

Loop Blow-up Inflation



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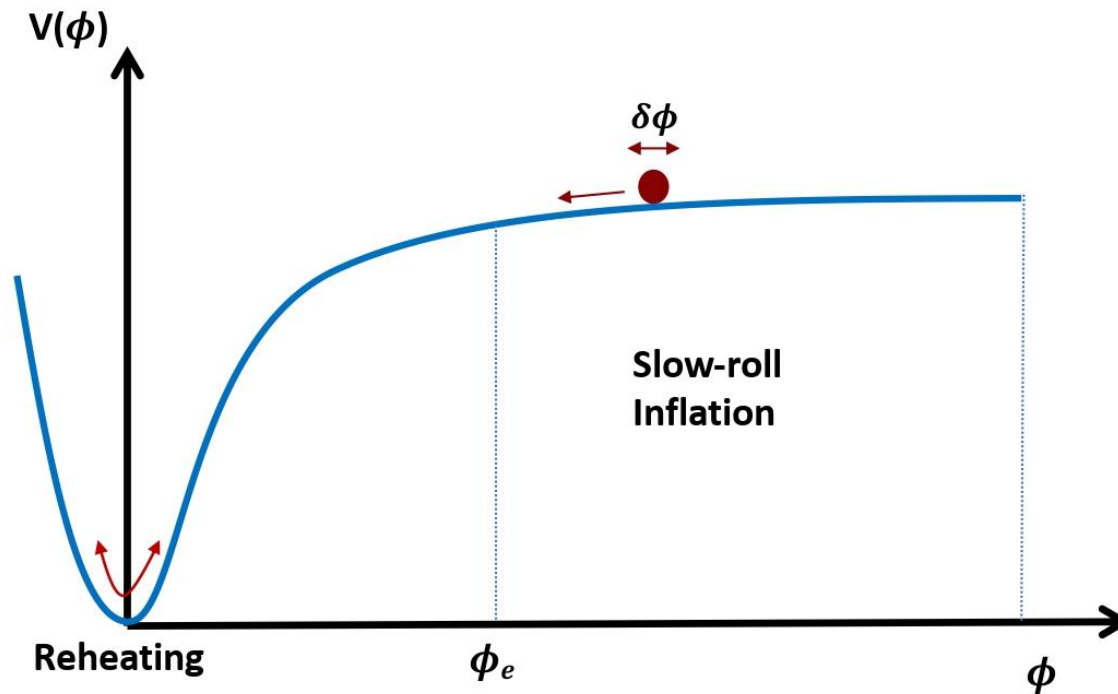


ALMA MATER STUDIORUM
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Based on:

S. Bansal, L. Brunelli, MC, A. Hebecker, R. Kuespert, 2403.04831

Standard slow-roll



$$V(\phi) = V_0[1 - g(\phi)] \simeq V_0$$

since $g(\phi) \ll 1$ for $\phi \gg 1$

Inflating with the Kaehler moduli

- Slow-roll picture with inflaton ϕ reproduced with type IIB Kaehler moduli
- Volume mode $\mathcal{V}$ couples to all sources of energy due to $e^K = \mathcal{V}^{-2}$
 - cannot have a ϕ -independent plateau if $\phi \equiv \mathcal{V}$
 - ϕ should be a direction $\perp \mathcal{V}$: $\phi \equiv \tau_\phi$
- Since each term in V depends on $\mathcal{V}$, $V(\phi) \simeq V_0$ only if leading dynamics fixes $\mathcal{V}$ but not τ_ϕ
 - $\phi \equiv \tau_\phi$ is a leading order flat direction with an approximate shift symmetry
[Burgess,MC,Quevedo,Williams][Burgess,MC,deAlwis,Quevedo]
- Type IIB Kaehler sector: tree-level no-scale cancellation
+ 1-loop extended no-scale [MC,Conlon,Quevedo]
- Leading no-scale breaking effects lift only $\mathcal{V}$:
 - i) $V_{\alpha'^3}(\mathcal{V})$ from $O(\alpha'^3)$ effects [Becker,Becker,Haack,Louis]
 - ii) $V_{up}(\mathcal{V})$ from uplifting (anti-D3, T-branes, $F^{cs} \neq 0$, FI-terms,...)
 - iii) $V_{np}(\mathcal{V})$ from non-pert. effects on n_{dP} dP divisors (after integrating out the dP moduli)
 - LVS dS min with $(h^{1,1} - 1 - n_{dP})$ flat directions which can all be ϕ
 - ϕ lifted by subdominant quantum effects

Leading dynamics

- Total potential with 1 leading order flat direction τ_ϕ :

$$V_{\text{tot}}(\mathcal{V}, \tau_\phi) = V_{\text{lead}}(\mathcal{V}) - V_{\text{sub}}(\mathcal{V}, \tau_\phi) \quad V_{\text{sub}}(\mathcal{V}, \tau_\phi) \ll V_{\text{lead}}(\mathcal{V})$$

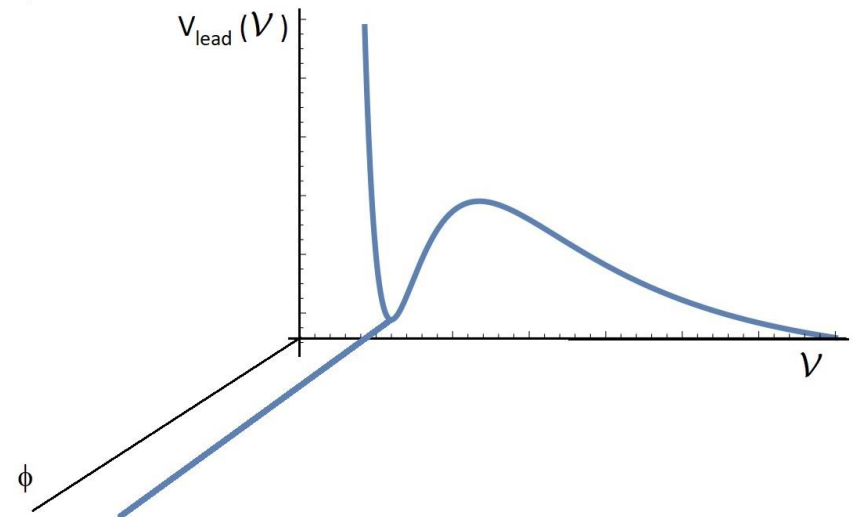
- Stabilisation:

$$\frac{\partial V_{\text{lead}}}{\partial \mathcal{V}}(\langle \mathcal{V} \rangle) = 0 \quad \text{and} \quad \frac{\partial V_{\text{sub}}}{\partial \tau_\phi}(\langle \mathcal{V} \rangle, \langle \tau_\phi \rangle) = 0$$

with:

$$V_{\text{lead}}(\langle \mathcal{V} \rangle) = V_{\text{sub}}(\langle \mathcal{V} \rangle, \langle \tau_\phi \rangle)$$

$$\longrightarrow V_{\text{tot}}(\langle \mathcal{V} \rangle, \langle \tau_\phi \rangle) = 0$$



Subleading dynamics

- Setting $\mathcal{V} = \langle \mathcal{V} \rangle$, $V_{\text{tot}}(\langle \mathcal{V} \rangle, \tau_\phi)$ becomes:

$$V(\phi) = V_0[1 - g(\phi)]$$

with:

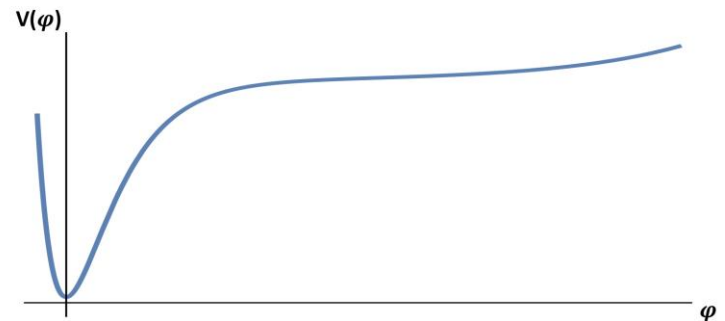
$$V_0 \equiv V_{\text{sub}}(\langle \mathcal{V} \rangle, \langle \tau_\phi \rangle) \quad \text{and} \quad g(\phi) \equiv \frac{V_{\text{sub}}(\langle \mathcal{V} \rangle, \tau_\phi(\phi))}{V_{\text{sub}}(\langle \mathcal{V} \rangle, \langle \tau_\phi \rangle)}$$

where $\tau_\phi(\phi)$ is determined by canonical normalisation

- Since τ_ϕ is a leading order flat direction

$$V_{\text{sub}}(\langle \mathcal{V} \rangle, \tau_\phi) \ll V_{\text{sub}}(\langle \mathcal{V} \rangle, \langle \tau_\phi \rangle) \quad \text{for} \quad \tau_\phi > \langle \tau_\phi \rangle$$

→ $g(\phi) \ll 1 \quad \text{and} \quad V(\phi) \simeq V_0 \quad \text{for} \quad \phi \gg 1$



String inflation potentials

Function $g(\phi)$ depends on 2 features:

1. Origin of effects which generate $V_{\text{sub}}(\langle \mathcal{V} \rangle, \tau_\phi)$:

- **Perturbative** effects:

$$V_{\text{sub}}(\langle \mathcal{V} \rangle, \tau_\phi) \propto \frac{1}{\tau_\phi^p} \rightarrow 0 \quad \text{for } \tau_\phi \rightarrow \infty \text{ if } p > 0$$

- **Non-perturbative** effects:

$$V_{\text{sub}}(\langle \mathcal{V} \rangle, \tau_\phi) \propto e^{-k\tau_\phi} \rightarrow 0 \quad \text{for } \tau_\phi \rightarrow \infty \text{ if } k > 0$$

2. Topology of τ_ϕ which determines $\tau_\phi(\phi)$ (canonical normalisation):

- **Bulk** (fibre) modulus:

$$\tau_\phi = e^{\lambda\phi} \quad \text{with} \quad \lambda \sim \mathcal{O}(1)$$

- **Local** (blow-up) modulus:

$$\tau_\phi = \mu \mathcal{V}^{2/3} \phi^{4/3} \quad \text{with} \quad \mu \sim \mathcal{O}(1)$$

String inflation potentials

$$V(\phi) = V_0[1 - g(\phi)]$$

- Non-perturbative Blow-up Inflation: [Conlon,Quevedo][Bond,Kofman,Prokushkin,Vaudrevange]

$$g(\phi) \propto e^{-k\mu \nu^{2/3} \phi^{4/3}} \ll 1 \quad \text{for} \quad \phi > 0$$

- Non-perturbative Fibre Inflation: [MC,Pedro,Tasinato][Luest,Zhang]

$$g(\phi) \propto e^{-k e^{\lambda\phi}} \ll 1 \quad \text{for} \quad \phi > 0$$

- Loop Fibre Inflation: [MC,Burgess,Quevedo][Broy,Ciupke,Pedro,Westphal][MC,Ciupke,deAlwis,Muia]

$$g(\phi) \propto e^{-p\lambda\phi} \ll 1 \quad \text{for} \quad \phi > 0$$

- Loop Blow-up Inflation: [Bansal,Brunelli,MC,Hebecker,Kuespert]

$$g(\phi) \propto \frac{1}{\nu^{2p/3} \phi^{4p/3}} \ll 1 \quad \text{for} \quad \phi \lesssim 1$$

$$p = 1/2$$



$$V = V_0 \left(1 - \frac{c}{\nu^{1/3} \phi^{2/3}} \right)$$

The model

- Type IIB compactification on CY with volume:

$$\mathcal{V} = \tau_b^{3/2} - \tau_s^{3/2} - \tau_\phi^{3/2} \simeq \tau_b^{3/2} \quad T_i = \tau_i + i\vartheta_i$$

- Kaehler potential (tree-level + α'^3) and superpotential (tree-level + non-pert.):

$$K = -2 \ln \left(\mathcal{V} - \frac{\xi}{2g_s^{3/2}} \right) \quad W = W_0 + A_s e^{-a_s T_s} + A_\phi e^{-a_\phi T_\phi}$$

- Scalar potential:

$$V = V_{\text{lead}}(\mathcal{V}, \tau_s) + V_{\text{sub}}(\mathcal{V}, \tau_\phi)$$

$$V_{\text{lead}}(\mathcal{V}, \tau_s) = C_0 \left[\frac{C_{up}}{\mathcal{V}^2} + C_s \frac{\sqrt{\tau_s} e^{-2a_s \tau_s}}{\mathcal{V}} - D_s \frac{\tau_s e^{-a_s \tau_s}}{\mathcal{V}^2} + \frac{3\xi}{4g_s^{3/2} \mathcal{V}^3} \right]$$

$$V_{\text{sub}}(\mathcal{V}, \tau_\phi) = C_0 \left[C_\phi \frac{\sqrt{\tau_\phi} e^{-2a_\phi \tau_\phi}}{\mathcal{V}} - D_\phi \frac{\tau_\phi e^{-a_\phi \tau_\phi}}{\mathcal{V}^2} \right] \quad a_s^{3/2} \ll a_\phi^{3/2}$$

- Minkowski minimum at:

$$\tau_s \sim (\xi/2)^{2/3} g_s^{-1} \quad \mathcal{V} \sim e^{a_s \tau_s} \sim e^{a_\phi \tau_\phi}$$

Loop corrections

- 1-loop K computed only in toroidal orientifolds: [Berg,Haack,Koers]

$$\mathcal{V} = \sqrt{\tau_1 \tau_2 \tau_3}$$

$$\delta K_{(g_s)} = \delta K_{(g_s)}^{KK} + \delta K_{(g_s)}^W$$

- i) tree-level exchange of KK closed strings between parallel D7/O7s:

$$\delta K_{(g_s)}^{KK} = g_s \left(\frac{C_1^{KK}(U, \bar{U})}{\tau_1} + \frac{C_2^{KK}(U, \bar{U})}{\tau_2} + \frac{C_3^{KK}(U, \bar{U})}{\tau_3} \right)$$

- ii) tree-level exchange of winding closed strings at D7 intersection:

$$\delta K_{(g_s)}^W = \frac{C_1^W(U, \bar{U})}{\tau_2 \tau_3} + \frac{C_2^W(U, \bar{U})}{\tau_1 \tau_3} + \frac{C_3^W(U, \bar{U})}{\tau_1 \tau_2}$$

- Closed string 1-loops (Klein bottle) cancel with some open string 1-loops (Moebius strip)

→ remain with just open string 1-loop correction to K
not necessarily true for CYs (with different brane setups)

- Conjecture for 1-loop K for CYs: [Berg,Haack,Pajer]

$$\delta K_{(g_s)}^{KK} = g_s \sum_i \frac{C_i^{KK}(U, \bar{U}) t_i}{\mathcal{V}} = \frac{g_s}{\mathcal{V}} \sum_i C_i^{KK}(U, \bar{U}) M_{KK,i}^{-2} \longrightarrow \text{Extended no-scale cancellation in V [MC,Conlon,Quevedo]}$$

$$\delta K_{(g_s)}^W = \sum_i \frac{C_i^W(U, \bar{U})}{\mathcal{V} t_i} = \frac{1}{\mathcal{V}} \sum_i C_i^W(U, \bar{U}) M_{W,i}^{-2}$$

Loop corrections from 4D

- 1-loop K yields corrections to kinetic terms and V

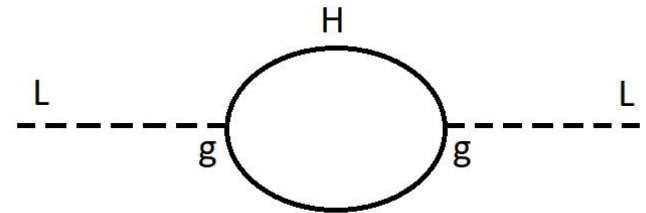
→ field theory interpretation [von Gersdorff, Hebecker][MC, Conlon, Quevedo][Gao, Hebecker, Schreyer, Venken]

- Heavy mode H coupled to a light mode L

$$\mathcal{L} \supset M^2 H^2 + g L H^2$$

- 2-point function 1-loop renormalisation:

$$\mathcal{L}_{kin} = \left[1 + c_{loop} \left(\frac{g}{M} \right)^2 \right] \partial_\mu L \partial^\mu L \quad c_{loop} \simeq \frac{1}{16\pi^2}$$



- Compute coupling g :

$$M^2(\tau) H^2 \simeq M^2 H^2 + \frac{\partial M^2}{\partial \tau} \Big|_{\langle \tau \rangle} \hat{\tau} H^2 \simeq M^2 H^2 + M^2 \frac{\hat{\tau}}{\langle \tau \rangle} H^2 \quad M^2 \equiv M^2(\langle \tau \rangle)$$

$$\frac{\hat{\tau}}{\langle \tau \rangle} \simeq \frac{L}{M_p} \quad \Rightarrow \quad g \simeq \frac{M^2}{M_p}$$

- 1-loop correction to K:

$$\mathcal{L}_{kin} = \left[1 + c_{loop} \left(\frac{M}{M_p} \right)^2 \right] \partial_\mu L \partial^\mu L \simeq \left[1 + c_{loop} \left(\frac{M}{M_p} \right)^2 \right] \frac{\partial_\mu \hat{\tau} \partial^\mu \hat{\tau}}{\langle \tau \rangle^2} = (K_{\tau\tau} + \delta K_{\tau\tau}) \partial_\mu \hat{\tau} \partial^\mu \hat{\tau}$$

→ $K_{\tau\tau} \simeq \frac{1}{\tau^2} \quad \delta K_{\tau\tau} \simeq \frac{c_{loop}}{\tau^2} \left(\frac{M}{M_p} \right)^2 \quad \Rightarrow \quad K = -3 \ln \tau$

$$\delta K \simeq c_{loop} \left(\frac{M}{M_p} \right)^2$$

Loop corrections from 4D

$$\delta K \simeq c_{\text{loop}} \left(\frac{M}{M_p} \right)^2$$

- If H = massive string state:

$$M \equiv M_s \simeq \frac{M_p}{\sqrt{\mathcal{V}}} \Rightarrow \delta K \simeq \frac{c_{\text{loop}}}{\mathcal{V}} \quad \text{matches scaling of } \delta K_{\alpha'^3} \text{ [Becker,Becker,Haack,Louis]}$$

no dependence on τ_ϕ $\longrightarrow$ irrelevant for inflation

- If H = winding mode:

$$M \equiv M_W \simeq M_s \tau^{1/4} \simeq \frac{M_p}{\sqrt{\mathcal{V}}} \tau^{1/4} \Rightarrow \delta K \simeq c_{\text{loop}} \frac{\sqrt{\tau}}{\mathcal{V}} \quad \text{matches scaling of } \delta K_{(g_s)}^{KK} \text{ [Berg,Haack,Pajer]}$$

$\longrightarrow \delta K_{(g_s)}^{KK}$ = tree-level KK closed strings = 1-loop winding open strings

extended no-scale suppresses contribution to $\mathcal{V}$ $\longrightarrow$ irrelevant for inflation

- If H = Kaluza-Klein mode:

$$M \equiv M_{KK} \simeq \frac{M_s}{\tau^{1/4}} \simeq \frac{M_p}{\sqrt{\mathcal{V}} \tau^{1/4}} \Rightarrow \delta K \simeq \frac{c_{\text{loop}}}{\mathcal{V} \sqrt{\tau}} \quad \text{matches scaling of } \delta K_{(g_s)}^W \text{ [Berg,Haack,Pajer]}$$

$\longrightarrow \delta K_{(g_s)}^W$ = tree-level winding closed strings = 1-loop KK open strings

if $\tau = \tau_\phi$ $\delta K \simeq \frac{c_{\text{loop}}}{\mathcal{V} \sqrt{\tau_\phi}} \Rightarrow \boxed{\delta V \simeq \frac{c_{\text{loop}}}{\mathcal{V}^3 \sqrt{\tau_\phi}}}$ leading correction to $\mathcal{V}$ $\longrightarrow$ crucial for inflation

Loop corrections from 4D

- 1-loop K from KK modes in loop should match 1-loop Coleman-Weinberg potential:

$$V_{1\text{-loop}}^{CW} \simeq \frac{1}{16\pi^2} \Lambda^2 \text{Str } M^2 \quad [\text{MC, Conlon, Quevedo}]$$

- Supertrace in supergravity:

$$\text{Str } M^2 \simeq m_{3/2}^2 \simeq \frac{M_p^2}{\mathcal{V}^2}$$

- Cut-off Λ given by KK mass of open strings on D7s

i) D7s on τ_b : $\Lambda \simeq \frac{M_p}{\mathcal{V}^{2/3}}$

$$\delta V_{(g_s)} \simeq \frac{c_{\text{loop}}}{\mathcal{V}^{10/3}}$$

no dependence on $\tau_\phi \longrightarrow$ irrelevant for inflation

ii) D7s on τ_ϕ : $\Lambda \simeq \frac{M_p}{\tau_\phi^{1/4} \sqrt{\mathcal{V}}}$

$$\delta V_{(g_s)} \simeq \frac{c_{\text{loop}}}{\mathcal{V}^3 \sqrt{\tau_\phi}}$$

same τ_ϕ dependence as from 1-loop 2-pt function

- If there is no D7 on τ_ϕ , can still have KK modes of τ_ϕ (closed strings) in loop

- τ_ϕ and its KK modes are localised around blow-up mode $\longrightarrow$ again $\Lambda \simeq \frac{M_p}{\tau_\phi^{1/4} \sqrt{\mathcal{V}}}$

$\longrightarrow$ τ_ϕ -dependent loop corrections to V are unavoidable

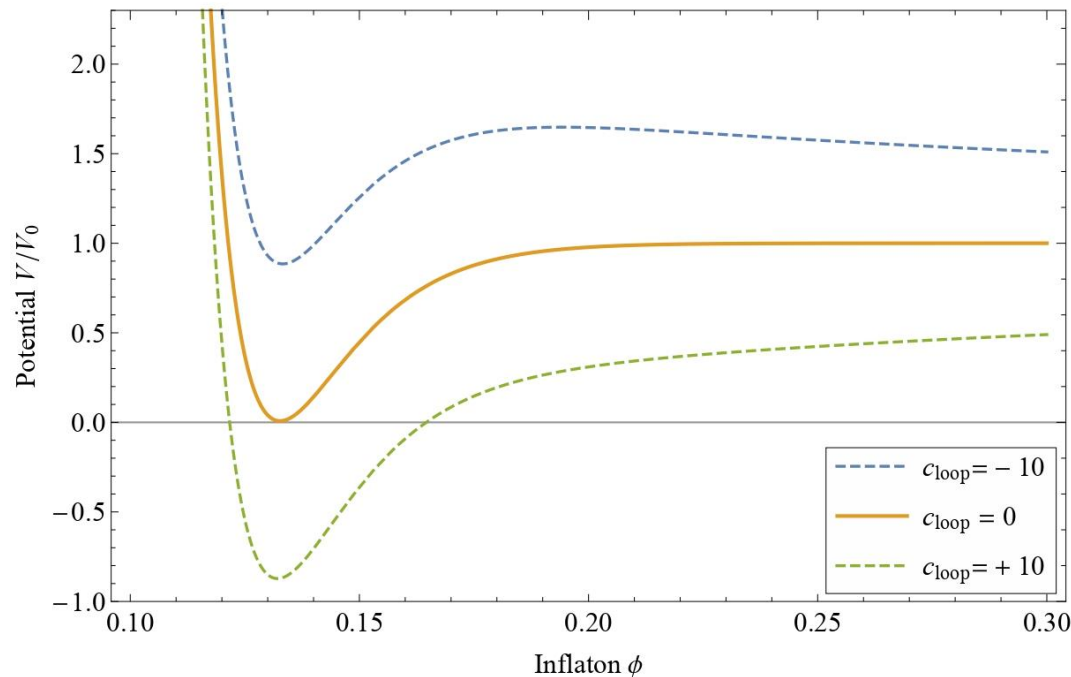
Inflaton potential

- Total potential including loops:

$$V(\tau_\phi) = C_0 \left[\frac{\beta}{\mathcal{V}^3} + C_\phi \frac{\sqrt{\tau_\phi} e^{-2a_\phi \tau_\phi}}{\mathcal{V}} - D_\phi \frac{\tau_\phi e^{-a_\phi \tau_\phi}}{\mathcal{V}^2} - \frac{c_{\text{loop}}}{\mathcal{V}^3 \sqrt{\tau_\phi}} \right]$$

$$\phi = \sqrt{\frac{4}{3\mathcal{V}}} \tau_\phi^{3/4}$$

Fixed parameters: $\mathcal{V} = 1000$, $C_\phi = D_\phi = a_\phi = \beta = 1$



- Non-perturbative blow-up inflation requires $c_{\text{loop}} \ll 10^{-6}$
- For $c_{\text{loop}} \gtrsim 10^{-6}$ potential in inflationary region is:

$$V \simeq C_0 \left(\frac{\beta}{\mathcal{V}^3} - \frac{c_{\text{loop}}}{\mathcal{V}^3 \sqrt{\tau_\phi}} \right) = V_0 \left(1 - \frac{b c_{\text{loop}}}{\mathcal{V}^{1/3} \phi^{4/3}} \right)$$

$$V_0 \equiv C_0 \frac{\beta}{\mathcal{V}^3}$$

$$b \equiv \frac{1}{\beta} \left(\frac{4}{3} \right)^{1/3}$$

Inflationary dynamics

- Slow-roll parameters:

$$\epsilon = \frac{1}{2} \left(\frac{V_\phi}{V} \right)^2 \simeq \frac{2}{9} \frac{(b c_{\text{loop}})^2}{\mathcal{V}^{2/3} \phi^{10/3}}$$

$$\eta = \frac{V_{\phi\phi}}{V} \simeq -\frac{10}{9} \frac{b c_{\text{loop}}}{\mathcal{V}^{1/3} \phi^{8/3}}$$

- Cosmological observables:

$$N_e = \int_{\phi_{\text{end}}}^{\phi_*} \frac{V}{V_\phi} d\phi \simeq \frac{9}{16} \frac{\mathcal{V}^{1/3} \phi_*^{8/3}}{b c_{\text{loop}}}$$

$$\hat{A}_s = \frac{9V_0}{4} \frac{\mathcal{V}^{2/3} \phi_*^{10/3}}{(b c_{\text{loop}})^2} \simeq 2.5 \times 10^{-7}$$

$$\phi_* = 0.06 N_e^{7/22}$$

$$\mathcal{V} = 1743 N_e^{5/11}$$

$$n_s = 1 + 2\eta - 6\epsilon \simeq 1 - \frac{20}{9} \frac{b c_{\text{loop}}}{\mathcal{V}^{1/3} \phi_*^{8/3}}$$

$$r = 16\epsilon \simeq \frac{32}{9} \frac{(b c_{\text{loop}})^2}{\mathcal{V}^{2/3} \phi_*^{10/3}}$$

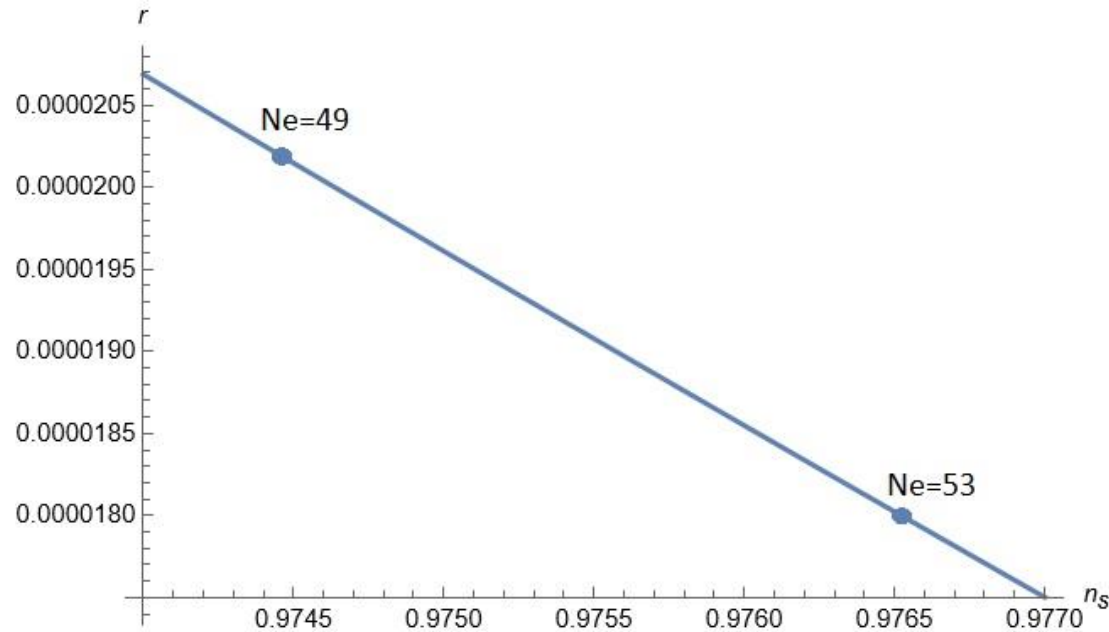
$$n_s \simeq 1 - \frac{1.25}{N_e} \quad r \simeq \frac{0.004}{N_e^{15/11}}$$



$$r \simeq 0.003(1 - n_s)^{15/11}$$

Cosmological predictions

$$r \simeq 0.003(1 - n_s)^{15/11}$$



for $49 \lesssim N_e \lesssim 53$

n_s in agreement with CMB data

$$r \simeq 2 \times 10^{-5}$$

determined by post-inflationary evolution

Control over EFT

- Values of microscopic parameters:

$$\text{for } 49 \lesssim N_e \lesssim 53 \quad \mathcal{V} = 1743 N_e^{5/11} \sim \mathcal{O}(10^4) \quad \phi_* = 0.06 N_e^{7/22} \sim \mathcal{O}(0.2)$$

- Canonical normalisation: $\phi \simeq \tau_\phi^{3/4} / \sqrt{\mathcal{V}}$

$\phi \sim \mathcal{O}(0.2)$ implies $\tau_\phi \lesssim \tau_b$ → can have inflation within Kaehler cone?

- Check in an explicit CY example from [MC,Krippendorf,Mayrhofer,Quevedo,Valandro]:

$$\mathcal{V} = \frac{1}{9} \sqrt{\frac{2}{3}} \left(\tau_b^{3/2} - \sqrt{3} \tau_s^{3/2} - \sqrt{3} \tau_\phi^{3/2} \right) \quad \tau_b = \frac{27}{2} t_b^2 \quad \tau_s = \frac{9}{2} t_s^2 \quad \tau_\phi = \frac{9}{2} t_\phi^2$$

- Kaehler cone conditions:

$$t_b + t_s > 0 \quad t_b + t_\phi > 0 \quad t_s < 0 \quad t_\phi < 0$$

- From canonical normalisation:

$$\tau_\phi = \left(\frac{\sqrt{3}}{4} \right)^{2/3} \mathcal{V}^{2/3} \phi^{4/3} \simeq \left(\frac{1}{18\sqrt{2}} \right)^{2/3} \tau_b \phi^{4/3}$$

- At horizon exit:

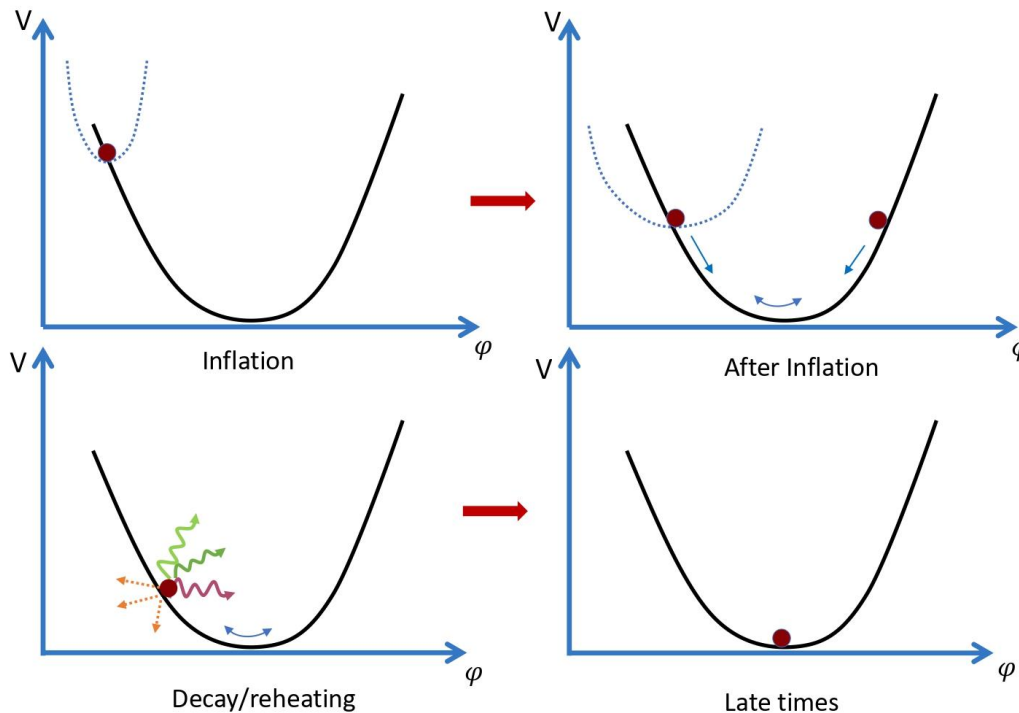
$$\frac{|t_\phi|}{t_b} = \left(\frac{1}{2\sqrt{6}} \right)^{1/3} \phi^{2/3} \simeq 0.6 \phi^{2/3} \simeq 0.2 \quad \text{for } \phi \simeq 0.2 \quad \text{well inside Kaehler cone!}$$

N_e from post-inflation

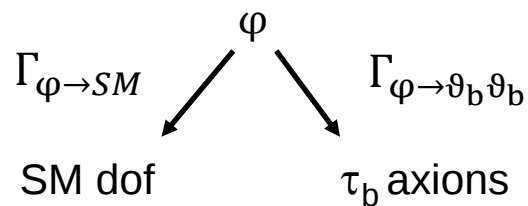
$$N_e \simeq 57 + \frac{1}{4} \ln r - \frac{1}{4} N_\phi - \frac{1}{4} N_\chi + \frac{1}{4} \ln \left(\frac{\rho_*}{\rho(t_{\text{end}})} \right)$$

τ_ϕ domin.

$\mathcal{V}$ domin.



$\phi \equiv \tau_\phi$ or $\mathcal{V}$



$\Delta N_{\text{eff}} \lesssim 0.2 - 0.5$ at 95% CL

$\longrightarrow \Delta N_{\text{eff}} \neq 0$

SM realisation

- SM D7s cannot wrap τ_s due to tension between non-pert effects and chirality [Blumenhagen, Møster, Plauschinn]
- SM D7s cannot wrap τ_ϕ since τ_ϕ -dependent FI-term would make τ_ϕ too heavy
 → need to introduce 2 additional intersecting blow-ups τ_{SM} and τ_{int}

$$\mathcal{V} = \tau_b^{3/2} - \tau_s^{3/2} - \tau_\phi^{3/2} - \tau_{SM}^{3/2} - \lambda(\tau_{int} - \tau_{SM})^{3/2}$$

- D-term stabilisation:

$$\xi_{FI} = 0 \quad \Leftrightarrow \quad \tau_{SM} = \lambda^2(\tau_{int} - \tau_{SM})$$

- i) if $\lambda = 0$, $\tau_{SM} \rightarrow 0$ → SM on D3-branes at a CY singularity
- ii) if $\lambda \neq 0$, $\xi_{FI} = 0$ fixes τ_{int} in terms of τ_{SM} and τ_{SM} remains as a flat direction fixed by loops

$$V(\tau_{SM}) = \left(\frac{d_{loop}}{\sqrt{\tau_{SM}}} - \frac{g_{loop}}{\sqrt{\tau_{SM}} - \sqrt{\tau_s}} \right) \frac{W_0^2}{\mathcal{V}^3} \quad [MC, Mayrhofer, Valandro]$$

$$\rightarrow \tau_s = \left(1 + \sqrt{\frac{g_{loop}}{d_{loop}}} \right)^2 \tau_{SM} \sim \tau_{SM} \sim \mathcal{O}(10) \simeq g_{SM}^{-2}$$

→ SM on D7-branes wrapped around τ_{SM}

Volume decay rates

- Masses of canonically normalised moduli: τ_ϕ becomes ϕ and $\mathcal{V}$ becomes χ

$$m_\phi \simeq \frac{W_0 \ln \mathcal{V}}{\mathcal{V}} M_p \quad \text{and} \quad m_\chi \simeq \frac{W_0}{\mathcal{V}^{3/2} \sqrt{\ln \mathcal{V}}} M_p$$

- Volume χ :

- i) decay into closed string axions ϑ_b $\Gamma_{\chi \rightarrow \vartheta_b \vartheta_b} = \frac{1}{48\pi} \frac{m_\chi^3}{M_p^2}$
- ii) decay into MSSM Higgses H_u and H_d $\Gamma_{\chi \rightarrow H_u H_d} = \frac{Z^2}{24\pi} \frac{m_\chi^3}{M_p^2} = 2Z^2 \Gamma_{\chi \rightarrow \vartheta_b \vartheta_b}$
- iii) decay into SM Higgses h $\Gamma_{\chi \rightarrow hh} = \frac{c_{\text{loop}}^2}{32\pi} \left(\frac{m_0}{m_\chi} \right)^4 \frac{m_\chi^3}{M_p^2}$

$$\longrightarrow \frac{\Gamma_{\chi \rightarrow hh}}{\Gamma_{\chi \rightarrow \vartheta_b \vartheta_b}} \simeq c_{\text{loop}}^2 \left(\frac{m_0}{m_\chi} \right)^4$$

SM on D7s: $m_0 \simeq \frac{M_p}{\mathcal{V}} \gg m_\chi$ $\frac{\Gamma_{\chi \rightarrow hh}}{\Gamma_{\chi \rightarrow \vartheta_b \vartheta_b}} \simeq (c_{\text{loop}} \mathcal{V})^2 \gg 1$

$\longrightarrow$ χ decays into SM Higgses h

SM on D3s: $m_0 \lesssim m_\chi$ $\frac{\Gamma_{\chi \rightarrow hh}}{\Gamma_{\chi \rightarrow \vartheta_b \vartheta_b}} \lesssim c_{\text{loop}}^2 \ll 1$

$\longrightarrow$ χ decays into ϑ_b axions, H_u and H_d

Inflaton decay rates

- Inflaton wrapped by **hidden D7s**:

decay into hidden gauge bosons γ_h

$$\Gamma_{\phi \rightarrow \gamma_h \gamma_h} \simeq \frac{\mathcal{V}}{64\pi} \frac{m_\phi^3}{M_p^2}$$

- Inflaton **not** wrapped by any D7:

i) decay into volume moduli χ and $\mathfrak{g}_b$ axions

$$\Gamma_{\phi \rightarrow \chi\chi} \simeq \Gamma_{\phi \rightarrow \vartheta_b \vartheta_b} \simeq \frac{(\ln \mathcal{V})^{3/2}}{64\pi \mathcal{V}} \frac{m_\phi^3}{M_p^2}$$

SM on **D7s**: χ then decays instantaneously into $h h$

SM on **D3s**: χ then decays later on into H_u and H_d , and $\mathfrak{g}_b \mathfrak{g}_b$

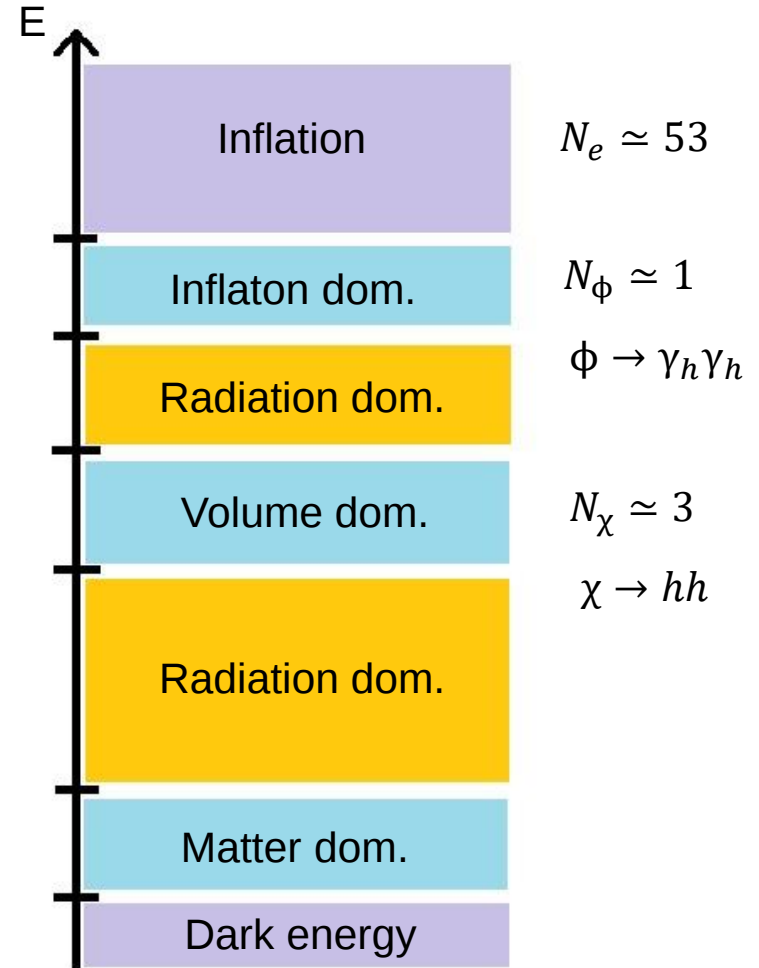
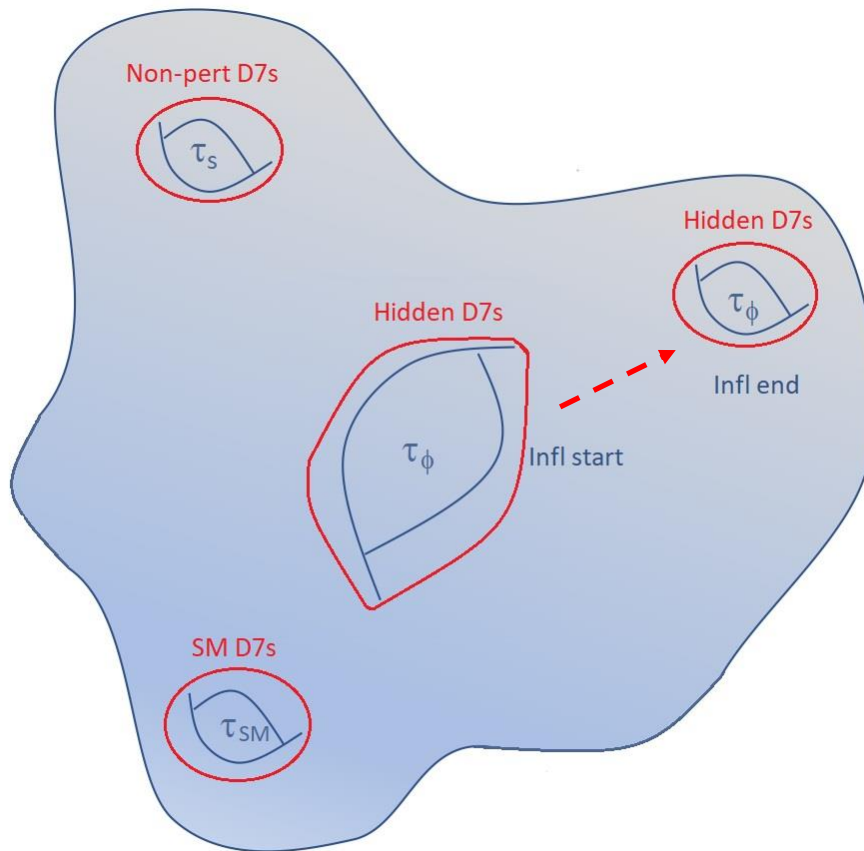
- ii) for SM on **D7s**, extra decays into SM gauge bosons γ , τ_{SM} moduli and $\mathfrak{g}_{SM}$ (QCD) axions

$$\Gamma_{\phi \rightarrow \tau_{SM} \tau_{SM}} \simeq \Gamma_{\phi \rightarrow \vartheta_{SM} \vartheta_{SM}} \simeq \Gamma_{\phi \rightarrow \chi\chi} \qquad \Gamma_{\phi \rightarrow \gamma\gamma} \simeq N_g \Gamma_{\phi \rightarrow \chi\chi} \simeq 12 \Gamma_{\phi \rightarrow \chi\chi}$$

τ_{SM} then decays instantaneously into $\gamma \gamma$, and $\mathfrak{g}_{SM} \mathfrak{g}_{SM}$ with [MC, Hebecker, Jaeckel, Wittner]

$$\frac{\Gamma_{\tau_{SM} \rightarrow \gamma\gamma}}{\Gamma_{\tau_{SM} \rightarrow \vartheta_{SM} \vartheta_{SM}}} = 8 N_g \geq 96 \gg 1$$

SM on D7s and inflaton wrapped by D7s



Predictions:

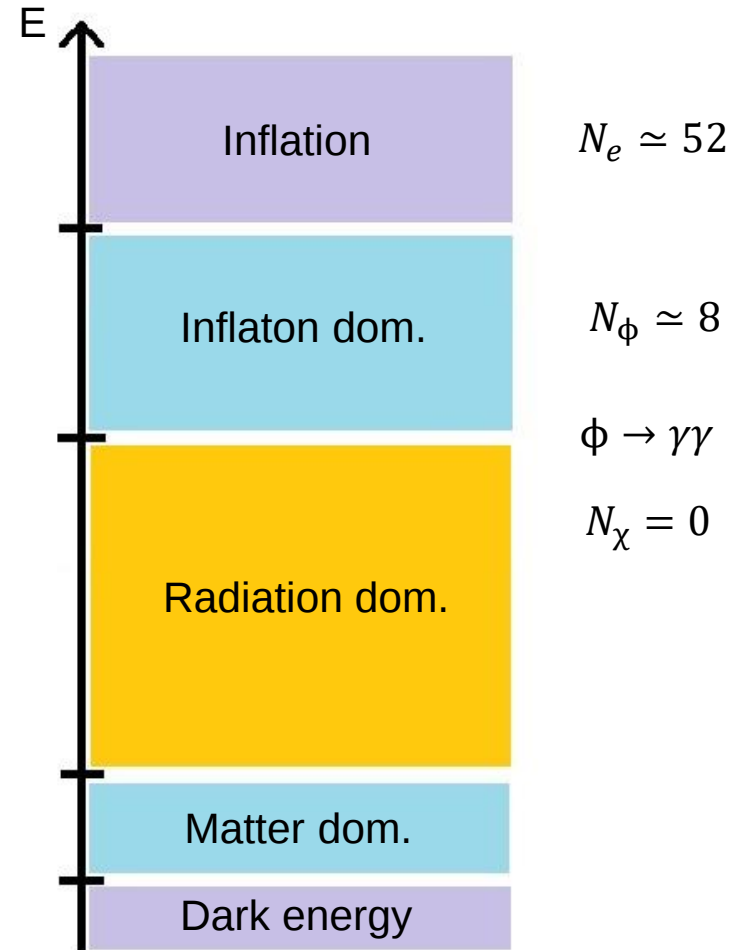
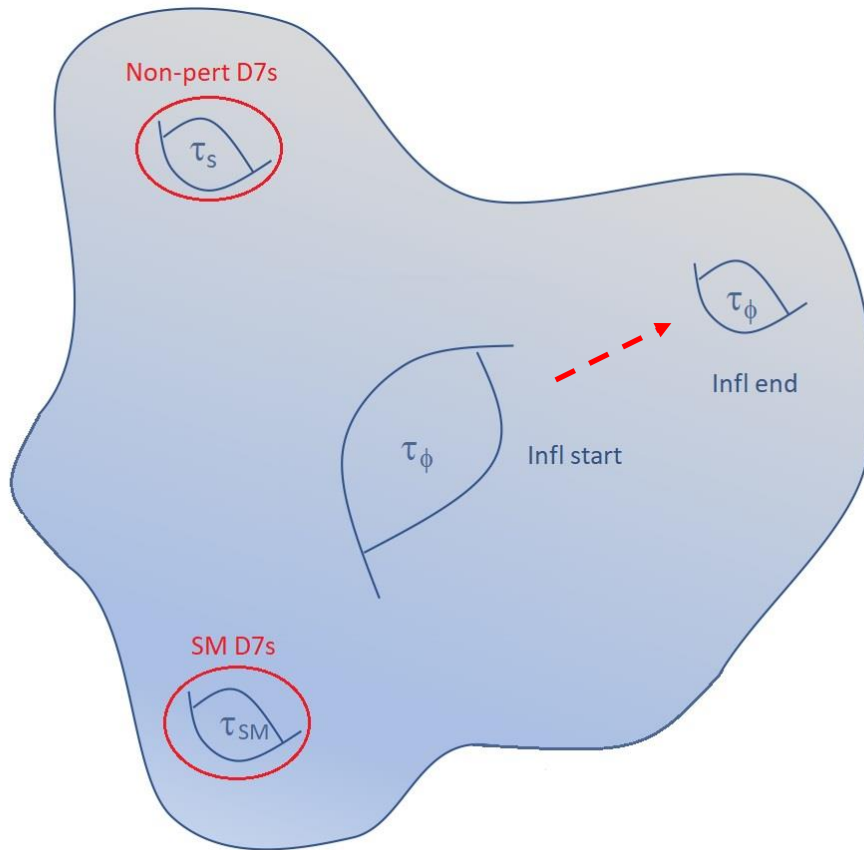
$$n_s \simeq 0.9765$$

$$r \simeq 1.7 \times 10^{-5}$$

$$T_{\text{rh}} \simeq 4 \times 10^{10} \text{ GeV}$$

$$\Delta N_{\text{eff}} \simeq 0$$

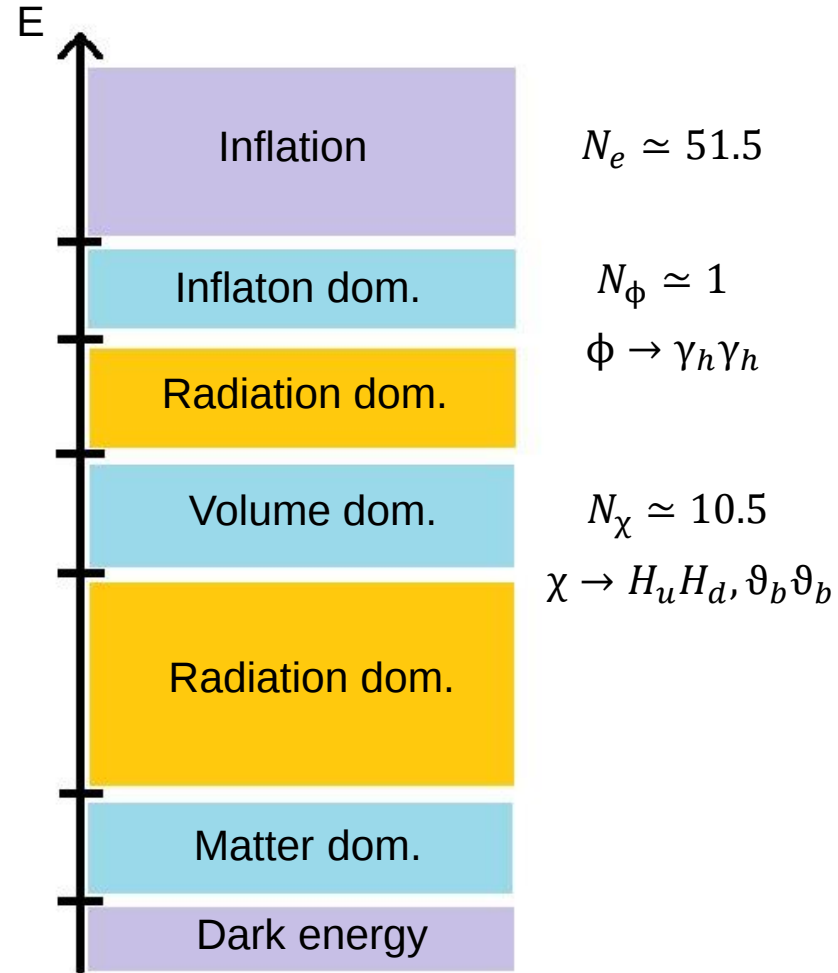
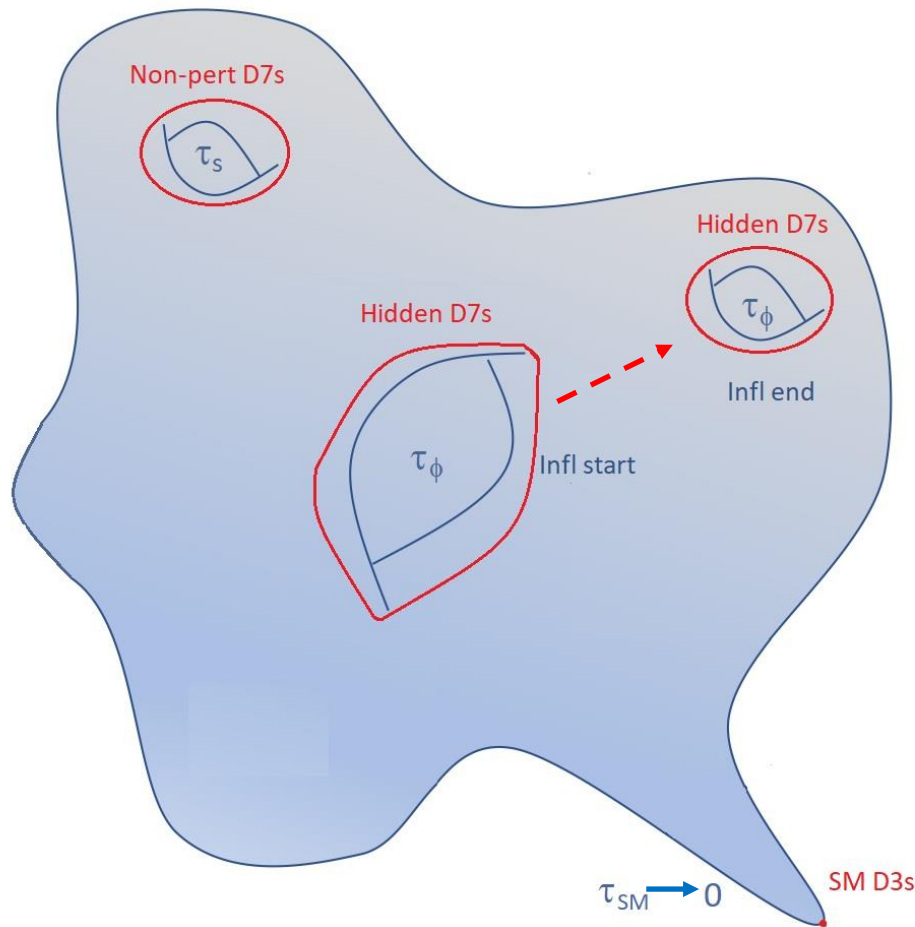
SM on D7s and unwrapped inflaton



Predictions:

$$n_s \simeq 0.9761 \quad r \simeq 1.7 \times 10^{-5} \quad T_{\text{rh}} \simeq 3 \times 10^{12} \text{ GeV} \quad \Delta N_{\text{eff}} \simeq 0.14$$

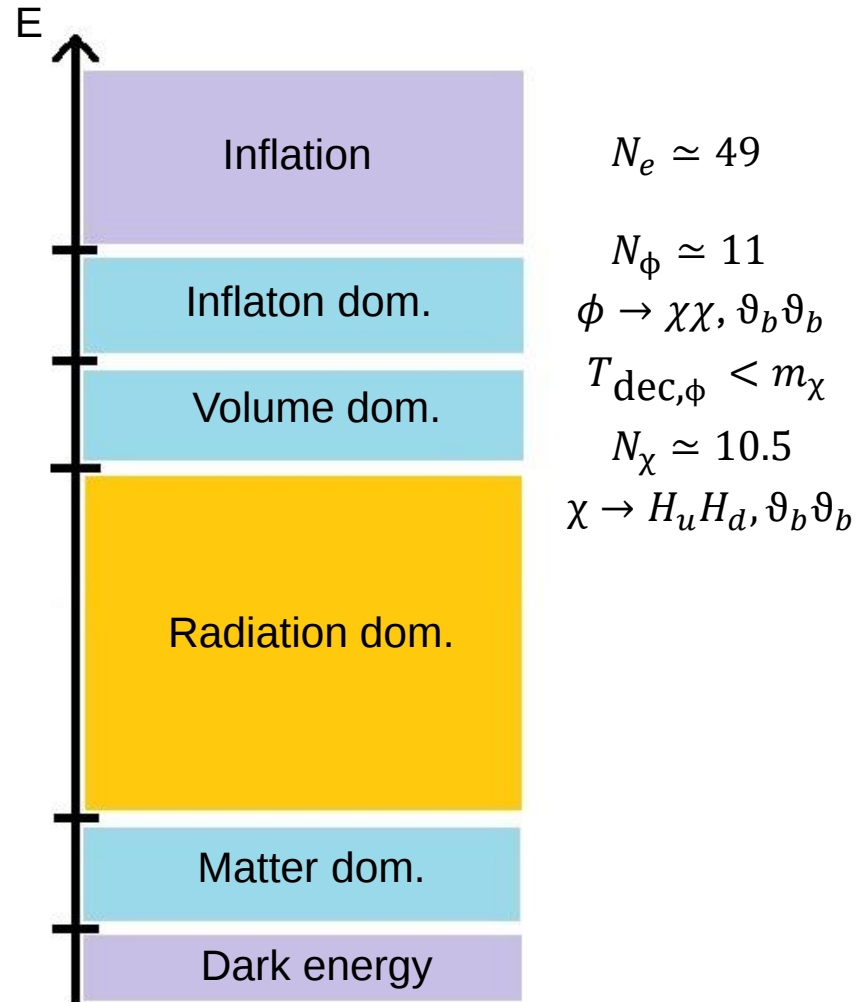
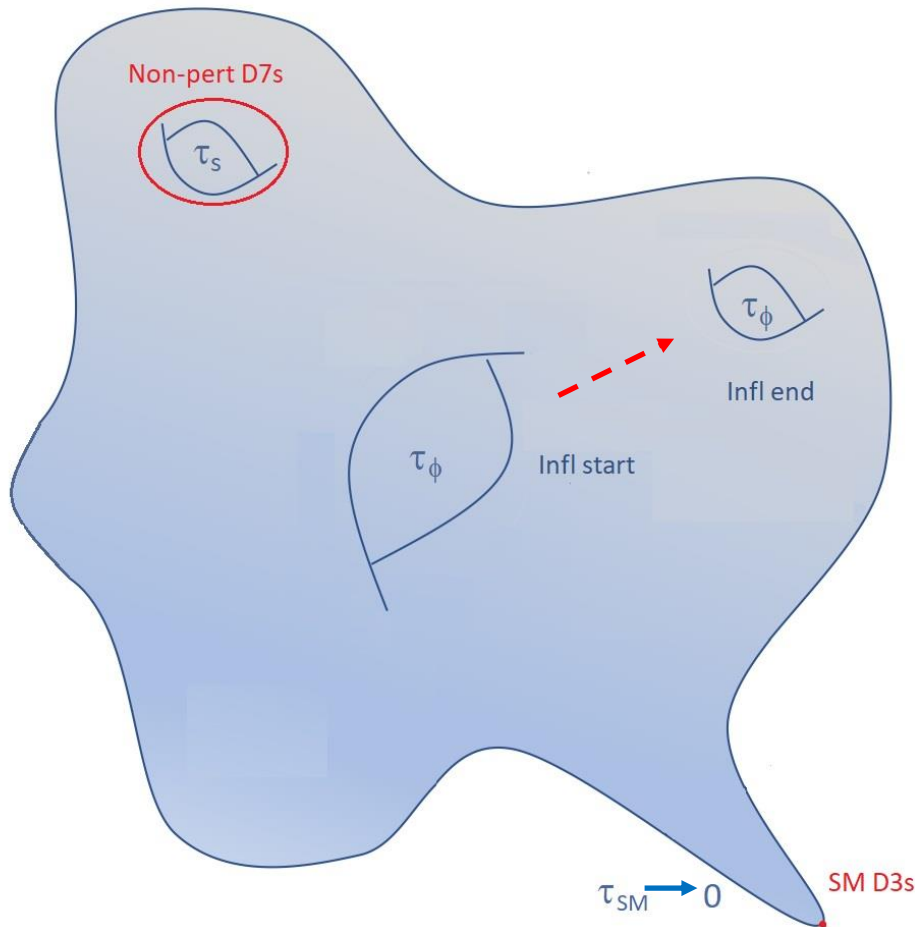
SM on D3s and inflaton wrapped by D7s



Predictions:

$$n_s \simeq 0.9757 \quad r \simeq 1.8 \times 10^{-5} \quad T_{\text{rh}} \simeq 1 \times 10^8 \text{ GeV} \quad \Delta N_{\text{eff}} \simeq \frac{1.43}{Z^2} \simeq 0.36 \quad Z = 2$$

SM on D3s and unwrapped inflaton



Predictions:

$$n_s \simeq 0.9744 \quad r \simeq 1.9 \times 10^{-5} \quad T_{\text{rh}} \simeq 2 \times 10^8 \text{ GeV} \quad \Delta N_{\text{eff}} \simeq \frac{1.43}{Z^2} \simeq 0.36 \quad Z = 2$$

Summary

- Type IIB Kaehler moduli $\perp \mathcal{V}$ are good inflatons ϕ due to **approximate shift symmetries**
- $V(\phi)$ determined by nature of **breaking effects** (pert/non-pert.) and **topology** (bulk/local cycle)
 - can have several scenarios
- New model: **Loop Blow-up Inflation**
- Inflation driven by a **blow-up mode** with $V(\phi)$ generated by **1-loop corrections to K**
- **1-loop K**: conjecture from toroidal computation
+ field theory matching with **1-loop 2-point function** and **Coleman-Weinberg potential**
- Inflaton potential:
$$V(\phi) = V_0 \left(1 - \frac{c}{\mathcal{V}^{1/3} \phi^{2/3}} \right)$$
- EFT under control with inflation inside Kaehler cone
- Microscopic parameters: $\mathcal{V} \sim \mathcal{O}(10^4)$ and $\phi_* \sim \mathcal{O}(0.2)$
- Predictions: $0.9744 \lesssim n_s \lesssim 0.9765$ and $r \simeq 2 \times 10^{-5}$
- Post-inflation with **moduli domination** and reheating from moduli decay
- Depending on SM realisation: $49 \lesssim N_e \lesssim 53$ and $0 \lesssim \Delta N_{\text{eff}} \lesssim 0.36$