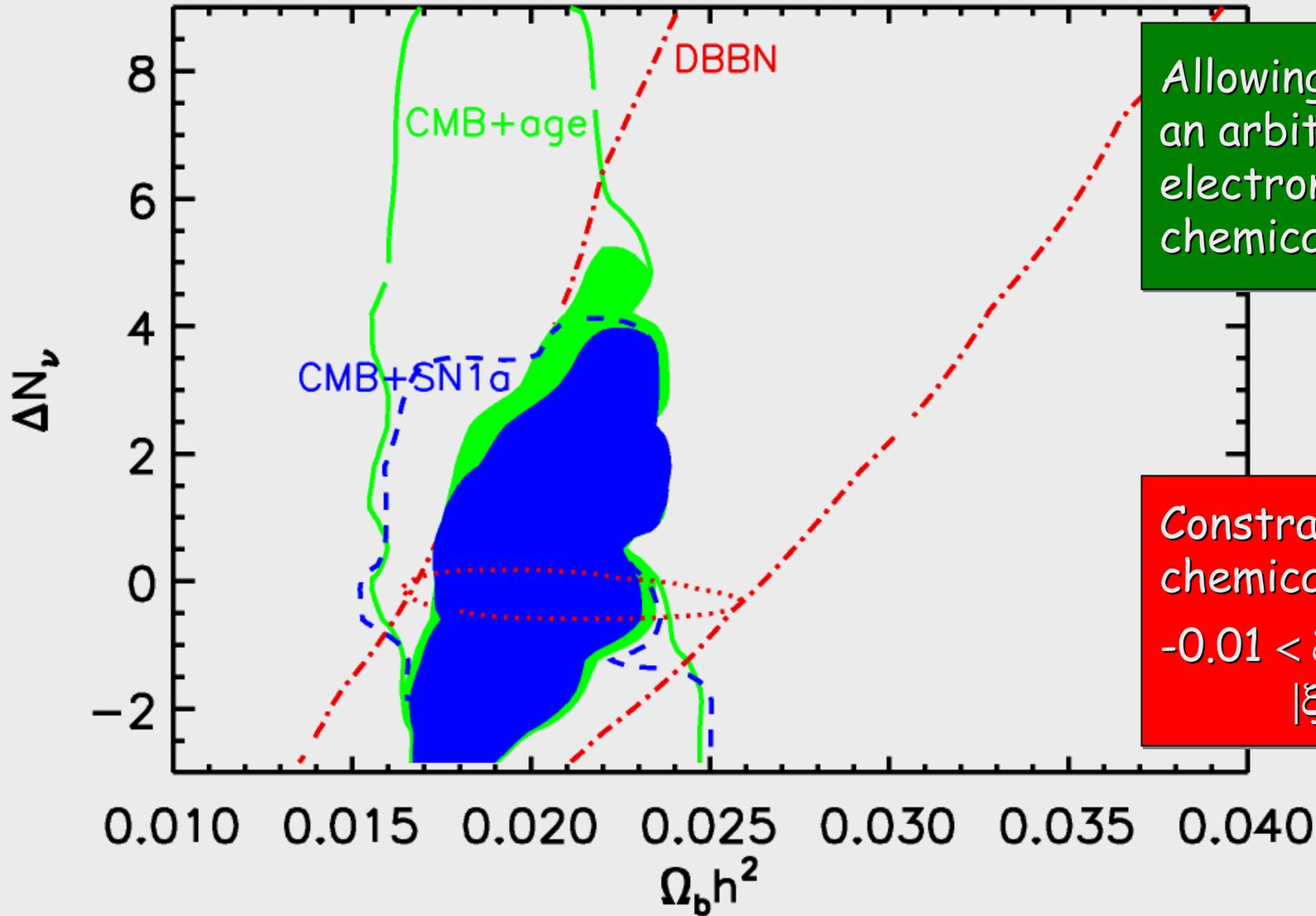
$$|\Delta N_{\text{eff}}| < 1$$



$$|\xi_{\nu_e}| < 0.06$$

- $\nu_e$  beta effect can compensate expansion-rate effect of  $\nu_{\mu,\tau}$
- No significant BBN limit on neutrino number density

# Limits on Radiation Density



Allowing for an arbitrary electron neutrino chemical potential

Constraints on nu chemical potentials

$$-0.01 < \xi_{\nu e} < 0.25$$

$$|\xi_{\nu \mu, \tau}| < 2.9$$

Hansen et al., astro-ph/0105385

# Chemical Potentials and Flavor Oscillations

Flavor mixing  
(neutrino oscillations)

Flavor lepton numbers  
not conserved

Only one common nu  
chemical potential

Stringent  $\xi_{\nu e}$  limit  
applies to all flavors

$$|\xi_{\nu e, \mu, \tau}| < 0.07$$

Extra neutrino density  
 $\Delta N_{\text{eff}} < 0.0064$

Cosmic neutrino density  
close to standard value

Flavor equilibrium before n/p  
freeze out?

yes

Solar LMA solution

maybe

LOW (depends on  $\Theta_{13}$ )

no

Solar SMA solution

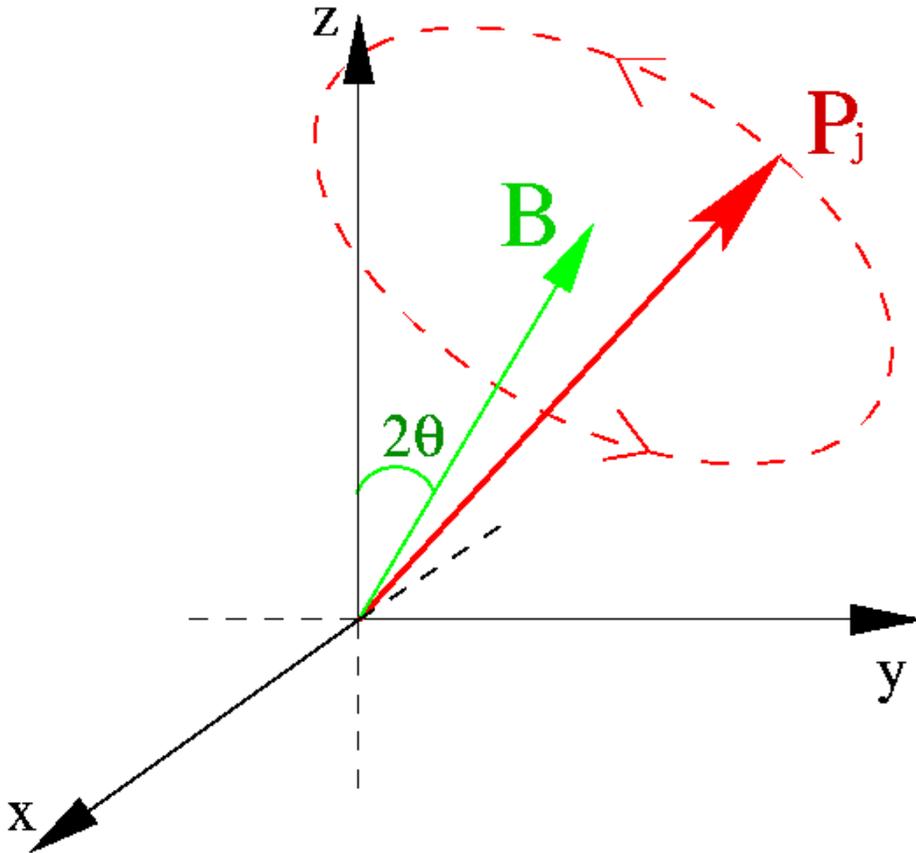
- Our knowledge of the cosmic nu density depends on the solution of the solar neutrino problem
- KamLAND most relevant experiment

- Lunardini & Smirnov, hep-ph/0012056
- Dolgov, Hansen, Pastor, Petcov, Raffelt & Semikoz, hep-ph/0201287
- Abazajian, Beacom & Bell, astro-ph/0203442
- Wong, hep-ph/0203180

# Two-Flavor Neutrino Oscillations

Evolution of neutrino ensemble described in terms of density matrices

$$f_p \rightarrow \rho_p = \begin{pmatrix} f_p^{ee} & f_p^{e\mu} \\ f_p^{e\mu} & f_p^{\mu\mu} \end{pmatrix} = \frac{1}{2} (f_p + \vec{\sigma} \cdot \vec{P}_p)$$



Flavor oscillations in vacuum:

$$\partial_t \vec{P}_p = \frac{\delta m^2}{2p} \vec{B} \times \vec{P}_p$$

with

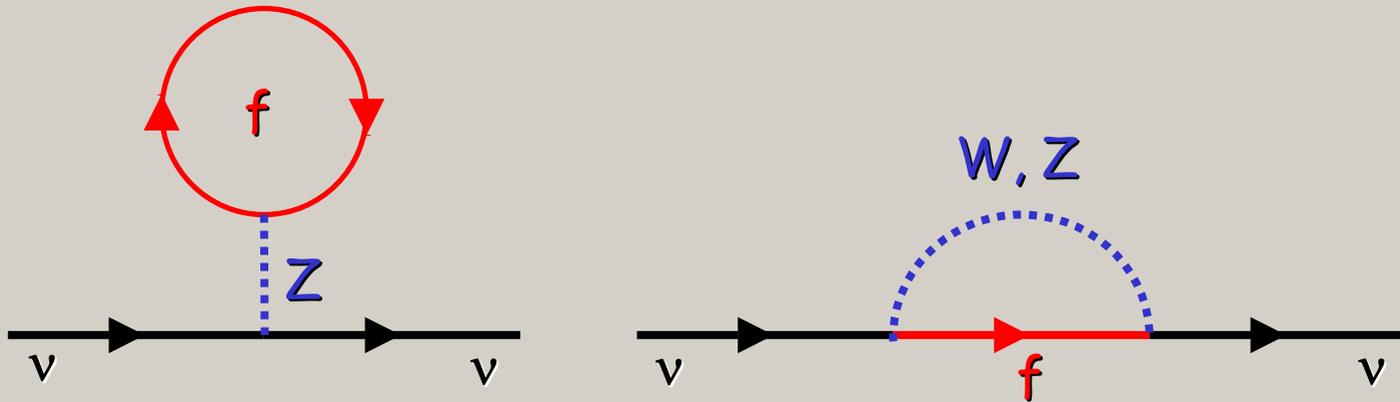
$$\vec{B} = \begin{pmatrix} \sin 2\theta \\ 0 \\ \cos 2\theta \end{pmatrix}$$

and

$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

# Two-Flavor Oscillations in Media

Neutrinos propagating in a medium suffer refraction (Wolfenstein 1978)



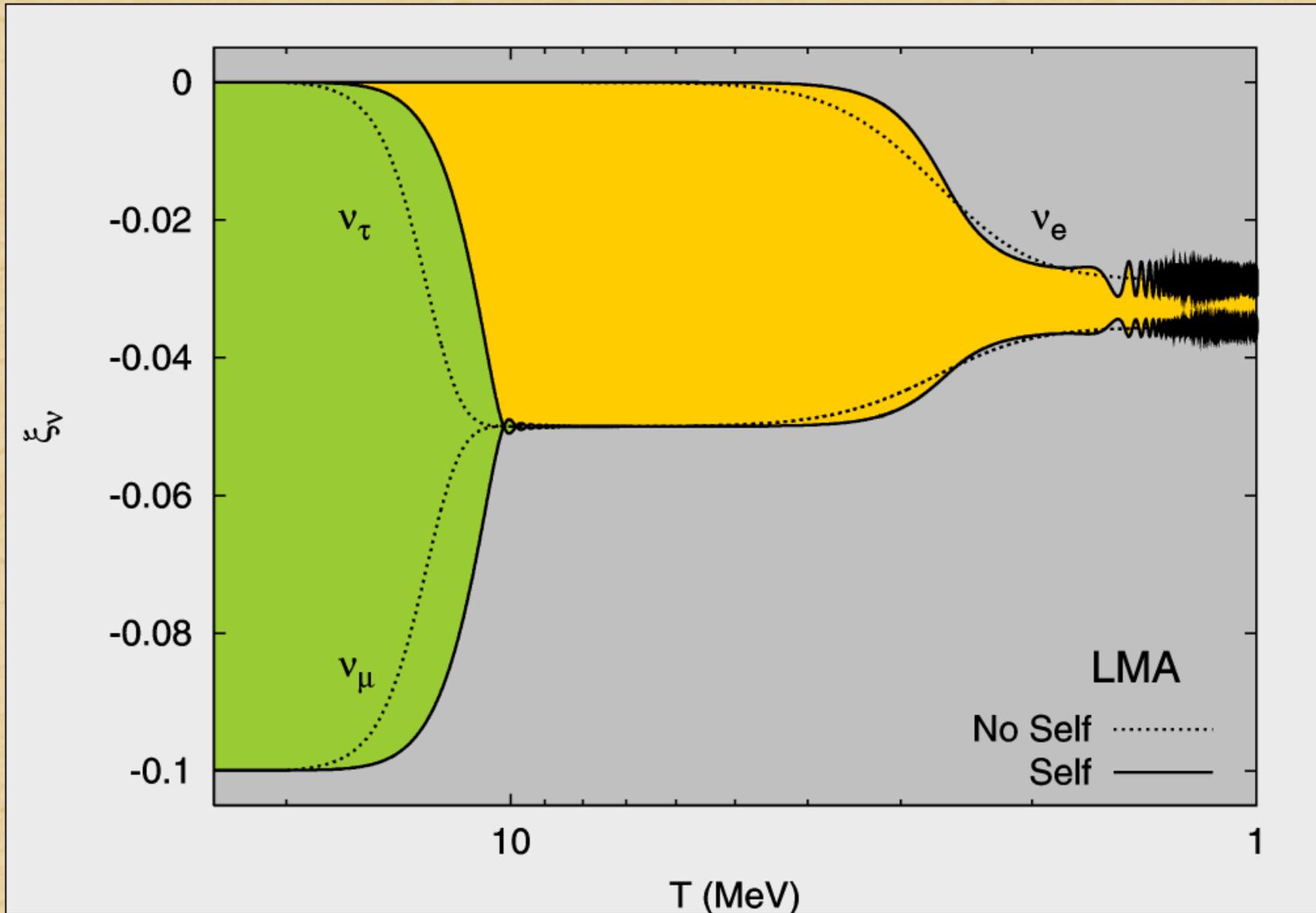
Effect is usually different for different flavors

Equation of motion in early universe (ignoring neutrino background)

$$\partial_t \vec{P}_p = \left( \frac{\delta m^2}{2p} \vec{B} - \frac{8\sqrt{2}G_F p}{3m_W^2} \rho_e \vec{z} \right) \times \vec{P}_p \quad \text{with } \rho_e \text{ the } e^+e^- \text{ energy density}$$

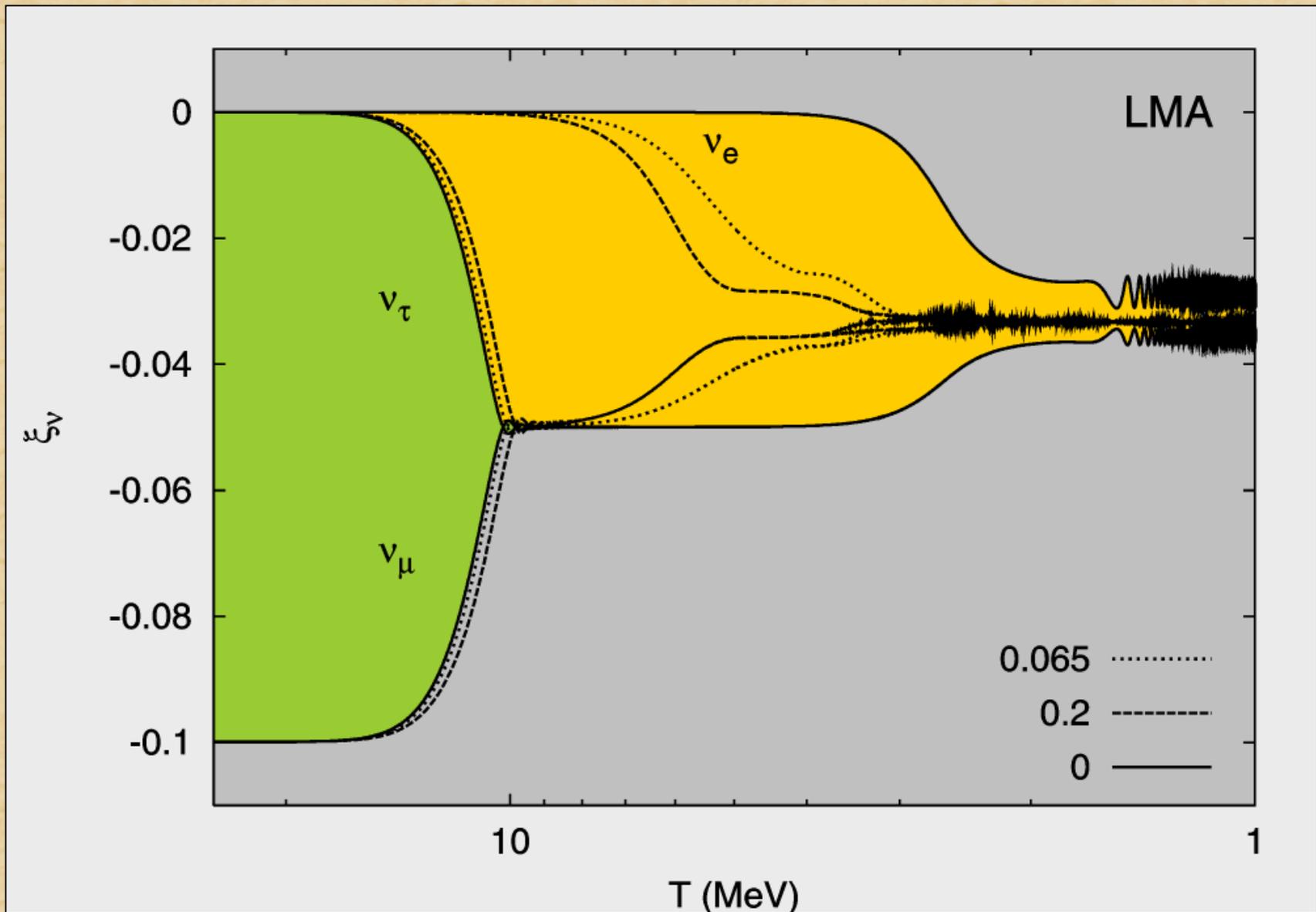
Oscillations begin when background medium is sufficiently diluted to avoid large medium effect compared to vacuum mixing

# Flavor Equilibration: LMA Solution



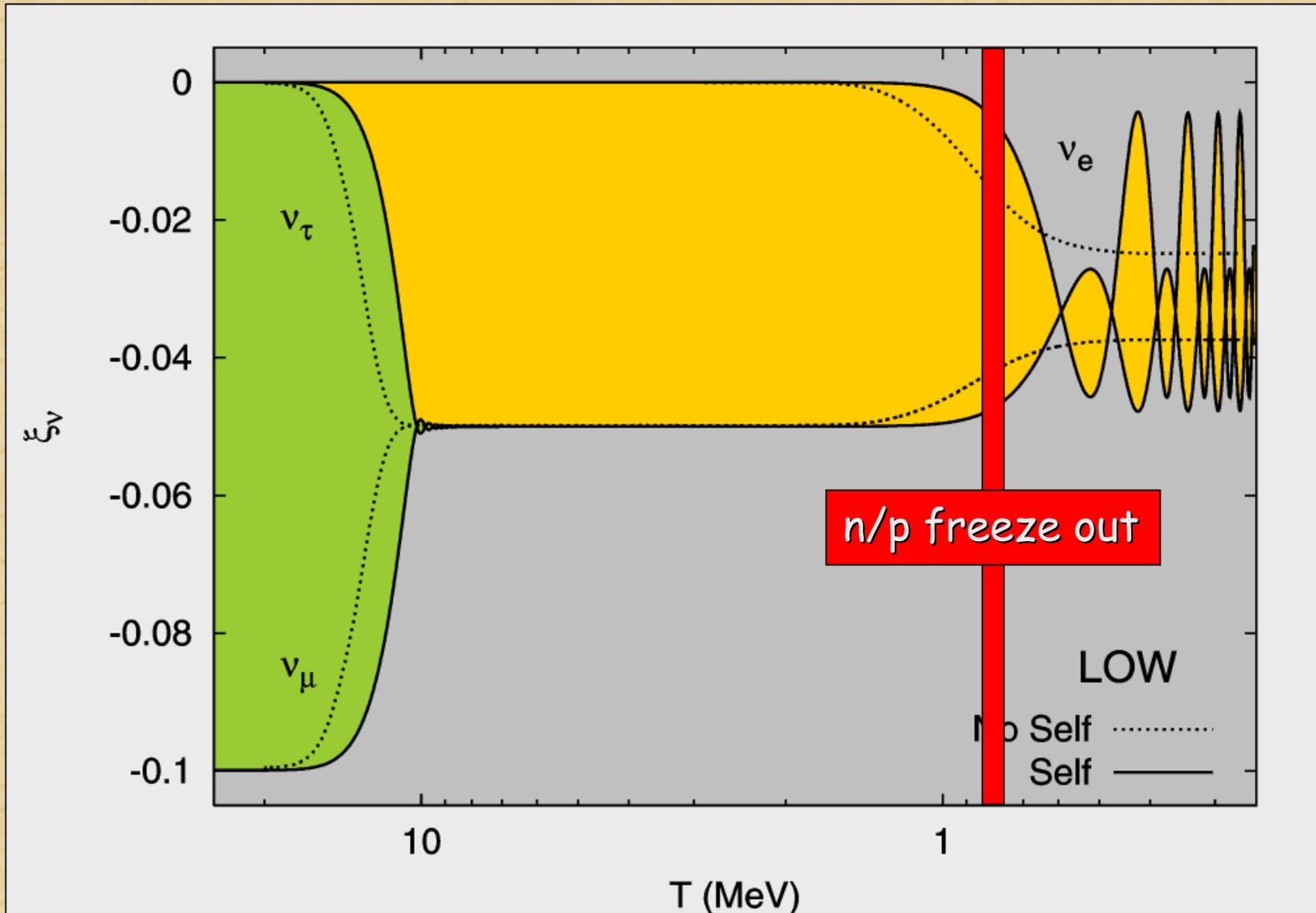
Dolgov, Hansen, Pastor, Petcov, Raffelt & Semikoz, hep-ph/0201287

# Flavor Equilibration: LMA With Non-Zero $\Theta_{13}$



Dolgov, Hansen, Pastor, Petcov, Raffelt & Semikoz, hep-ph/0201287

# Flavor Equilibration: LOW Solution



Dolgov, Hansen, Pastor, Petcov, Raffelt & Semikoz, hep-ph/0201287

# Synchronized Oscillations by Self-Interactions

Equation of motion in early universe with neutrino background

$$\partial_t \mathbf{P}_p = + \left( \frac{\delta m^2}{2p} \mathbf{B} - \frac{8\sqrt{2}G_F p}{3m_W^2} \rho_e \mathbf{z} \right) \times \mathbf{P}_p + \sqrt{2}G_F (\mathbf{P} - \bar{\mathbf{P}}) \times \mathbf{P}_p \quad \text{neutrinos}$$

$$\partial_t \bar{\mathbf{P}}_p = - \left( \frac{\delta m^2}{2p} \mathbf{B} - \frac{8\sqrt{2}G_F p}{3m_W^2} \rho_e \mathbf{z} \right) \times \bar{\mathbf{P}}_p + \sqrt{2}G_F (\mathbf{P} - \bar{\mathbf{P}}) \times \bar{\mathbf{P}}_p \quad \text{anti-neutrinos}$$

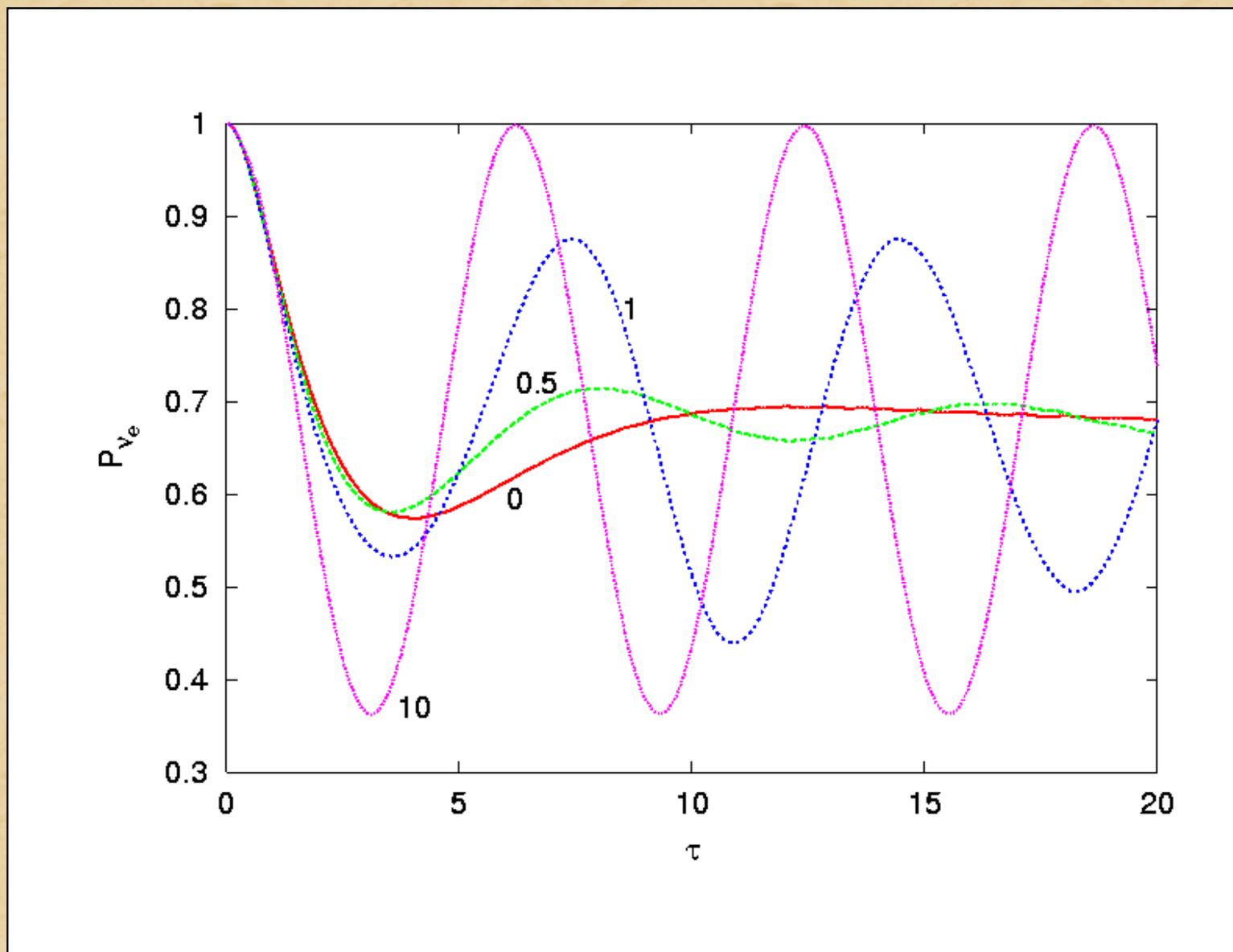
with the integrated neutrino polarization vectors

$$\mathbf{P} = \int \frac{d^3 p}{(2\pi)^3} \mathbf{P}_p \quad \text{and} \quad \bar{\mathbf{P}} = \int \frac{d^3 p}{(2\pi)^3} \bar{\mathbf{P}}_p$$

- "Magnetic field" caused by neutrinos themselves much larger than vacuum or medium terms.
- Couples "magnetic moments" to one large dipole which precesses with a single frequency.

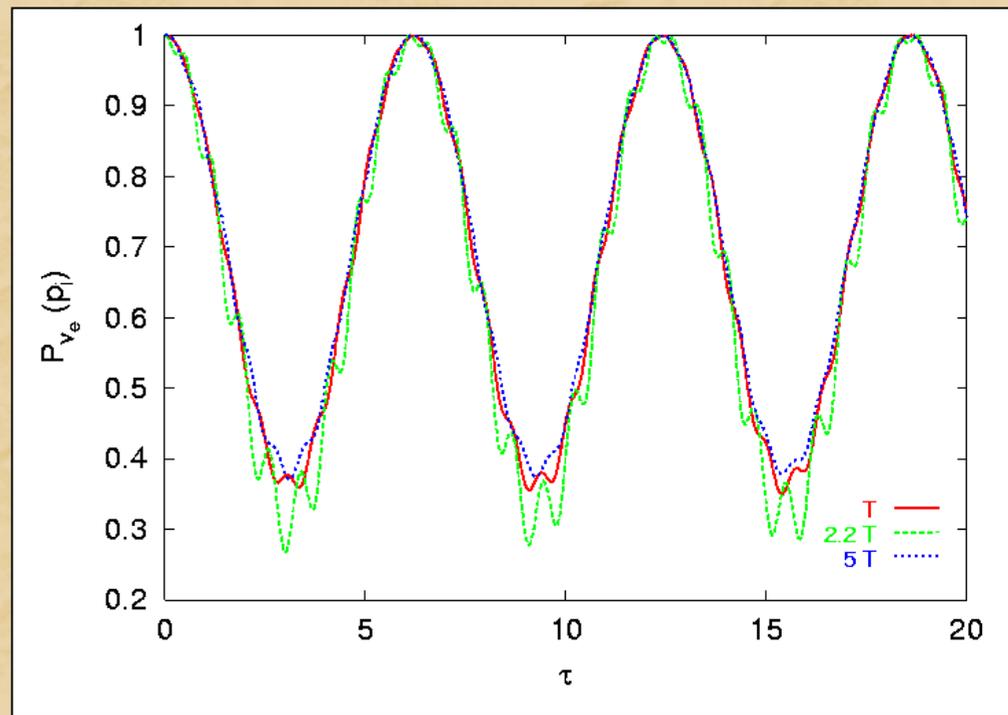
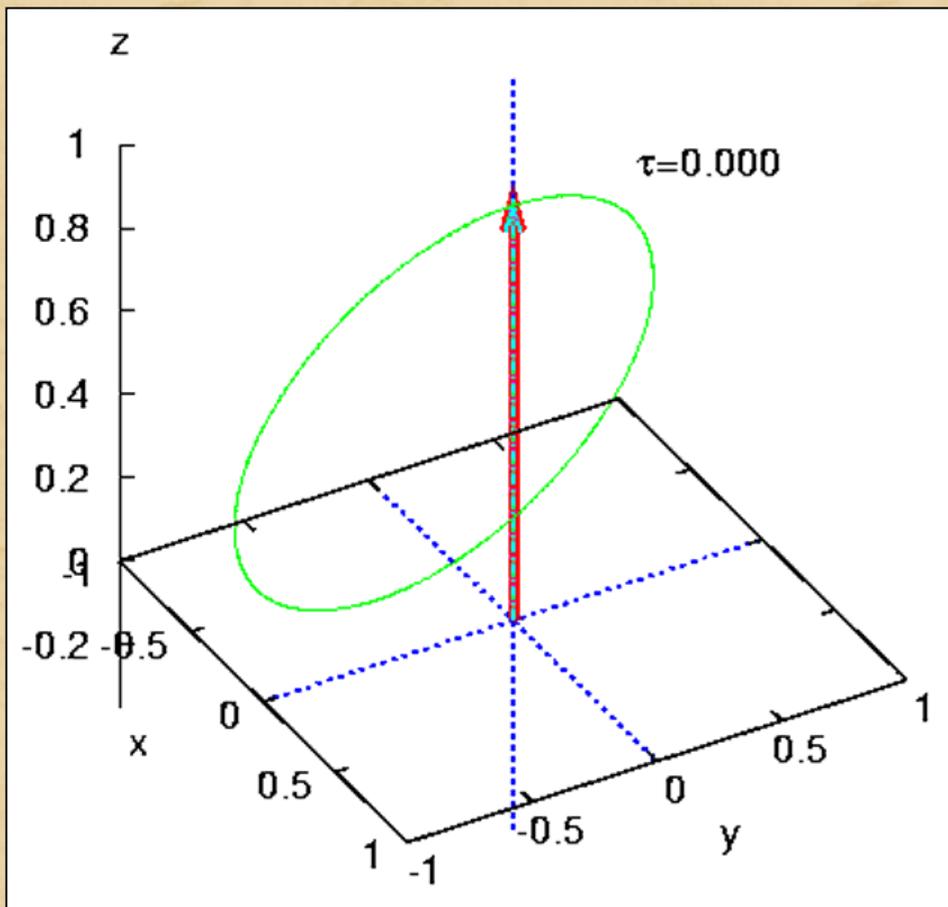
Pastor, Raffelt & Semikoz, PRD 65 (2002) 053011

# Synchronized Oscillations by Self-Interactions



Pastor, Raffelt & Semikoz, PRD 65 (2002) 053011

# Synchronized Oscillations by Self-Interactions



Individual modes precess around large common dipole moment

Pastor, Raffelt & Semikoz, PRD 65 (2002) 053011

# Zero-Frequency Synchronized Oscillations

Synchronized oscillation frequency, assuming all  $P$  vectors start parallel or antiparallel to  $z$ -axis

$$\omega_{\text{synch}} = \frac{\int \frac{d^3p}{(2\pi)^3} \frac{\delta m^2}{2p} (P_p + \bar{P}_p)}{\left| \int \frac{d^3p}{(2\pi)^3} (P_p - \bar{P}_p) \right|}$$

Only neutrinos, no anti-neutrinos

$$\omega_{\text{synch}} = \frac{\delta m^2}{2} \left\langle \frac{1}{p} \right\rangle$$

Equal distribution of neutrinos of one flavor and anti-neutrinos of the other

$$\omega_{\text{synch}} = 0$$

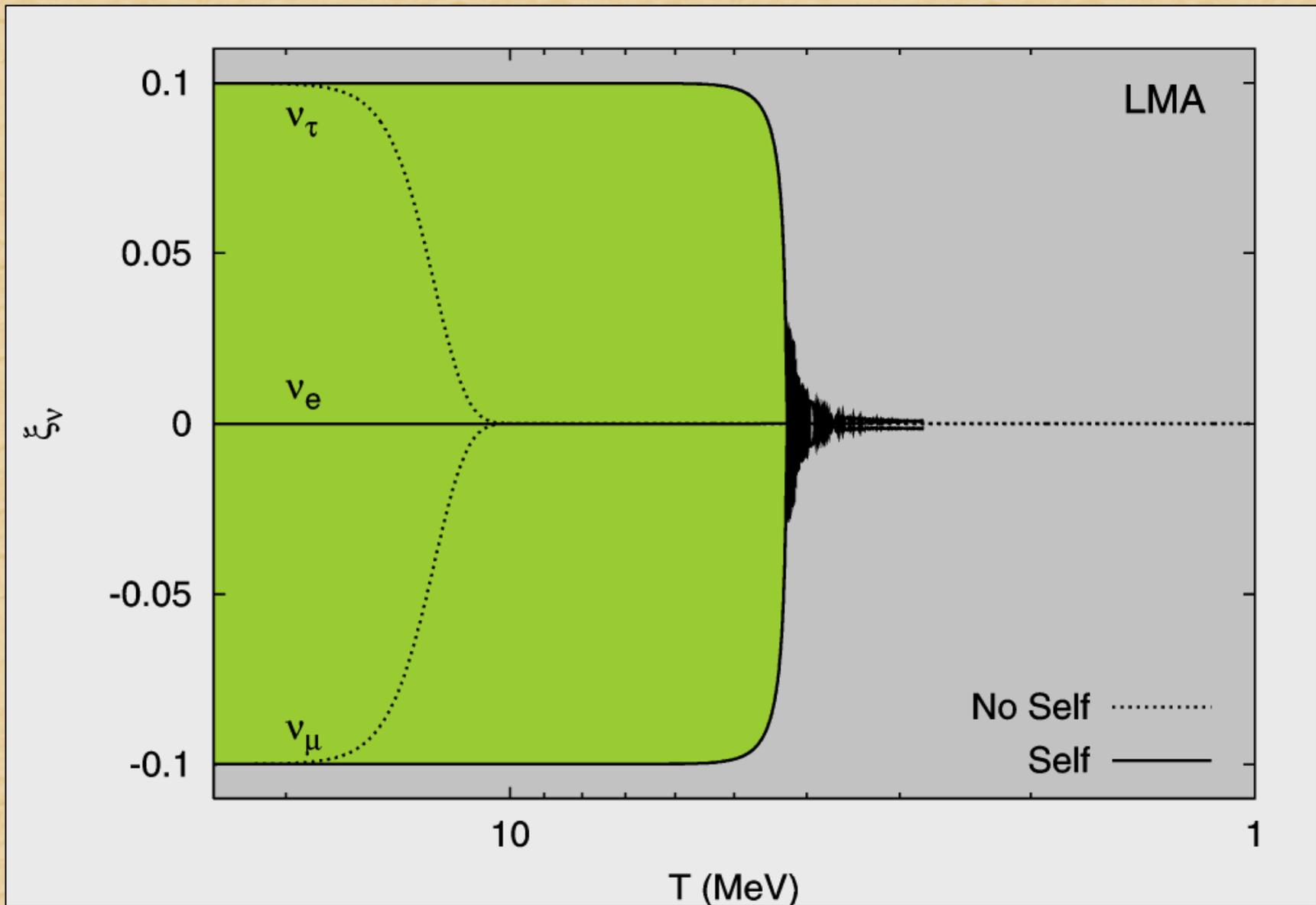
Oscillations completely suppressed

In a three-flavor system, oscillations are suppressed (infinitesimally slow) when

$$|\xi(\nu_e)| = |\xi(\nu_\mu)| = |\xi(\nu_\tau)|$$

Pastor, Raffelt & Semikoz, PRD 65 (2002) 053011

# Flavor Equilibration: LMA and $\xi(\nu_\mu) = -\xi(\nu_\tau)$



Dolgov, Hansen, Pastor, Petcov, Raffelt & Semikoz, hep-ph/0201287

# Summary

Confirmation of solar LMA solution by Kamland



De-facto neutrino flavor equilibrium before BBN

BBN limit on effective number of nu flavors



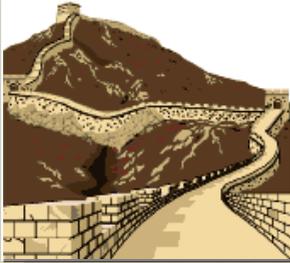
Cosmic nu density within 1% of standard value



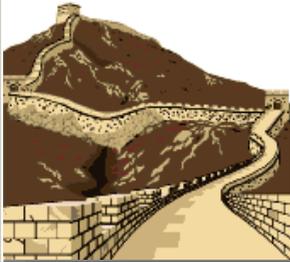
$$\Omega_\nu h^2 = \sum \frac{m_\nu}{94 \text{ eV}}$$

- Laboratory measurements of  $m_\nu$  imply  $\Omega_\nu$
- Structure-formation limits on  $\Omega_\nu$  directly constrain  $m_\nu$

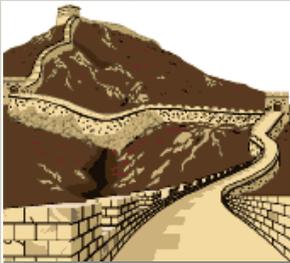
# Lecture II: Cosmological Neutrinos



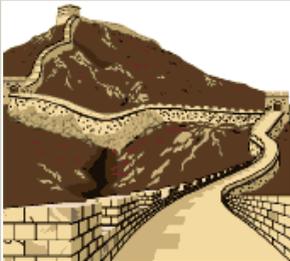
**Neutrino Dark Matter and  
Cosmic Structure Formation**



**Neutrino Chemical Potentials,  
Big-Bang Nucleosynthesis,  
and Flavor Oscillations**

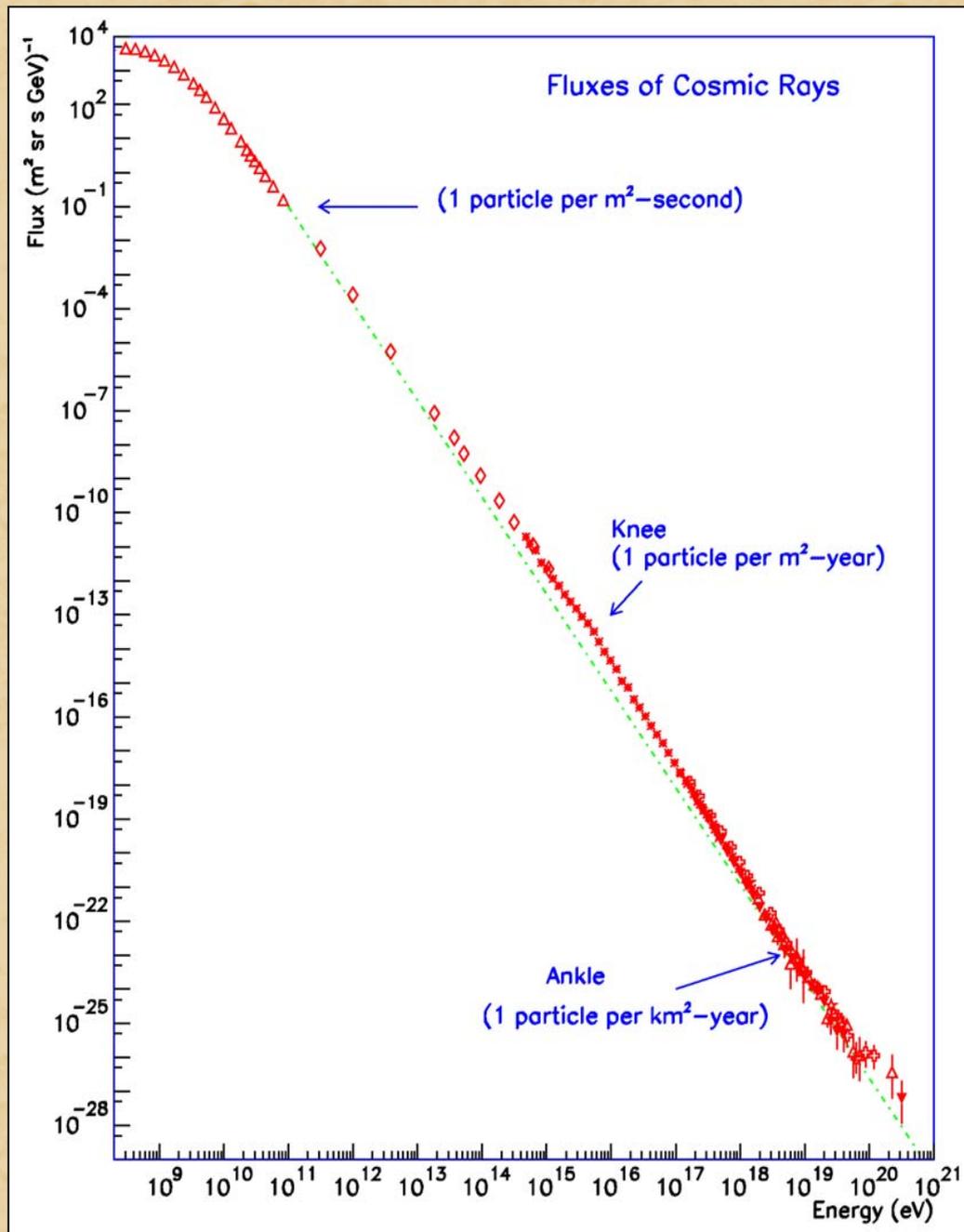


**Highest-Energy Cosmic Rays  
and the Cosmic Neutrino Sea**



**Massive Neutrinos and the  
Cosmic Baryon Asymmetry**

# Global Cosmic Ray Spectrum



# Greisen-Zatsepin-Kuzmin (GZK) Cutoff

END TO THE COSMIC-RAY SPECTRUM?

Kenneth Greisen

Cornell University, Ithaca, New York

(Received 1 April 1966)

PRL 16 (1966) 748



UPPER LIMIT OF THE SPECTRUM OF COSMIC RAYS

G. T. Zatsepin and V. A. Kuz'min

P. N. Lebedev Physics Institute, USSR Academy of Sciences

Submitted 26 May 1966

ZhETF Pis'ma 4, No. 3, 114-117, 1 August 1966

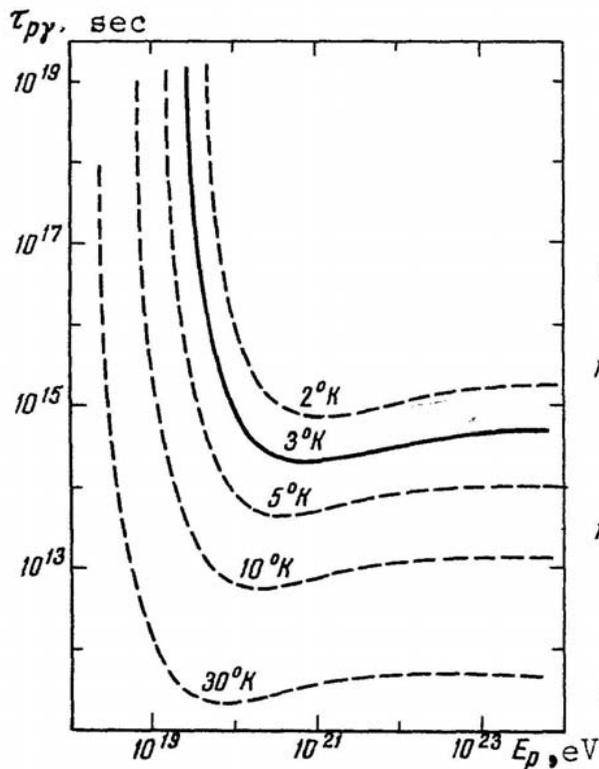


Fig. 1

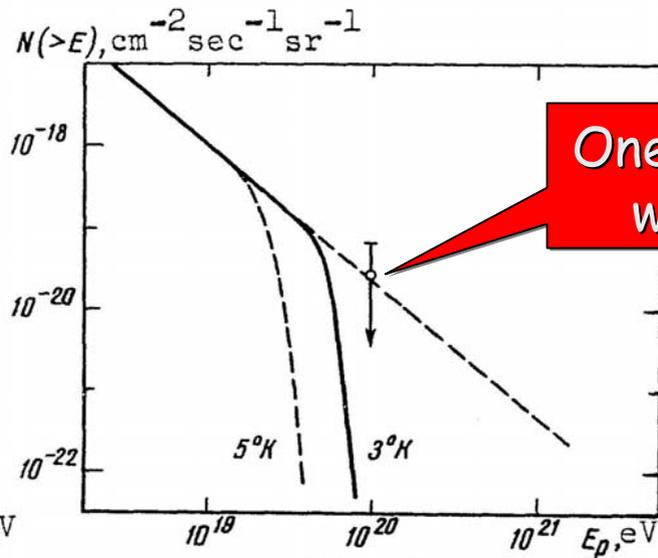


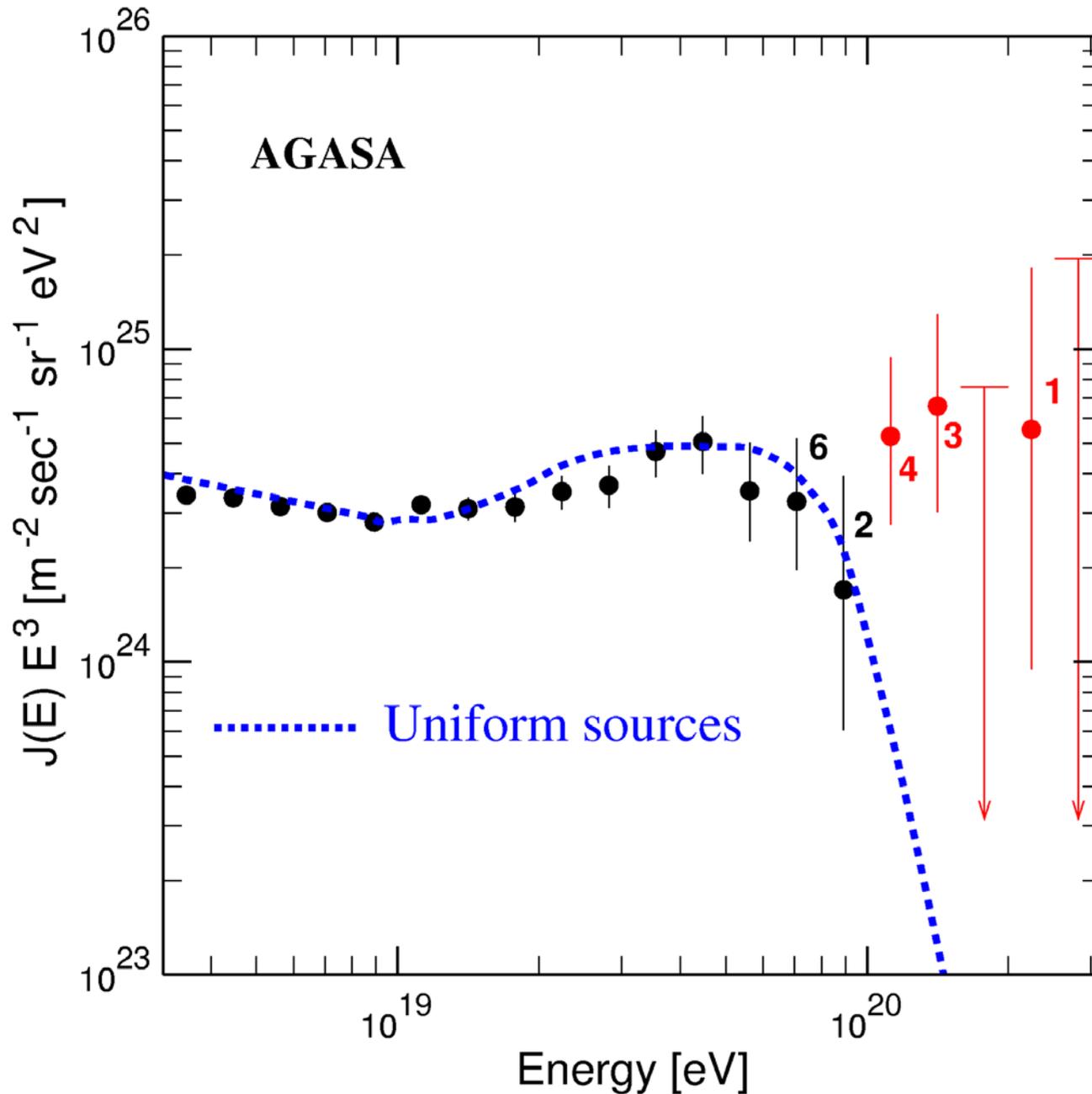
Fig. 2

One event (1962)  
with  $10^{20}$  eV

JETP Lett.  
4 (1966) 78

# Spectrum of Highest-Energy AGASA Events

astro-ph/0008102



# Z-Bursts and Highest-Energy Cosmic Rays

Neutrinos  
 $E_\nu \sim 10^{21} - 10^{22}$  eV  
from unknown sources

Resonant  
Z-Boson  
Production

Cosmic relic  
neutrinos  
 $m_\nu \sim 1$  eV

Neutrino energy  
on resonance

$$E_\nu = \frac{M_Z^2}{2m_\nu} = \frac{4.2 \times 10^{21} \text{ eV}}{m_{\text{eV}}}$$

Decay  
(Z-Burst)

On average  
2 Nucleons

$10 \pi^0 \rightarrow 20 \gamma$

$17 \pi^\pm \rightarrow e^\pm \nu \bar{\nu}$

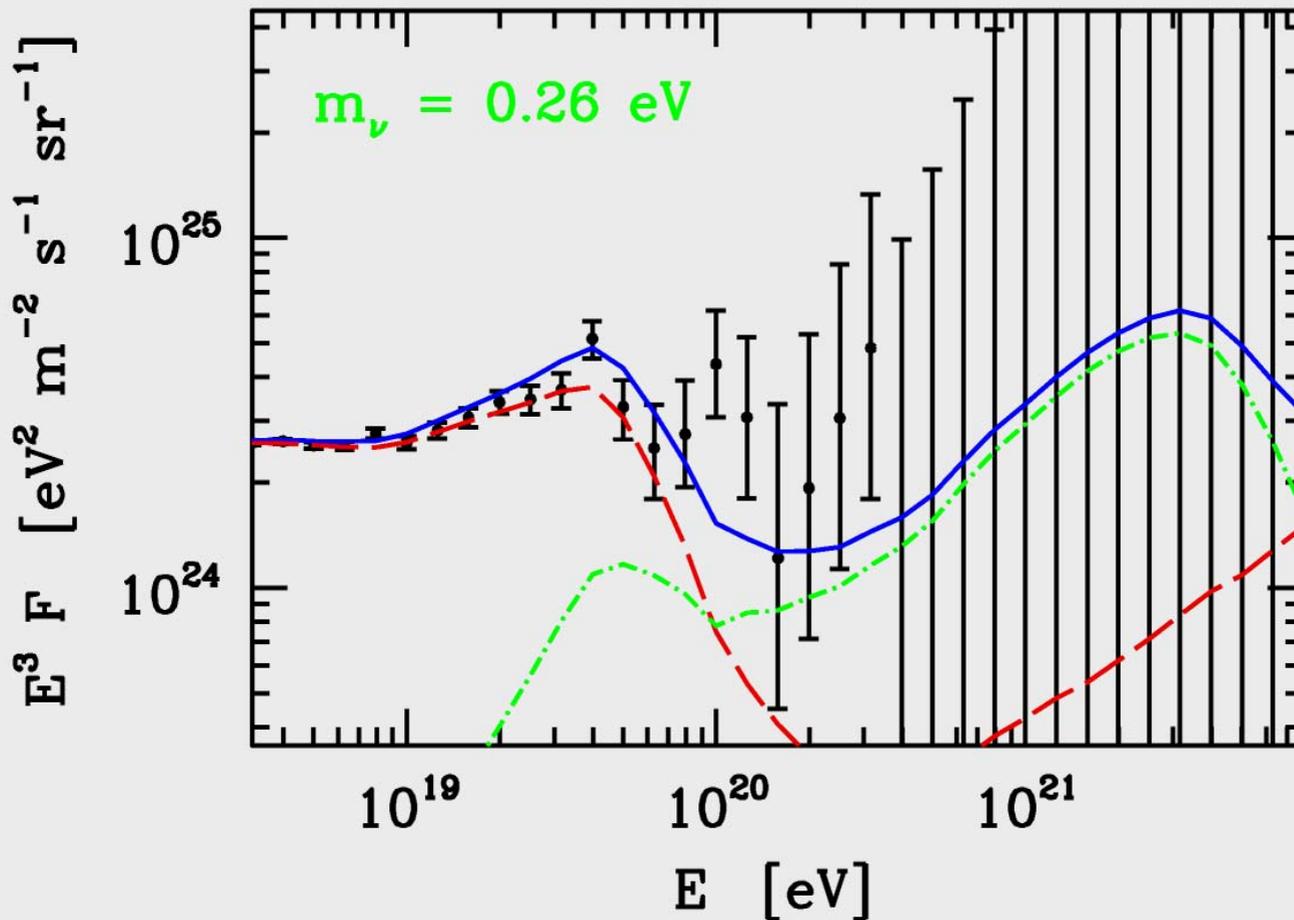
Measured cosmic rays

For example:

- Weiler  
hep-ph/9710431
- Fargion et al.  
hep-ph/0112014
- Fodor, Katz, Ringwald  
hep-ph/0203198

# Fitting the Cosmic Ray Spectrum with Z-Bursts

Cosmic ray spectrum near cutoff can be fit for a wide range of allowed neutrino masses



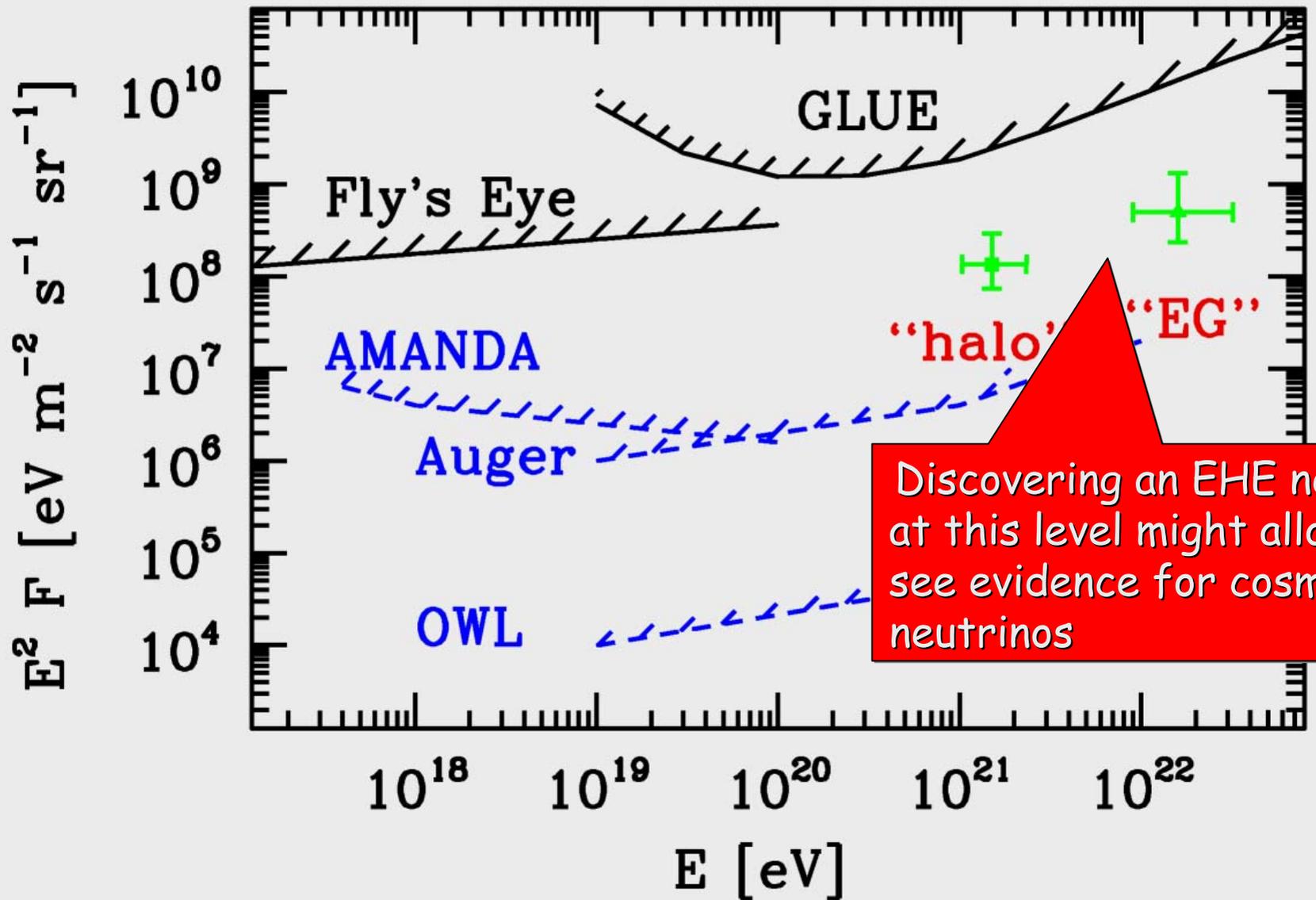
## Main problems

- Huge source flux of EHE neutrinos required
- No plausible sources known
- Accompanying photons must be perfectly obscured

Kalashov et al.  
hep-ph/0112351

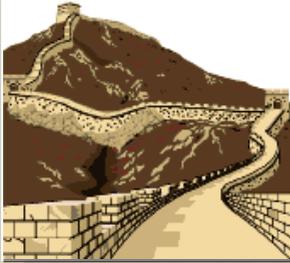
Fodor, Katz & Ringwald, hep-ph/0203198

# Discovery Potential for Required Neutrino Fluxes

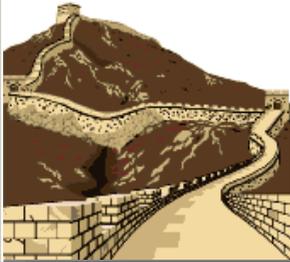


Fodor, Katz & Ringwald, hep-ph/0203198

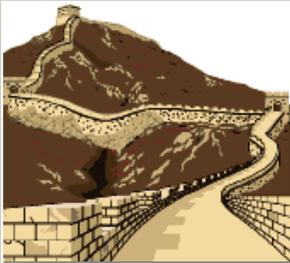
# Lecture II: Cosmological Neutrinos



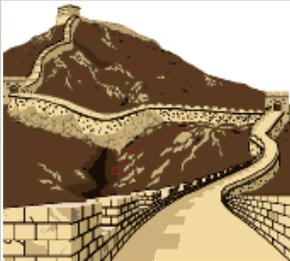
**Neutrino Dark Matter and  
Cosmic Structure Formation**



**Neutrino Chemical Potentials,  
Big-Bang Nucleosynthesis,  
and Flavor Oscillations**



**Highest-Energy Cosmic Rays  
and the Cosmic Neutrino Sea**



**Massive Neutrinos and the  
Cosmic Baryon Asymmetry**

# Baryogenesis in the Early Universe

Sakharov conditions for creating the **Baryon Asymmetry of the Universe (BAU)**

- C and CP violation
- Baryon number violation
- Deviation from thermal equilibrium

Particle-physics standard model

- Violates B and L by electroweak instanton effects
- Conserves B - L

In cosmological evolution

- Pre-existing B+L erased at EW phase transition
- Creation of BAU at phase transition not possible, except for special parameters in SUSY models

## Another classic paper

Volume 174, number 1

PHYSICS LETTERS B

26 June 1986

### **BARYOGENESIS WITHOUT GRAND UNIFICATION**

**M. FUKUGITA**

*Research Institute for Fundamental Physics, Kyoto University, Kyoto 606, Japan*

and

**T. YANAGIDA**

*Institute of Physics, College of General Education, Tohoku University, Sendai 980, Japan  
and Deutsches Elektronen-Synchrotron DESY, D-2000 Hamburg, Fed. Rep. Germany*

Received 8 March 1986

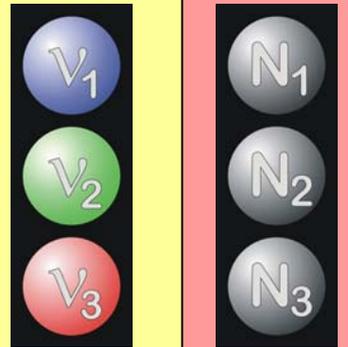
A mechanism is pointed out to generate cosmological baryon number excess without resorting to grand unified theories. The lepton number excess originating from Majorana mass terms may transform into the baryon number excess through the unsuppressed baryon number violation of electroweak processes at high temperatures.

# See-Saw Model for Neutrino Masses

## Charged Leptons



## Neutrinos



Dirac masses from coupling to standard Higgs field  $\phi$

Heavy Majorana masses  $M_j$

Lagrangian for particle masses

$$L_{\text{mass}} = -\bar{\ell}_L \phi g_\ell e_R - \bar{\ell}_L \phi g_\nu N_R - \frac{1}{2} \bar{N}_R^c M N_R + \text{h.c.}$$

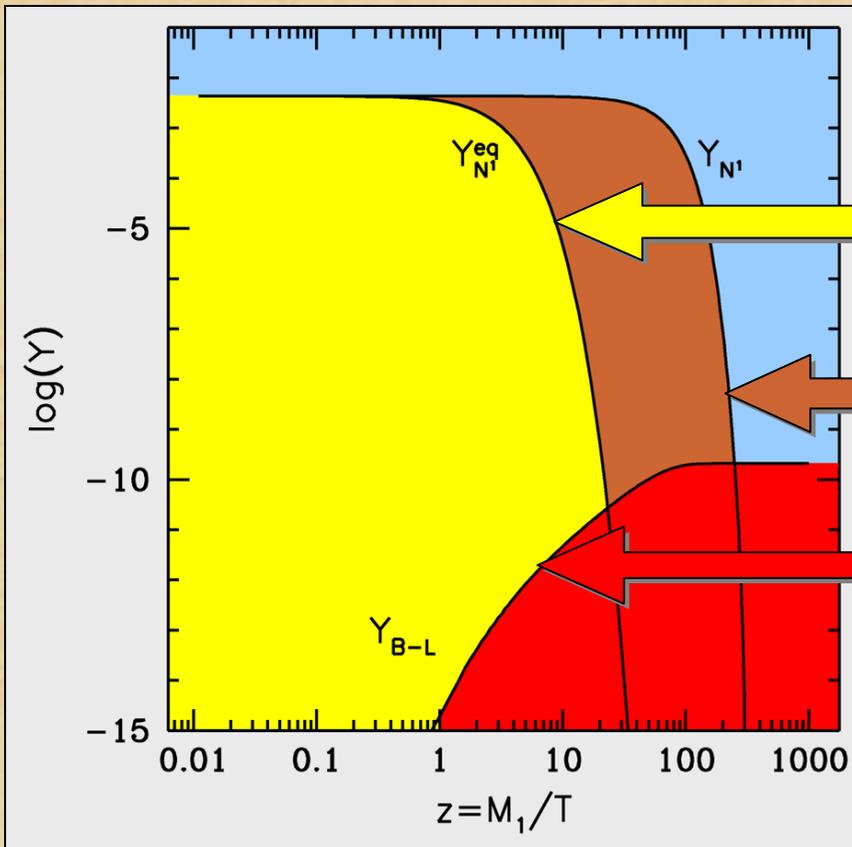
## Light Majorana mass

$$(\bar{\nu}_L \quad \bar{N}_R) \begin{pmatrix} 0 & g_\nu \langle \phi \rangle \\ g_\nu \langle \phi \rangle & M \end{pmatrix} \begin{pmatrix} \nu_L \\ N_R \end{pmatrix}$$



$$(\bar{\nu}_L \quad \bar{N}_R) \begin{pmatrix} \frac{g_\nu^2 \langle \phi \rangle^2}{M} & 0 \\ 0 & M \end{pmatrix} \begin{pmatrix} \nu_L \\ N_R \end{pmatrix}$$

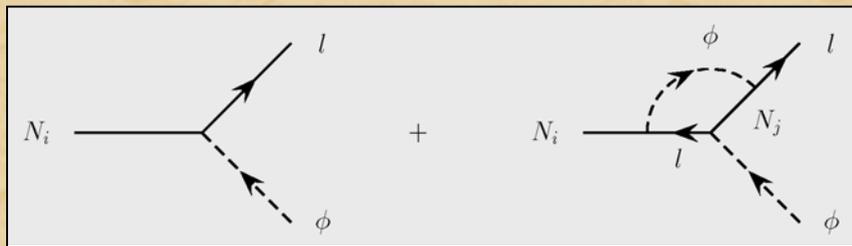
# Leptogenesis by Out-of-Equilibrium Decay



Equilibrium abundance of heavy Majorana neutrinos

Real non-equilibrium abundance determined by decay rate

Lepton-number abundance created by CP-violating decays



CP-violating decays by interference of tree-level with one-loop diagram

$$\Gamma_{\text{Decay}} = g_v^2 \frac{M}{8\pi}$$

# Connection to Neutrino Mass

$$\Gamma_{\text{Decay}} = g_v^2 \frac{M}{8\pi}$$

Decay rate of heavy Majorana neutrino

$$H \approx \sqrt{g_{\text{eff}}} \frac{T^2}{m_{\text{pl}}}$$

Cosmic expansion rate

$$\Gamma_{\text{Decay}} < H|_{T=M}$$

Requirement for strong deviation from equilibrium ...

$$g_v^2 \frac{M}{8\pi} < \sqrt{g_{\text{eff}}} \frac{M^2}{m_{\text{pl}}}$$

$$\frac{g_v^2}{M} < \frac{8\pi\sqrt{g_{\text{eff}}}}{m_{\text{pl}}}$$

$$m_\nu = \frac{g_v^2 \langle \phi \rangle^2}{M} < \frac{8\pi\sqrt{g_{\text{eff}}}}{m_{\text{pl}}} \langle \phi \rangle^2 \sim 10^{-3} \text{ eV}$$

... translates into a limit on the observable neutrino mass

# Leptogenesis by Majorana Neutrino Decays

In see-saw models of neutrino masses, right-handed heavy Majorana neutrinos provide source for L-violation

Cosmological evolution:

- $B = L = 0$  early on
- Thermal freeze-out of heavy Majorana neutrinos
- Out-of-equilibrium CP-violating decay creates net L
- Shift L excess into B by sphaleron effects

Sufficient deviation from equilibrium distribution of heavy Majorana neutrinos at freeze-out

Limits on Yukawa couplings

Limits on *light* neutrino masses

Consistent with hierarchical masses below 0.1 eV

# Leptogenesis - A Popular Research Topic

Fukugita & Yanagida  
PLB 174 (1986) 45

Langacker, Peccei & Yanagida  
Mod. Phys. Lett. A 1 (1986) 541

Campbell, Davidson & Olive  
NPB 399 (1993) 111

Gherghetta & Jungmann  
PRD 48 (1993) 1546

Muryama & Yanagida  
PLB 322 (1994) 349

Worah  
PRD 53 (1996) 3902

Jeannerot  
PRL 77 (1996) 3292

Dine, Randall & Thomas  
NPB 458 (1996) 291

Buchmüller & Plümacher  
PLB 389 (1996) 73

Lazarides, Schaefer & Shafi  
PRD 56 (1997) 1324

Ma & Sarkar  
PRL 80 (1998) 5716

Plümacher  
NPB 530 (1998) 207

Flanz & Paschos  
PRD 58 (1998) 113009

Lazarides & Shafi  
PRD 58 (1998) 071702

Akhmedov, Rubakov & Smirnov  
PRL 81 (1998) 1562

Carlier, Frère & Ling  
PRD 60 (1999) 096003

Giudice, Peloso, Riotto & Tkachev  
JHEP 9908 (1999) 014

Berger & Brahmachari  
PRD 60 (1999) 073009

Ellis, Lola & Nanopoulos  
PLB 452 (1999) 87

Barbieri, Creminelli, Strumia & Tetradis  
NPB 575 (2000) 61

Frère, Ling, Tytgat & v.Elewyck  
PRD 60 (1999) 016005

Dick, Lindner, Ratz & Wright  
PRL 84 (2000) 4039

Lalakulich, Paschos & Flanz  
PRD 62 (2000) 053006

Asaka, Hamaguchi, Kawasaki & Yanagida  
PRD 61 (2000) 083512

Berger  
PRD 62 (2000) 013007

Hambye, Ma & Sarkar  
PRD 62 (2000) 015010

Mangano & Miele  
PRD 62 (2000) 063514

Goldberg  
PLB 474 (2000) 389

Rangarajan & Mishra  
PRD 61 (2000) 043509

Hirsch & King  
PRD 64 (2001) 113005

Falcone & Tramontano  
PRD 63 (2001) 073007

Bastero-Gil & King  
PRD 63 (2001) 123509

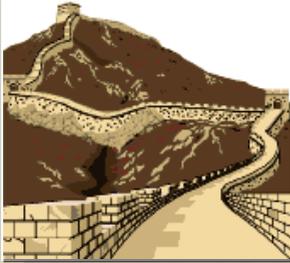
Joshiyura, Paschos & Rodejohann  
NPB 611 (2001) 227

Branco, Morozumi, Nobre & Rebelo  
NPB 617 (2001) 475

Hambye, Ma & Sarkar  
NPB 602 (2001) 23

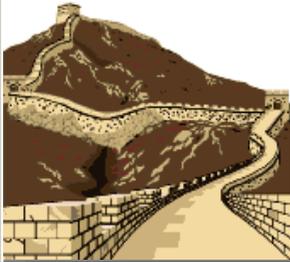
AND MANY MORE ...

# Conclusions of Lecture II

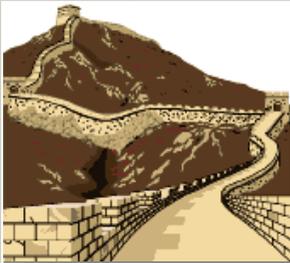


Large-scale galaxy redshift surveys

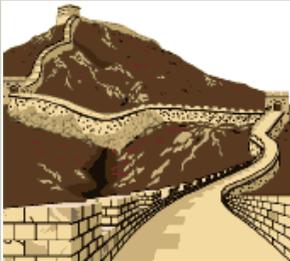
- Best limit of  $m_\nu < 0.8 \text{ eV}$ ,
- Future sensitivity  $\sim 0.3 \text{ eV}$



If solar LMA solution applies,  
cosmic neutrino number density  
precisely determined by BBN



If highest-E cosmic-ray neutrinos are found,  
Z-bursts provide handle on  $m_\nu$



Majorana neutrino masses in the favored  
range suggest a leptogenesis scenario  
for generating cosmic baryon asymmetry