

# Introduction to Gauge/Gravity Duality

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# 1 Introduction

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### 2.3 Conformal symmetry

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### 3.3 Superstring Theory: Type IIB string theory and supergravity

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