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## Quantum Fields in Curved Spacetime

### Examples X

To hand in Wednesday 7th January in the lecture

#### 1. Surface Gravity

Calculate the acceleration  $a_\mu = U^\rho \nabla_\rho U_\mu$  of a static observer near the horizon of the Schwarzschild black hole, where  $U^\mu$  is the four-velocity. What is the magnitude of the acceleration  $a = \sqrt{a_\mu a^\mu}$ ?

Show that for a Schwarzschild black hole the surface gravity  $\kappa = (4GM)^{-1}$  is the magnitude of acceleration of a static test particle near the horizon, as measured by a static observer at infinity.

(5 pts)

#### 2. Conformal Diagram

Draw a conformal diagram of 1 + 1 dimensional Minkowski spacetime. In particular explain the different kinds of infinities occurring in the conformal diagram. How does the conformal diagram of 3 + 1 dimensional Minkowski spacetime look like?

(5 pts)