

Why the GSI anomaly cannot be explained by Quantum Beats

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Heidelberg

- AM: *Why a splitting in the final state cannot explain the GSI-Oscillations*, to appear soon
- H. Kienert, J. Kopp, M. Lindner, AM: *The GSI anomaly*, J. Phys. Conf. Ser. **136**, 022049, 2008, arXiv:0808.2389

SFB Tr 27 Meeting, Project C1, Heidelberg, 2009

Outline

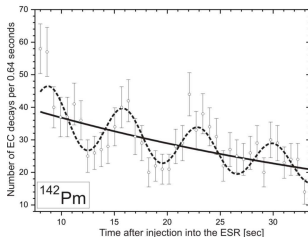
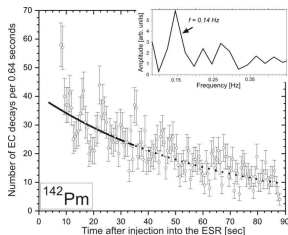
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- 2 Quantum Beats
- 3 One atom of type I
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- observation: cos-modulation superimposed on the exponential decay law
- oscillation frequency $\sim 7 \text{ sec} \Rightarrow \sim 10^{-15} \text{ eV!!!}$
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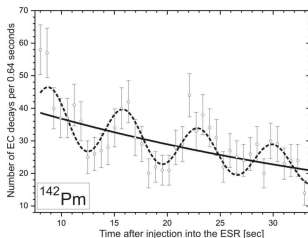
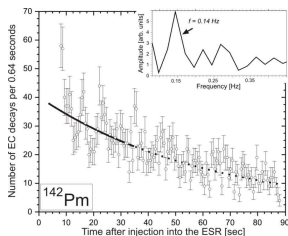
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Y. A. Litvinov et al.,
Phys. Lett. **B664**,
162 (2008),
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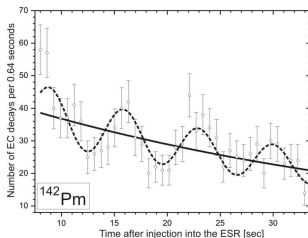
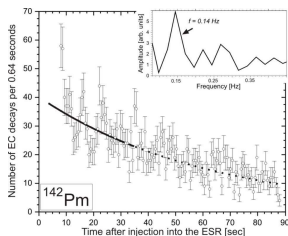
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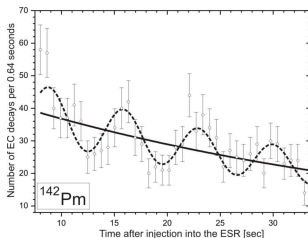
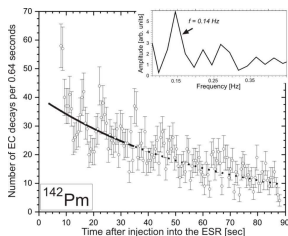
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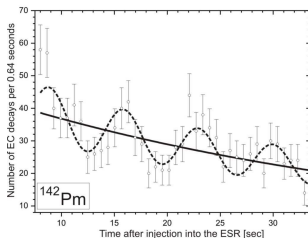
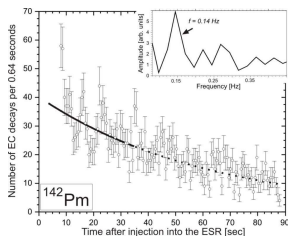
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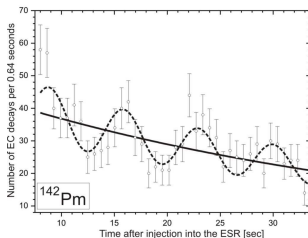
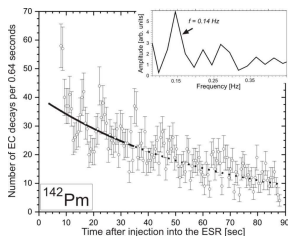
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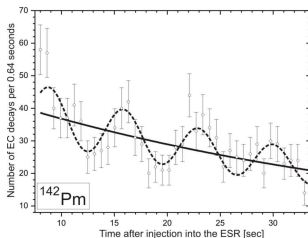
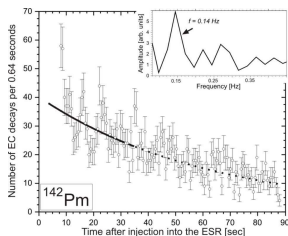
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Type II

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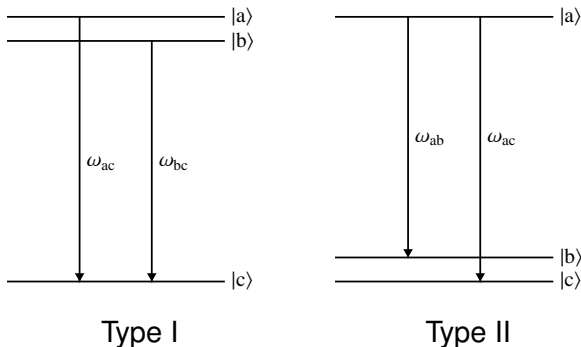


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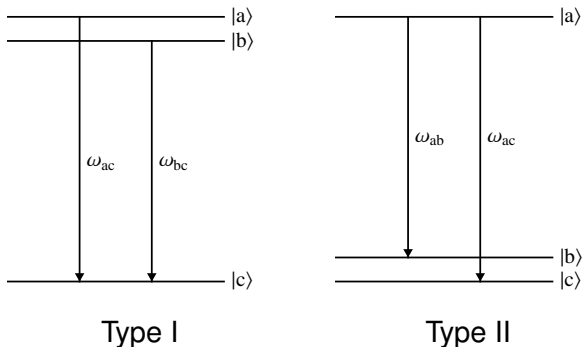
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- important: the states $|a\rangle$, $|b\rangle$, and $|c\rangle$ correspond to different energy eigenvalues
 - ⇒ They are orthogonal!
- this orthogonality is not touched by the uncertainty relation
- BUT: an uncertainty allows for a coherent superposition

Quantum Beats (Chow et al., Phys. Rev. A, **11**, 1380)



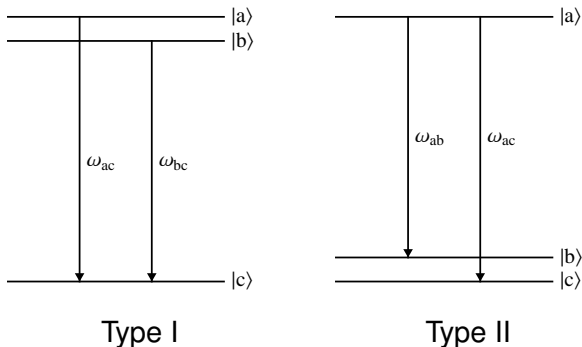
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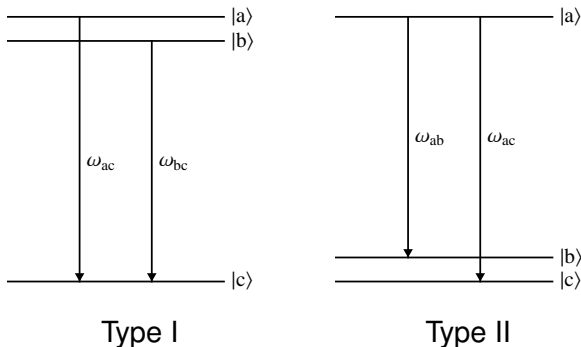
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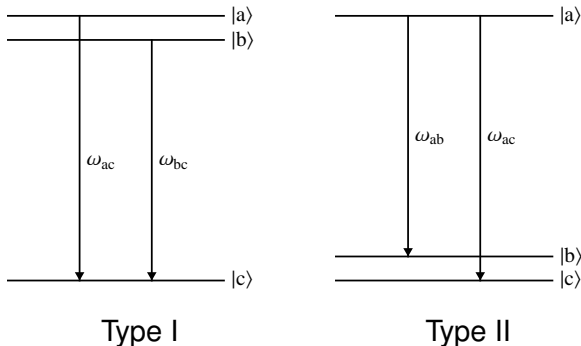
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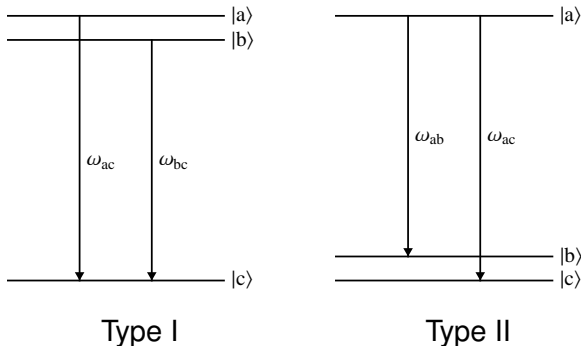
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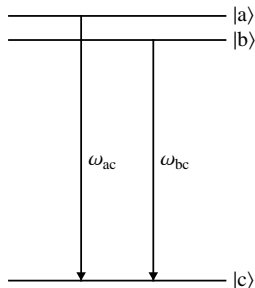
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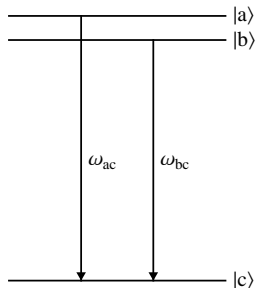
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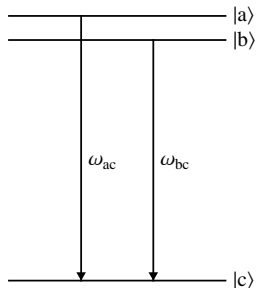
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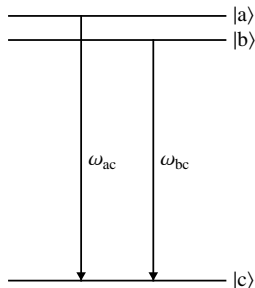
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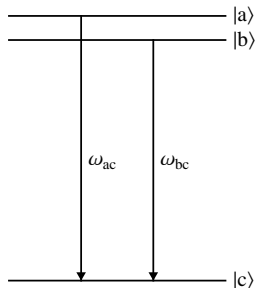
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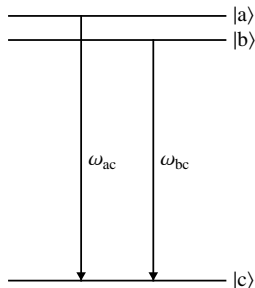
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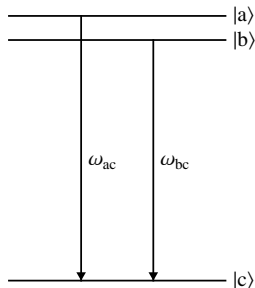
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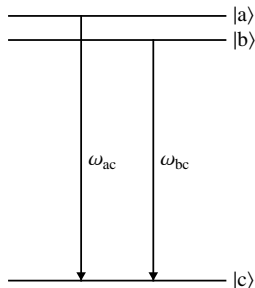
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- electric field operator: $\vec{E}(\vec{x}, t) = \sum_{\vec{k}, \lambda} \epsilon_{\vec{k}, \lambda} \left(a_{\vec{k}, \lambda} e^{-ikx} + a_{\vec{k}, \lambda}^\dagger e^{+ikx} \right)$
- radiated photon intensity:

$$I \propto \langle \Psi(t) | \vec{E}^2(\vec{0}, t) | \Psi(t) \rangle$$

- effectively:

$$\begin{aligned} \vec{E}^2(\vec{0}, t) = & \epsilon_{ac}^2 (1 + 2a_{ac}^\dagger a_{ac}) + \epsilon_{bc}^2 (1 + 2a_{bc}^\dagger a_{bc}) + \\ & + 2\epsilon_{ac}\epsilon_{bc} (a_{ac}^\dagger a_{bc} e^{i\Delta t} + a_{bc}^\dagger a_{ac} e^{-i\Delta t}) \end{aligned}$$

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Relation to the GSI-experiment: atom \rightarrow ion, photon \rightarrow neutrino

- if there is a splitting in the initial state, this can cause oscillations in the decay rate
- HOWEVER: splitting $\sim 10^{-15}$ eV \Rightarrow tiny, not at all explained...
- furthermore: preliminary data on β^+ -decays show no oscillatory behavior (Ivanov et al., 0905.1904)
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Outline

- 1 Introduction
- 2 Quantum Beats
- 3 One atom of type I
- 4 One atom of type II**
- 5 Two atoms of type II
- 6 Conclusions

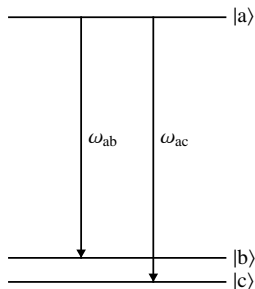
Single atom of type II

- superposition of $|a\rangle$, $|b\rangle$, and $|c\rangle$
- initially:
$$|\Psi(0)\rangle = \mathcal{A}_0|a\rangle|0\rangle_\gamma + \mathcal{B}_0|b\rangle|0\rangle_\gamma + \mathcal{C}_0|c\rangle|0\rangle_\gamma$$
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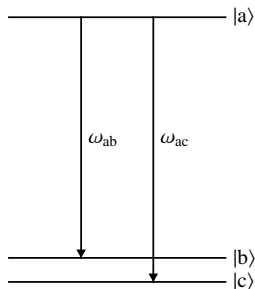


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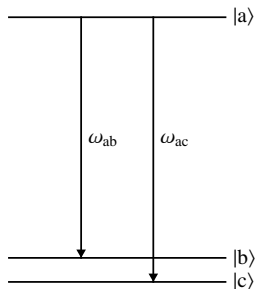
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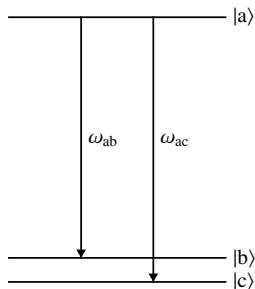
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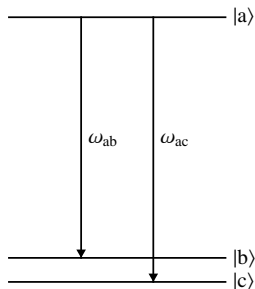


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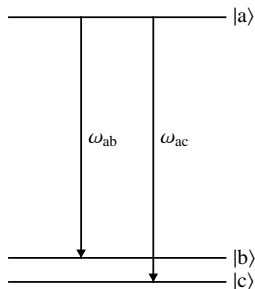
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⇒ No oscillatory terms left! ⇒ No Quantum Beats!

Intuitively:

By waiting long enough, one could determine the photon's energy by measuring the atomic final state. ⇒ No interferences expected!

Single atom of type II

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Intuitively:

By waiting long enough, one could determine the photon's energy by measuring the atomic final state. ⇒ No interferences expected!

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- 0-photon state with 1-photon state: e.g. $\mathcal{B}(t)^* \mathcal{B}'(t)$

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- the neutrino is not expected to interact before losing its coherence (estimates: $L_{\text{coh}} \lesssim 10^{19}$ m, mean free path $\sim 10^{40}$ m in the Galaxy)
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- 1 Introduction
- 2 Quantum Beats
- 3 One atom of type I
- 4 One atom of type II
- 5 Two atoms of type II**
- 6 Conclusions

Two atoms of type II

- if the spatial separation of the two atoms is smaller than the wavelength of the photon, one can write down a combined state:

$$\begin{aligned} |\Psi(0)\rangle = & \mathcal{A}_0|a\rangle_1|a\rangle_2|0\rangle_\gamma + \mathcal{B}_0|b\rangle_1|b\rangle_2|0\rangle_\gamma + \mathcal{C}_0|c\rangle_1|c\rangle_2|0\rangle_\gamma + \\ & + \mathcal{D}_{1,0}|a\rangle_1|b\rangle_2|0\rangle_\gamma + \mathcal{D}_{2,0}|b\rangle_1|a\rangle_2|0\rangle_\gamma + \mathcal{E}_{1,0}|a\rangle_1|c\rangle_2|0\rangle_\gamma + \\ & + \mathcal{E}_{2,0}|c\rangle_1|a\rangle_2|0\rangle_\gamma + \mathcal{F}_{1,0}|b\rangle_1|c\rangle_2|0\rangle_\gamma + \mathcal{F}_{2,0}|c\rangle_1|b\rangle_2|0\rangle_\gamma \end{aligned}$$

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- there can indeed be oscillatory terms, e.g. $\mathcal{J}_1^* \mathcal{K}_1 e^{-i\Delta t}$, which is proportional to:

$$\begin{aligned} \gamma \langle 1_{ab} | a_{ab}^\dagger a_{ac} | 1_{ac} \rangle_\gamma &= \gamma \langle 0 | a_{ab} a_{ab}^\dagger a_{ac} a_{ac}^\dagger | 0 \rangle_\gamma = \\ &= \gamma \langle 0 | (1 + \underbrace{a_{ab}^\dagger a_{ab}}_{0 \leftarrow}) (1 + a_{ac}^\dagger \underbrace{a_{ac}}_{\rightarrow 0}) | 0 \rangle_\gamma = \gamma \langle 0 | 0 \rangle_\gamma = 1 \end{aligned}$$

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 - \Rightarrow No way to measure the photon's frequency!
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Relation to the GSI-experiment: atom \rightarrow ion, photon \rightarrow neutrino

- even in runs where there was only one EC-decay, there might have been more ions in the ring \rightarrow this possibility has to be considered!
- the wavelength has to be replaced by the de Broglie wavelength of the neutrino
- Y. A. Litvinov et al., Phys. Lett. **B664**, 162 (2008), arXiv:0801.2079 \Rightarrow Q-value \sim 1 MeV
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→ If you have any idea...

- in principle, Quantum Beats seem to be a tempting possibility for an explanation for the GSI anomaly
- a single type I model would work, but has its problems
- a single type II model is claimed to be the solution by some authors, but actually it does not work
- a double type II model might be okay, but the numbers are wrong by orders
- a satisfying explanation is still missing...

→ If you have any idea...

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THANK YOU!!!