

MODULI

FIXING

IN

REALISTIC

STRING

VACUA

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ELEMENTS OF STRING UNIFICATION

Classically : $g^{\alpha\beta} \longrightarrow \eta^{\alpha\beta}$

Quantum : $D=26$ (bosonic)
 $D=10$ (fermionic)

Heterotic string $\rightarrow D_L = 10 \quad D_R = 10$

Real World $D = 4$

Bosonic $\rightarrow 4_{L+R} + 22_{L+R}$

Superstring $\rightarrow 4_{L+R} + 6_{L+R}$

Heterotic-string $\rightarrow 4_{L+R} + (6_L + 6_R) + 16_R$

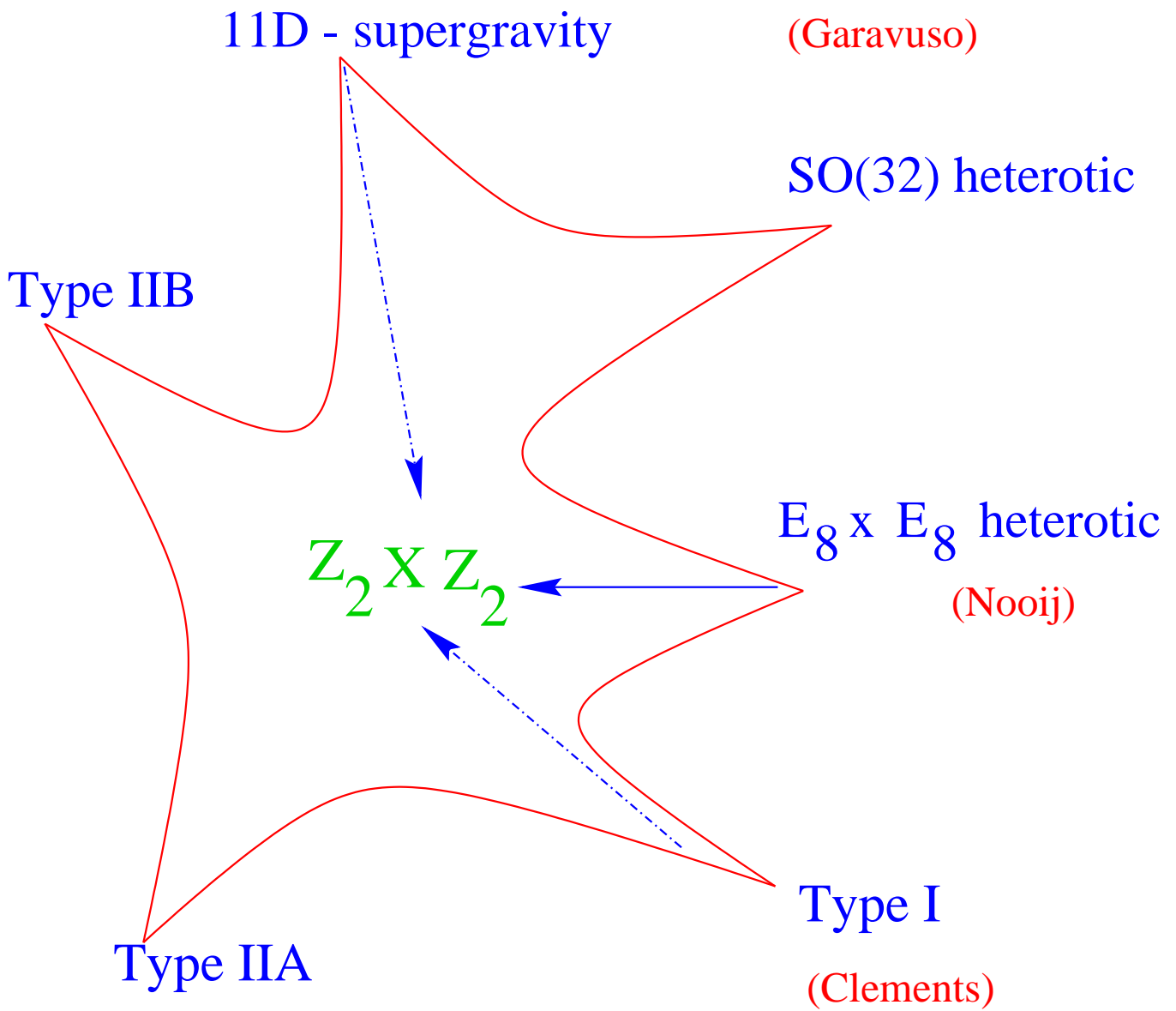
$\underbrace{\hspace{10em}}$
 6D internal
 manifold

\downarrow
 16D lattice
 $R = \sqrt{2}$

moduli \rightarrow size & shape of internal 6D manifold.
 Twisted moduli

no known mechanism selects and fixes these moduli

realistic string vacua $\langle - \rangle$ phenomenological guide?



DATA \rightarrow STANDARD MODEL

$$\text{SU}(3) \times \text{SU}(2) \times \text{U}(1)_Y \rightarrow \text{SU}(5) \rightarrow \text{SO}(10)$$

$$\left[\begin{pmatrix} e \\ \end{pmatrix} + D_L^c \right] + \left[U_L^c + \begin{pmatrix} u \\ d \end{pmatrix} + E_L^c \right] + N_L^c$$
$$\bar{5} \quad + \quad 10 \quad + \quad 1 \quad \quad \quad \frac{\quad}{16}$$

STANDARD MODEL \rightarrow UNIFICATION

ADDITIONAL EVIDENCE:

Logarithmic running, proton longevity, neutrino masses

PRIMARY GUIDES:

3 generations

SO(10) embedding

REALISTIC STRING MODELS :

heterotic 10D \rightarrow heterotic 4D

6D compactifications $(T^2 \times T^2 \times T^2)$

Z_3 Orbifold $\rightarrow U(1)_Y \notin SO(10)$

$Z_2 \times Z_2$ Orbifold $\rightarrow U(1)_Y \in SO(10)$

$$\Rightarrow \sin^2 \Theta_w = 3/8 \quad \text{at } M_{\text{string}}$$

low energy data distinguishes between
classes of string compactifications !!!

$Z_2 \times Z_2$ orbifold based models - Gross Structure

Untwisted sector

$$SO(10) \longrightarrow SU(3) \times SU(2) \times U(1)_{T_3R} \times U(1)_{B-L}$$

Three twisted sectors $\implies 1 + 1 + 1$

$$16 + 16 + 16$$

decomposed under $(3, 2, 1, 1)$

⊕ Hidden sector : $E_8 \rightarrow$ subgroup + matter

⊕ Exotics \rightarrow decouple from the low energy spectrum

primarily studied in the free fermionic formulation

Free Fermionic Model Building

Models \longrightarrow set of boundary condition basis vectors

The NAHE set $\{1, S, b_1, b_2, b_3\}$

$\longrightarrow Z_2 \times Z_2$ orbifold compactification

Gauge Group : $SO(10) \times SO(6)^{1,2,3} \times E_8$

beyond the NAHE set Add $\{\alpha, \beta, \gamma\}$

number of generations is reduced to three

$$SO(10) \longrightarrow SU(3) \times SU(2) \times U(1)_{T_{3R}} \times U(1)_{B-L}$$

$$U(1)_Y = \frac{1}{2}(B - L) + T_{3R} \in SO(10) !$$

$$SO(6)^{1,2,3} \longrightarrow U(1)^{1,2,3} \times U(1)^{1,2,3}$$

Realistic free fermionic models

Phenomenology of the Standard Model and string unification

1. Top quark mass $\sim 175 - 180$ GeV PLB 274 (1992) 47
2. Generation mass hierarchy NPB 407 (1993) 57
3. CKM mixing NPB 416 (1994) 63
with Edi Halyo
4. Stringy see-saw mechanism PLB 307 (1993) 311
with Edi Halyo
5. Gauge coupling unification NPB 457 (1995) 409
with Keith Dienes
6. Proton stability NPB 428 (1994) 111
7. Squark degeneracy NPB 526 (1998) 21
with jogesh Pati
8. Minimal Superstring Standard Model PLB 455 (1999) 135
with Cleaver & Nanopoulos

$$\text{NAHE} \oplus (\xi_2 = \{\bar{\psi}_{1,\dots,5}, \bar{\eta}^1, \bar{\eta}^2, \bar{\eta}^3\} = 1) \rightarrow \{1, S, \xi_1, \xi_2, b_1, b_2\}$$

Gauge group: $SO(4)^3 \times E_6 \times U(1)^2 \times E_8$ and 24 generations.

toroidal compactification $(6_L + 6_R)$ g_{ij}, b_{ij}

$$g_{ij} = \begin{pmatrix} 2 & -1 & 0 & 0 & 0 & 0 \\ -1 & 2 & -1 & 0 & 0 & 0 \\ 0 & -1 & 2 & -1 & 0 & 0 \\ 0 & 0 & -1 & 2 & -1 & -1 \\ 0 & 0 & 0 & -1 & 2 & 0 \\ 0 & 0 & 0 & -1 & 0 & 2 \end{pmatrix} \quad b_{ij} = \begin{cases} g_{ij} & i > j \\ 0 & i = j \\ -g_{ij} & i < j \end{cases}$$

$R_i \rightarrow$ the free fermionic point \rightarrow G.G. $SO(12) \times E_8 \times E_8$

mod out by a $Z_2 \times Z_2$ with standard embedding

\Rightarrow $SO(4)^3 \times E_6 \times U(1)^2 \times E_8$ with 24 generations

Exact correspondence

In the realistic free fermionic models

replace $X = \{\bar{\psi}_{1,\dots,5}, \bar{\eta}^1, \bar{\eta}^2, \bar{\eta}^3\} = 1$
with $2\gamma = \{\bar{\psi}_{1,\dots,5}, \bar{\eta}^1, \bar{\eta}^2, \bar{\eta}^3, \bar{\phi}_{1,\dots,4}\} = 1$

Then

$$\{\vec{1}, \vec{S}, \vec{\xi}_1 = \vec{1} + \vec{b}_1 + \vec{b}_2 + \vec{b}_3, 2\gamma\} \rightarrow \text{N=4 SUSY and } SO(12) \times SO(16) \times SO(16)$$

apply $b_1 \times b_2 \rightarrow Z_2 \times Z_2 \rightarrow$

$$\text{N=1 SUSY and } SO(4)^3 \times SO(10) \times U(1)^3 \times SO(16)$$

$$\begin{aligned} b_1, \quad b_2, \quad b_3 &\Rightarrow (3 \times 8) \cdot 16 \text{ of } SO(10)_O \\ b_1 + 2\gamma, \quad b_2 + 2\gamma, \quad b_3 + 2\gamma &\Rightarrow (3 \times 8) \cdot 16 \text{ of } SO(16)_H \end{aligned}$$

This will be important for the twisted moduli.

Moduli?

Untwisted moduli – > shape & size of the internal dimensions

Twisted moduli – > arise from the twisted sectors

models

$$\frac{T^6}{Z_2 \times Z_2}$$

$$T^6 : \quad G_{IJ} \quad ; \quad B_{IJ} \quad I, J = 1, \dots, 6 .$$

untwisted moduli: coefficients of exactly marginal operators

moduli fields: massless chiral superfields with flat scalar potential
to all orders in string perturbation theory

VEVs are unconstrained – > parametrize connected vacua

Narain construction : Scalar couplings of $N = 4$ SUGRA

$$\frac{SO(6,6)}{SO(6) \times SO(6)} \quad \times \quad \frac{SU(1,1)}{U(1)}$$

internal manifold dilaton

Up to orbifold projections

$$\frac{T^6}{Z_2 \times Z_2} \implies \frac{SO(6,6)}{SO(6) \times SO(6)} \longrightarrow \left(\frac{SO(2,2)}{SO(2) \times SO(2)} \right)^3$$

\implies 3 complex structures + 3 Kähler moduli

In all symmetric $Z_2 \times Z_2$ orbifolds

We would like to identify these moduli in the fermionic formalism

In symmetric orbifolds:

$$\text{EMO} \rightarrow \partial X^I \bar{\partial} X^J$$

$$X^I \quad I = 1, \dots, 6 \quad \rightarrow \quad T^6$$

$$S = \frac{1}{8\pi} \int d^2\sigma \quad (G_{IJ} \partial X^I \bar{\partial} X^J + B_{IJ} \partial X^I \bar{\partial} X^J)$$

In FFF $\partial X_L^I \rightarrow y^I \omega^I$

$i\partial X_L^I \rightarrow U(1)$ current in the Cartan subalgebra

In the fermionic language

$$i\partial X_L^I \rightarrow J_L^I = y^I \omega^I$$

$$\Rightarrow \partial X^I \bar{\partial} X^J \rightarrow J_L^I(z) \bar{J}_R^J(\bar{z})$$

→ WS Thirring interactions $(R - \frac{1}{R})J_L(z)\bar{J}(\bar{z})$

Thirring interactions vanish at free fermionic point with $R = \frac{1}{R}$

To identify the untwisted moduli in the free fermionic models

→ find the operators of the form

$$J_L^I(z)\bar{J}_R^J(\bar{z})$$

that are allowed by the orbifold (fermionic) symmetry group

Free Fermionic Construction

$$C_L = D \cdot 1 + D \cdot \frac{1}{2} + \frac{1}{2}N_{f_\ell} - 26 + 11 = 0$$

$$C_R = D \cdot 1 + \frac{1}{2}N_{f_r} - 26 = 0$$

$$D = 4 \rightarrow n_L^f = 18, \quad n_R^f = 44$$

free fermion world-sheet content in LCG

$$\text{L : } \psi_{1,2}^\mu \quad \chi_i \quad y^i \quad \omega^i \quad i = 1, \dots, 6$$

$$\text{R : } \bar{y}^i \quad \bar{\omega}^i \quad \bar{\psi}^{1\dots 5} \bar{\eta}^1 \bar{\eta}^2 \bar{\eta}^3 \bar{\phi}^{1\dots 8}$$

$$T_F(z) = \psi^\mu \partial X_\mu + \sum \chi^j y^j \omega^j$$

$$f \rightarrow -e^{i\pi\alpha(f)} f \quad \alpha(f) = (-1, +1]$$

$$\vec{b} = (b_1^L, \dots, b_{20}^L \mid b_{21}^R, \dots, b_{64}^R)$$

orbifold twists; Wilson lines \rightarrow parallel transport phases

$$B = \{ \vec{b}_1, \dots, \vec{b}_n \}$$

1-loop partition function

$$Z = \sum_{\substack{\text{all spin} \\ \text{structures}}} c \begin{pmatrix} \vec{\alpha}_i \\ \vec{\alpha}_j \end{pmatrix} \mathcal{Z} \begin{pmatrix} \vec{\alpha}_i \\ \vec{\alpha}_j \end{pmatrix}$$

$$\vec{\alpha}_i = m_1^i \vec{b}_1 + \cdots + m_n^i \vec{b}_n$$

Models \rightarrow specified by a consistent \mathbf{B} and $c \begin{pmatrix} b_i \\ b_j \end{pmatrix}$

Construction of the physical states \rightarrow GSO projection

$$e^{i\pi(\vec{b}_i \cdot \vec{F}_\alpha)} |s\rangle_{\vec{\alpha}} = \delta_\alpha c^* \begin{pmatrix} \vec{\alpha} \\ \vec{b}_i \end{pmatrix} |s\rangle_{\vec{\alpha}}$$

$$\begin{pmatrix} NS \\ \vec{b}_i \end{pmatrix} = \delta_{b_i} = e^{i\pi b_i(\psi^\mu)}$$

Each complex fermion : \rightarrow $U(1)$ current ff^*

$$Q(f) = \frac{1}{2}\alpha(f) + F(f)$$

Bosonization

$$\xi_i = \sqrt{\frac{1}{2}}(y_i + i\omega_i) = e^{iX_i}, \eta_i = \sqrt{\frac{i}{2}}(y_i - i\omega_i) = ie^{-iX_i}$$

similarly for the right-movers

Boundary conditions translate to twists and shifts

$$X^I(z, \bar{z}) = X_L^I(z) + X_R^I(\bar{z})$$

Complex internal coordinates

$$Z_k^\pm = (X^{2k-1} \pm iX^{2k}), \quad \psi_k^\pm = (\chi^{2k-1} \pm i\chi^{2k}) \quad (k = 1, 2, 3)$$

Untwisted moduli

$$S = \int d^2 z h_{ij}(X) J_L^i(z) \bar{J}_R^j(\bar{z})$$

J_L^i $i = 1, \dots, 6$ are chiral currents of $U(1)_L^6$

J_R^i $i = 1, \dots, 22$ are chiral currents of $U(1)_R^{22}$

$h_{ij} \rightarrow$ four dimensional scalar fields that are identified with the scalar components of untwisted moduli

$$J_L^i \sim y^i \omega^i \quad i = 1, \dots, 6$$

$$J_R^j \sim \bar{\phi}^a \bar{\phi}^{*a} \quad a = 1, \dots, 22$$

some of these operators are projected out in concrete models that are specified by the basis vectors

The basis vectors determine how the WS fermions transform under parallel transport

\Rightarrow some of the EMO may not be invariant

Models

$$\{1, S\} \quad \vec{1} = (\vec{1}_L; \vec{1}_R)$$

$$\vec{S} = (\psi_{1,2}^\mu, \chi_{1,\dots,6} : \vec{0}_R) \equiv 1$$

$$N = 4$$

$$SO(44)$$

$$\frac{SO(6, 22)}{SO(6) \times SO(22)}$$

Moduli space

$$\chi^i \otimes \bar{\phi}^a \bar{\phi}^{*a} |0\rangle$$

moduli fields

$$6 \times 22$$

scalar fields

$$Z_2 \times Z_2 \quad \{ 1 , S , \xi_1 , \xi_2 \} + \{ b_1 , b_2 \}$$

$$SO(12) \times E_8 \times E_8 \quad Z_2 \times Z_2$$

$$\rightarrow SO(4)^3 \times E_6 \times U(1)^2 \times E_8$$

The Thirring interactions that remain invariant are

$$J_L^{1,2} \bar{J}_R^{1,2} \quad ; \quad J_L^{3,4} \bar{J}_R^{3,4} \quad ; \quad J_L^{5,6} \bar{J}_R^{5,6}$$

$$y^{1,2} \omega^{1,2} \bar{y}^{1,2} \bar{\omega}^{1,2} \quad ; \quad y^{3,4} \omega^{3,4} \bar{y}^{3,4} \bar{\omega}^{3,4} \quad ; \quad y^{5,6} \omega^{5,6} \bar{y}^{5,6} \bar{\omega}^{5,6}$$

These moduli are always present in symmetric $Z_2 \times Z_2$ orbifolds