

# Decay asymmetries in $B \rightarrow K^* \ell^+ \ell^-$

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## 1. Introduction

## 2. QCD aspects

- “factorisable” vs. “non-factorisable”

## 3. Phenomenology

- forward-backward and isospin asymmetry

## 4. Conclusions

M. Beneke, TF, D. Seidel [NPB612, 25 (2001)]

TF, J. Matias [JHEP 0301:074 (2003)]



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- Exclusive decay modes:

[ → A. Ali's talk and references therein]

- ★ easier accessible in experiment
- ★ may provide complementary constraints on NP
- ★ test our understanding of QCD in exclusive decays

(spectator effects)



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- ★ photon/lepton-pair radiation through  $H_{\text{eff}}$ 
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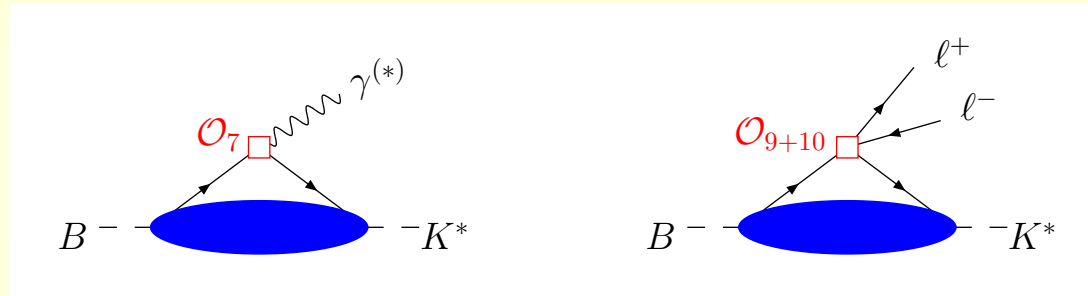
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- “non-factorisable” corrections:
  - ★ photon radiation from internal lines
    - contributions cannot be absorbed into  $B \rightarrow K^*$  form factors

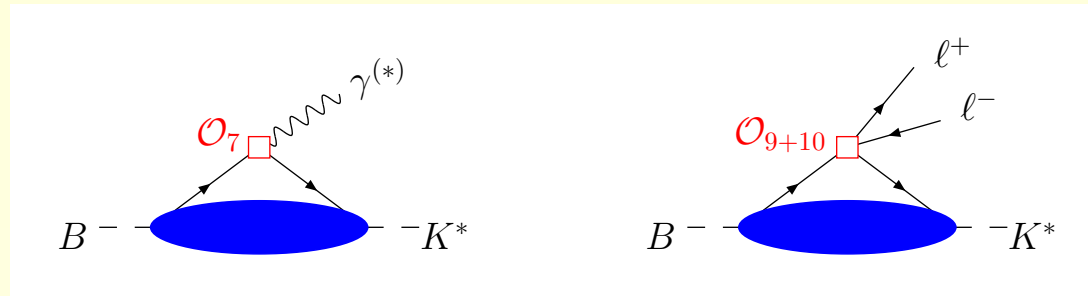


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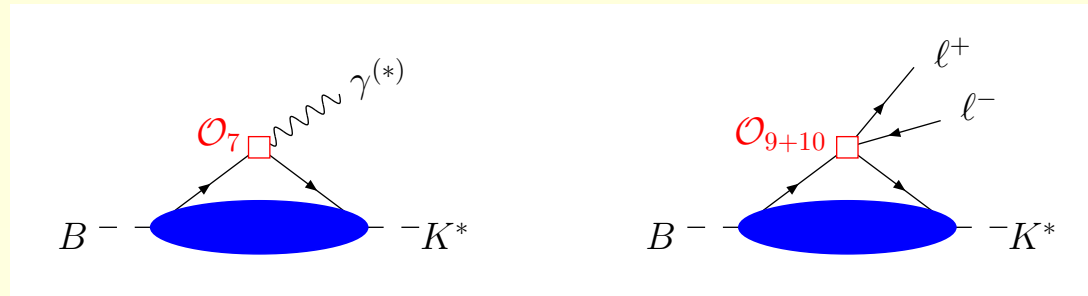


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- soft form factor relations at leading order in  $\alpha_s$  and  $1/m_b$

[Charles et al. 98]

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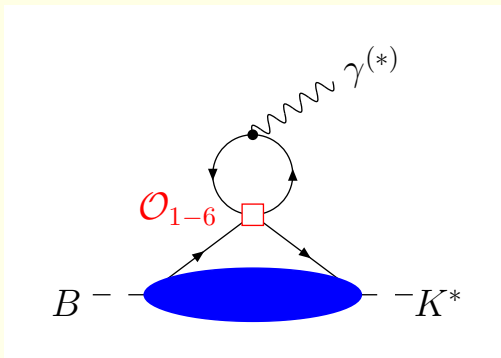
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Contributions from quark loops induced by  $\mathcal{O}_{1-6}$  absorbed into effective quantities  $C_7^{\text{eff}}, C_9^{\text{eff}}(q^2)$ .  
 Perturbative treatment of  $C_9^{\text{eff}}$  requires  $0 < q^2 < 4m_c^2$ .

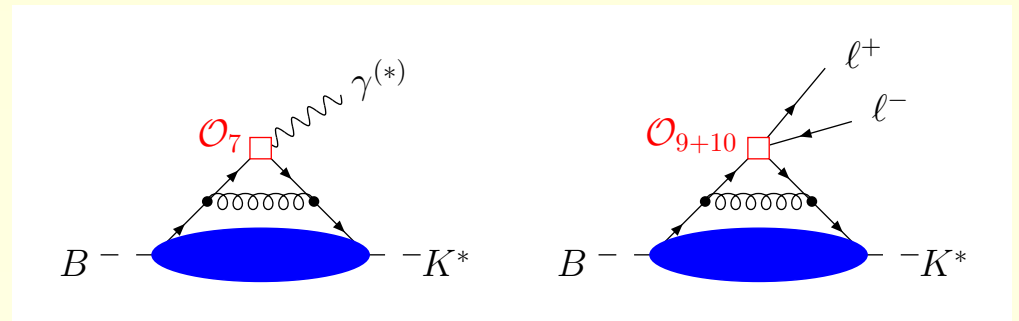
## (b) higher-order corrections to $b \rightarrow s$ transition

(i) “factorisable” vertex corrections

[Beneke/TF 2000]

⇒ scale-dependence of tensor form factors

⇒ multiplicative corrections to soft form factor relations

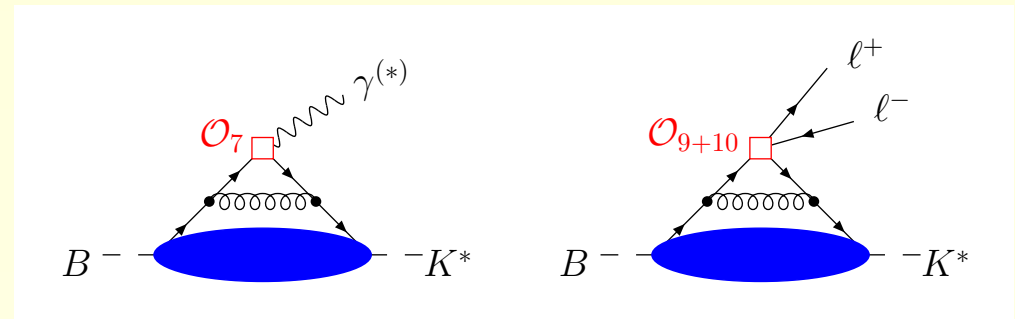


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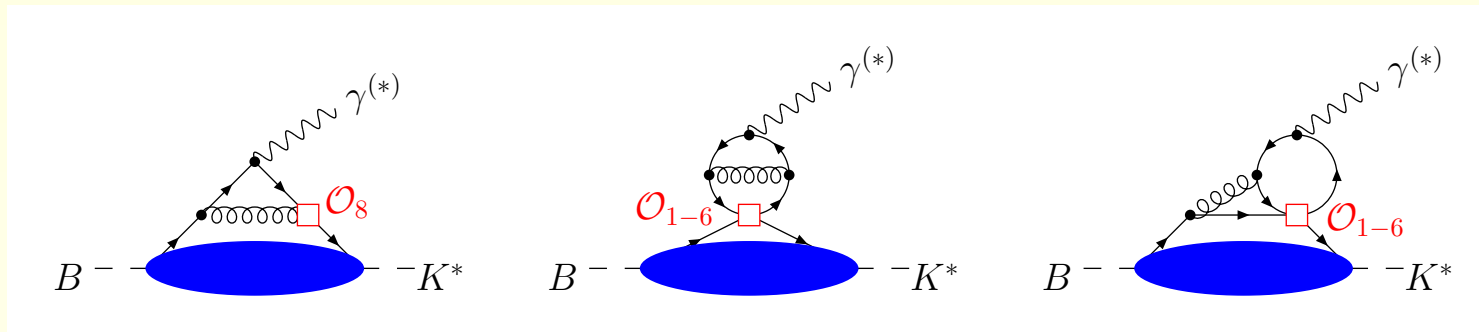
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(ii) “non-factorisable” contributions from hadronic operators



etc.

- calculated in context of inclusive  $b \rightarrow s \ell^+ \ell^-$  decays
- contributions from small penguin coefficients  $C_{3-6}$  neglected

$(q^2 \ll m_b^2)$

[Asatrian, Asatryan, Greub, Walker 01]

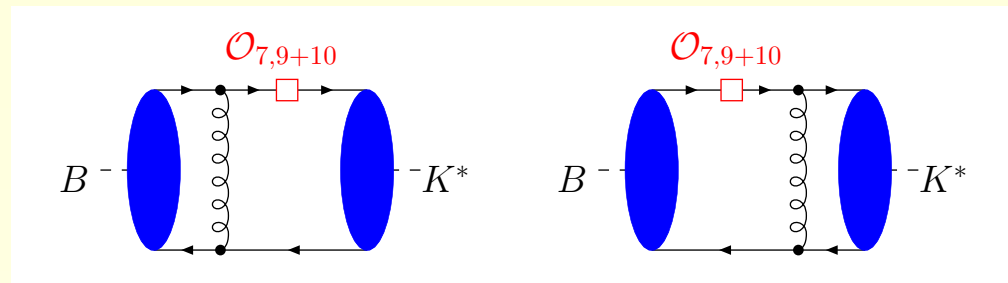


## (c) spectator interactions

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⇒ additive corrections to  
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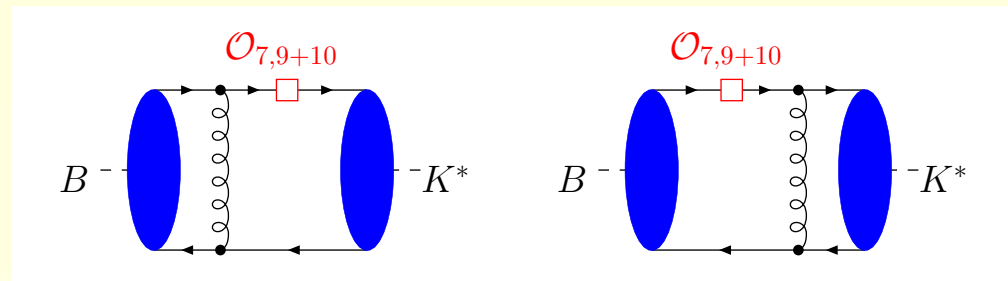


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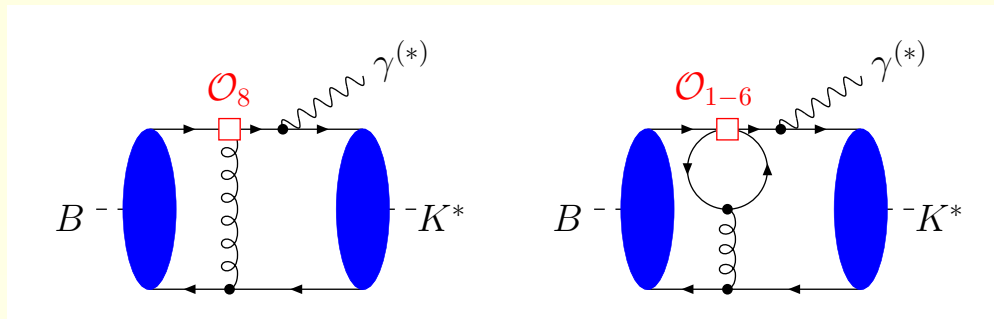
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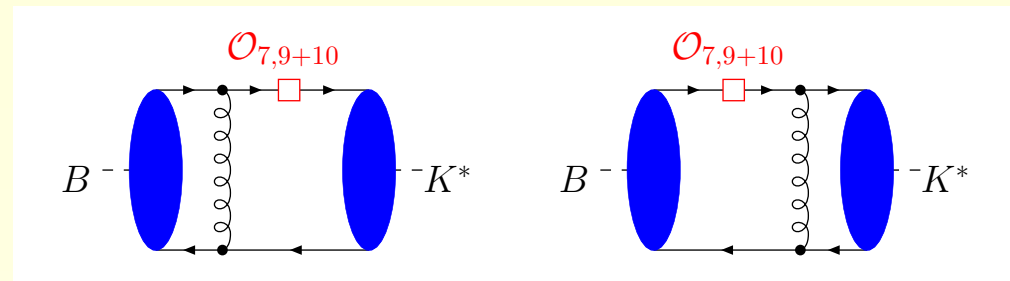
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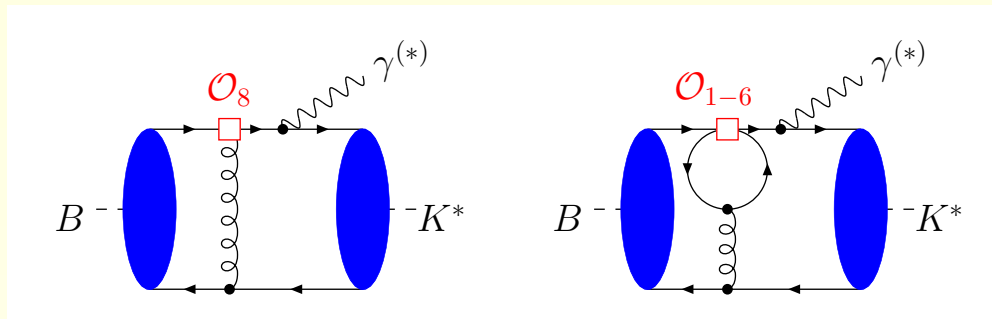
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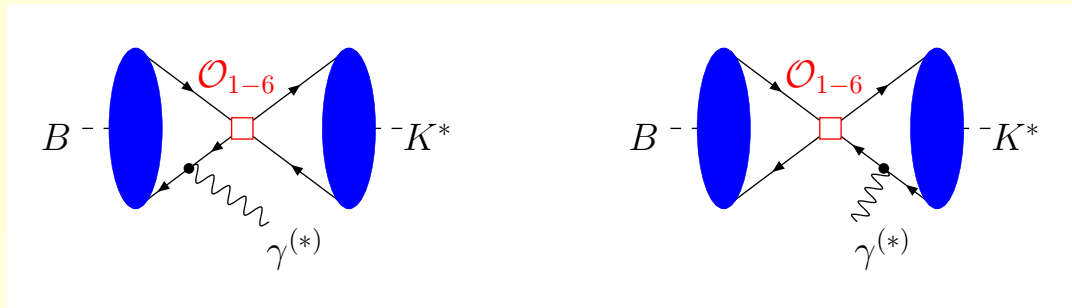


etc.

- leading contributions of  $1/m_b$  expansion calculable in terms of light-cone wave functions for  $B$  and  $K^*$  and perturbative hard-scattering kernels ( $q^2 \ll m_b^2$ )

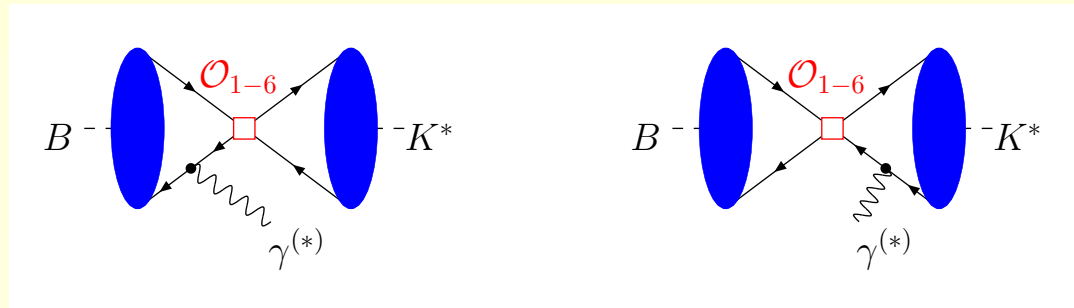


## (d) annihilation topologies (LO)



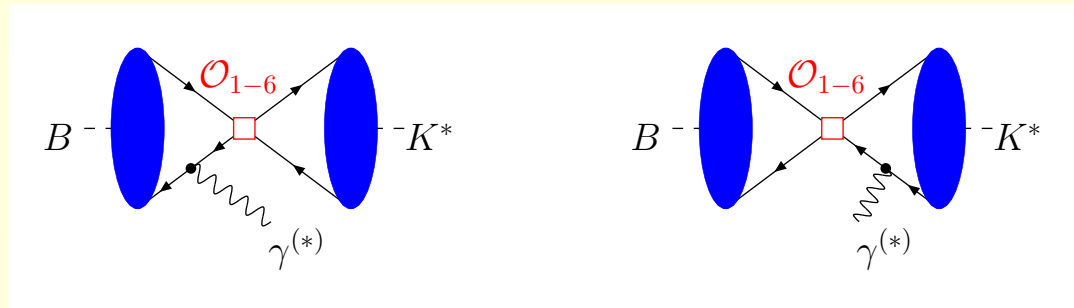
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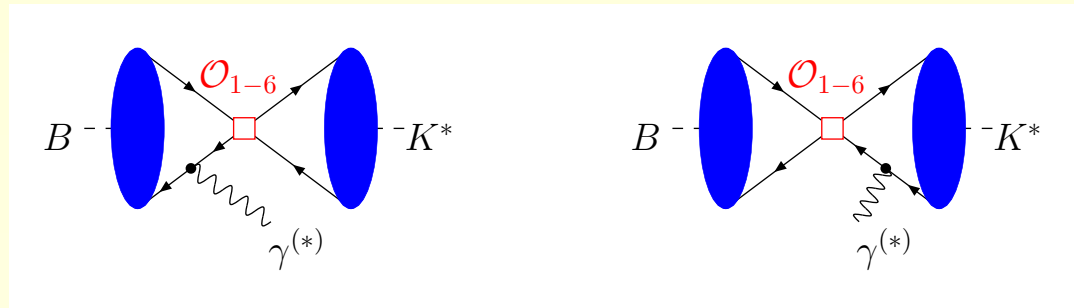
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- Sub-leading terms numerically important for  $B \rightarrow K^*$  isospin asymmetry!  
[Kagan/Neubert 01, TF/Matias 03]
- Radiative corrections and scale-dependence:
  - ★ interesting for theoretical considerations related to factorisation
  - ★ (at present level of accuracy) less important for  $B \rightarrow K^*$  phenomenology

## → Description of exclusive $b \rightarrow s$ decays beyond LO

- In the heavy quark limit decay amplitudes can be expressed in terms of
  - ★ soft form factors  $\xi_{\perp}(q^2)$ ,  $\xi_{\parallel}(q^2)$
  - ★ generalised “exclusive Wilson coefficients”

$$C_7 = C_7^{\text{eff}} + \text{“(b) + (c) + (d)”}$$

$$C_{9,\perp}(q^2) = C_9 + Y(q^2) + \frac{2m_b M_B}{q^2} C_7^{\text{eff}} + \text{“(b) + (c) + (d)”}$$

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- Inclusion of NLO terms reduces renormalisation scale-dependence

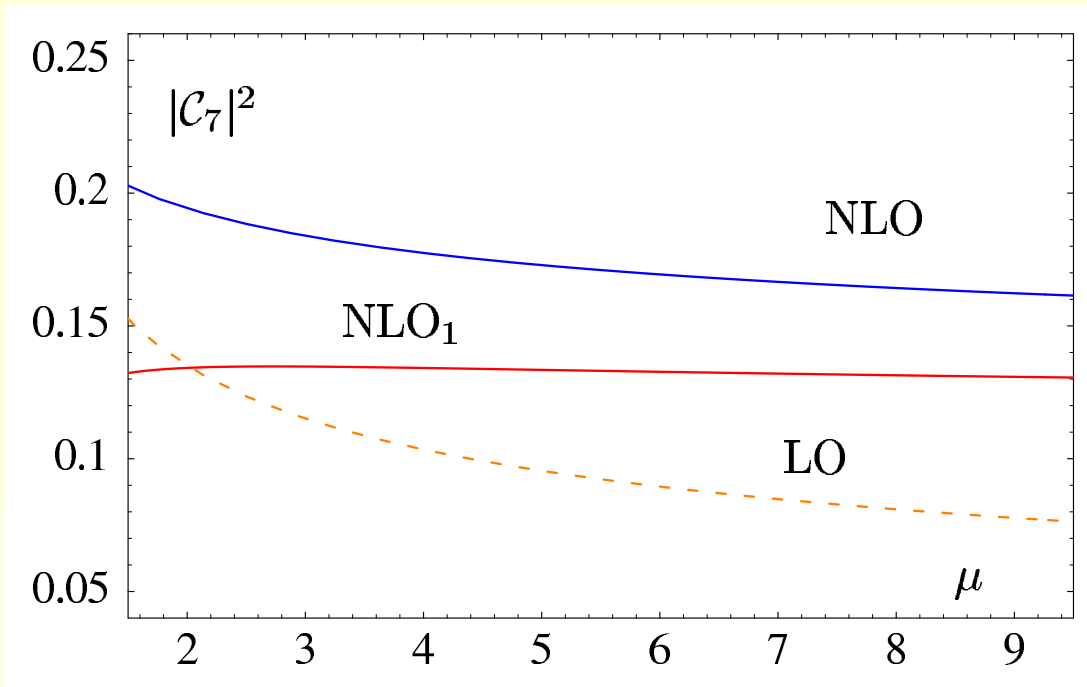
In our case:

$$\mu \frac{d}{d\mu} \{ m_b C_7, C_{9,\perp}, C_{9,\parallel} \} = \mathcal{O}(\alpha_s^2, \underline{\alpha_s C_{3-6}})$$

(unknown two-loop matrix elements of penguin operators, radiative corrections to annihilation effects in  $C_{9,\parallel}$ )



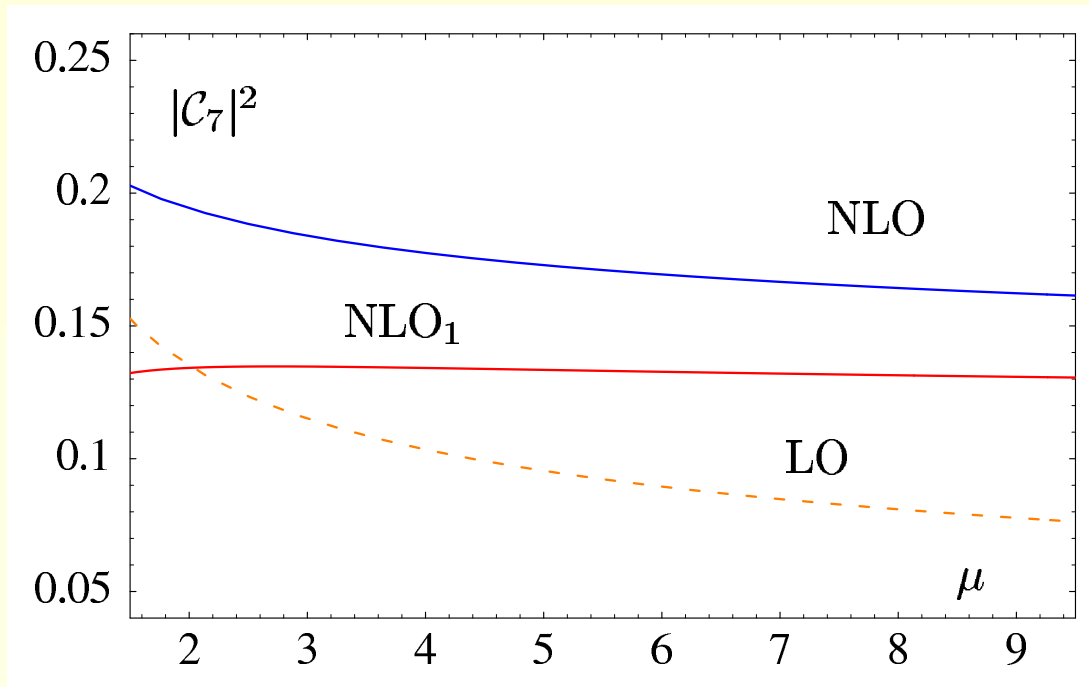
## Example: Scale-dependence of $|C_7|^2$



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[from Beneke/TF/Seidel 01]

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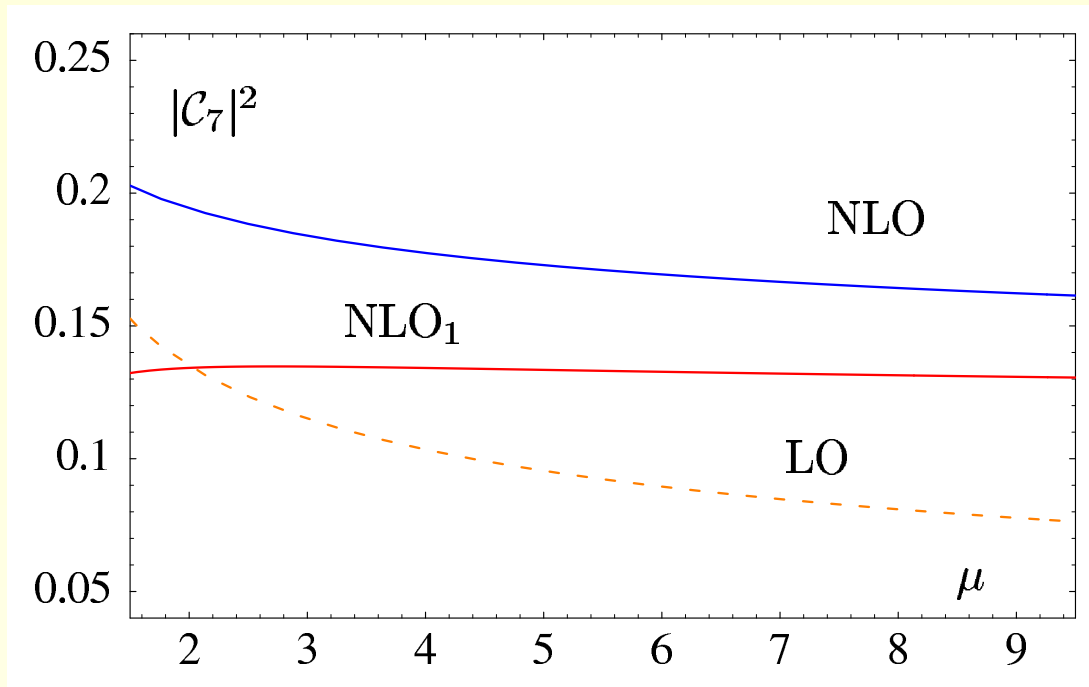


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- spectator effects only enter at NLO, related scale-dependence still sizeable

$$(\mu' = \sqrt{0.5 \text{ GeV} \cdot \mu})$$



## Including $1/m_b$ effects relevant for isospin asymmetry

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$b_q^\perp$  and  $b_q^\parallel$  determine size of  
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- Calculation of  $b_q^\perp$  requires inclusion of  $1/m_b$  effects

[Kagan/Neubert 01, TF/Matias 03]



### 3. Phenomenology

- SM and non-perturbative input parameters:

$M_W$	80.4 GeV	$f_B$	$180 \pm 30$ MeV
$\hat{m}_t(\hat{m}_t)$	$167 \pm 5$ GeV	$\lambda_{B,+}^{-1}$	$(3 \pm 1)$ GeV <sup>-1</sup>
$ V_{ts} $	$0.041 \pm 0.003$	$f_{K^*,\perp}(1 \text{ GeV})$	$185 \pm 10$ MeV
$\alpha_{\text{em}}$	1/137	$f_{K^*,\parallel}$	$225 \pm 30$ MeV
$\Lambda_{\text{QCD}}^{(n_f=5)}$	$220 \pm 40$ MeV	$a_1(K^*)_{\perp,\parallel}$	$0.2 \pm 0.1$
$m_{b,\text{PS}}(2 \text{ GeV})$	$4.6 \pm 0.1$ GeV	$a_2(K^*)_{\perp,\parallel}$	$0.05 \pm 0.1$
$m_c$	$1.4 \pm 0.2$ GeV	$M_B \xi_{\parallel}(0)/(2m_{K^*})$	$0.47 \pm 0.09$
		$\xi_{\perp}(0)$	$0.35 \pm 0.07$

from [Beneke/TF/Seidel 01]

- variation of renormalisation scales:

$$m_b/2 < \mu < 2m_b, \quad \mu' = \sqrt{0.5 \text{ GeV} \cdot \mu}$$

- remaining systematic uncertainty: neglect of  $1/m_b$  effects (model-dependent)



### 3.1 Forward-backward asymmetry

$$\begin{aligned} \frac{dA_{\text{FB}}}{dq^2} &\equiv \frac{1}{d\Gamma/dq^2} \left\{ \int_0^1 d(\cos \theta) - \int_{-1}^0 d(\cos \theta) \right\} \frac{d^2\Gamma[B \rightarrow K^* \ell^+ \ell^-]}{dq^2 d \cos \theta} \\ &\propto \text{Re} [C_{9,\perp}(q^2)] \end{aligned}$$

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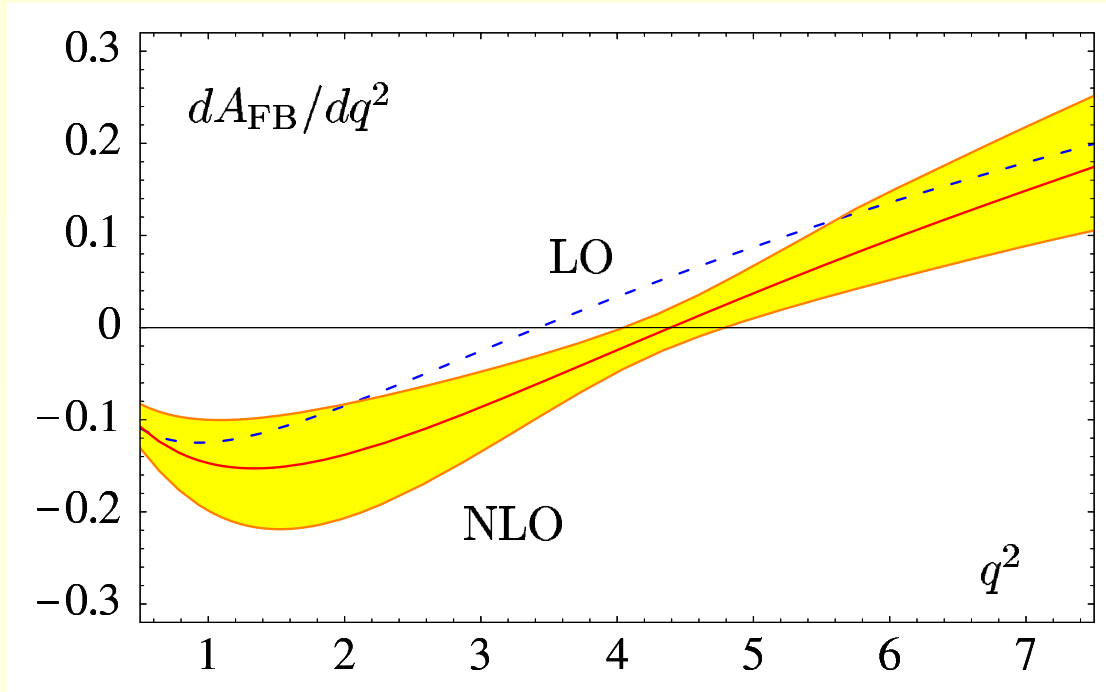
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- Leading-order in  $1/m_b$  and  $\alpha_s$ : 
$$C_9 + \text{Re}(Y(q_0^2)) = -\frac{2M_B m_b}{q_0^2} C_7^{\text{eff}} .$$

- ★ free of hadronic uncertainties (consequence of soft form factor relations) [Burdman 98]
- ★ perturbative corrections are calculable  $\longrightarrow$  precise test of the SM [Beneke/TF/Seidel 01]

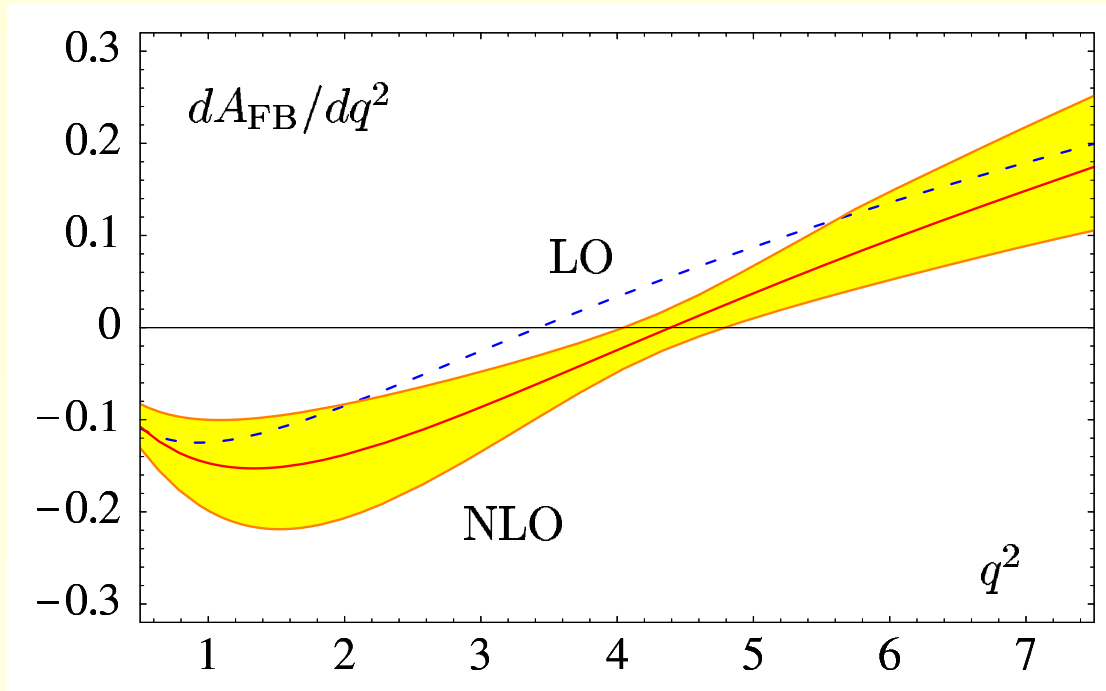


## Forward-backward asymmetry (SM)



[from Beneke/TF/Seidel 01]

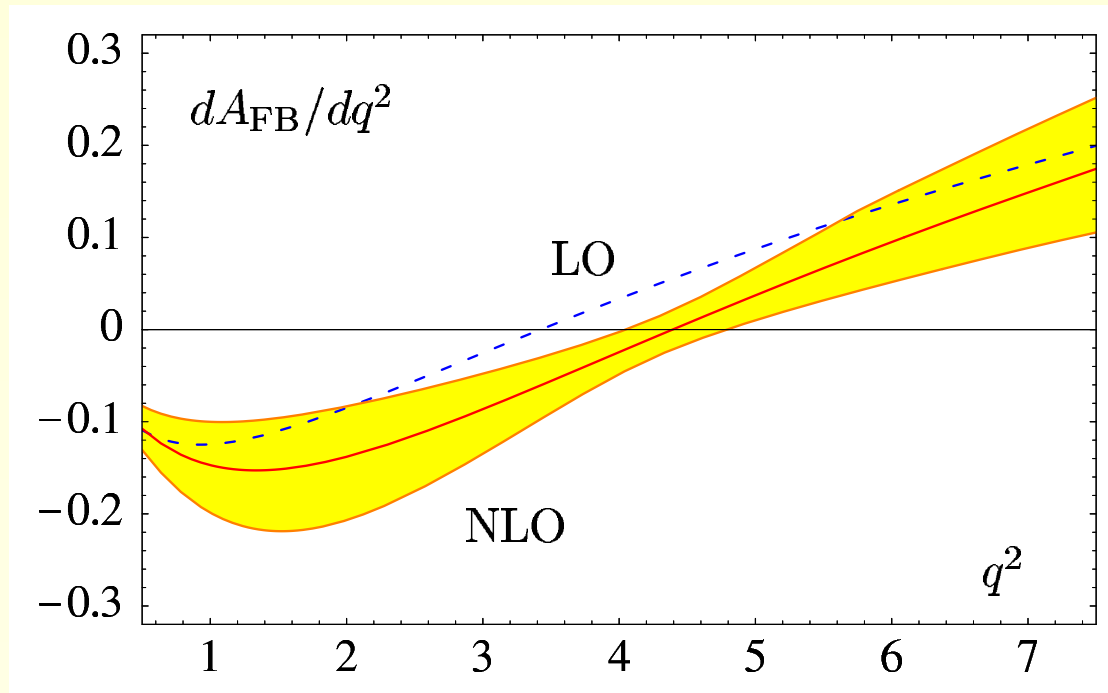
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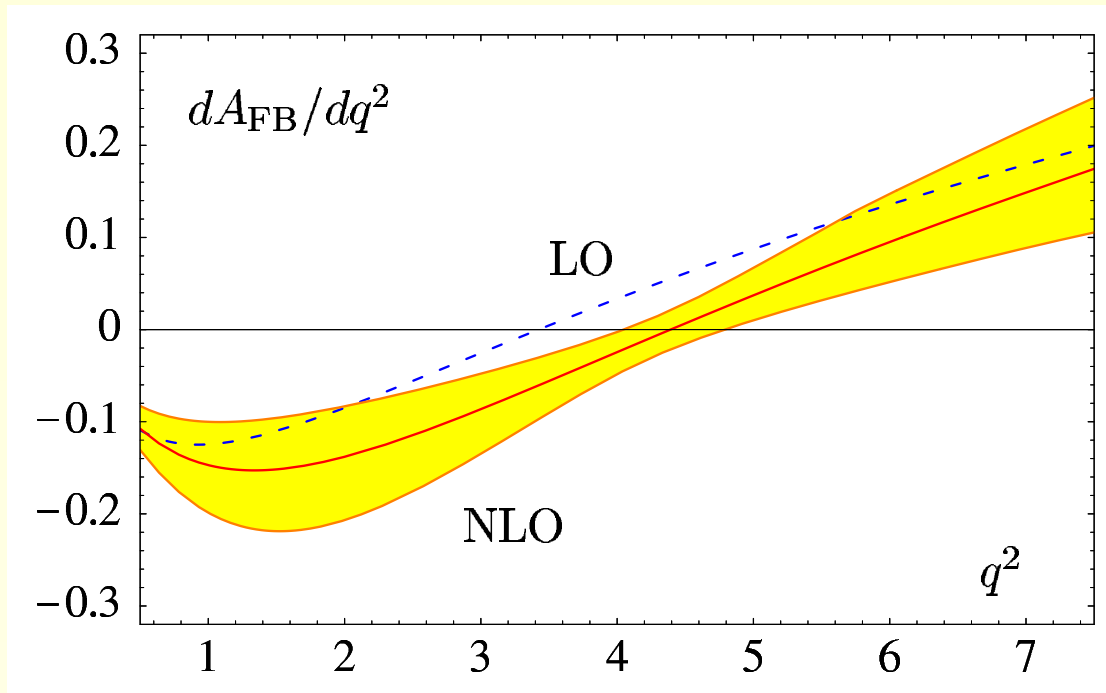
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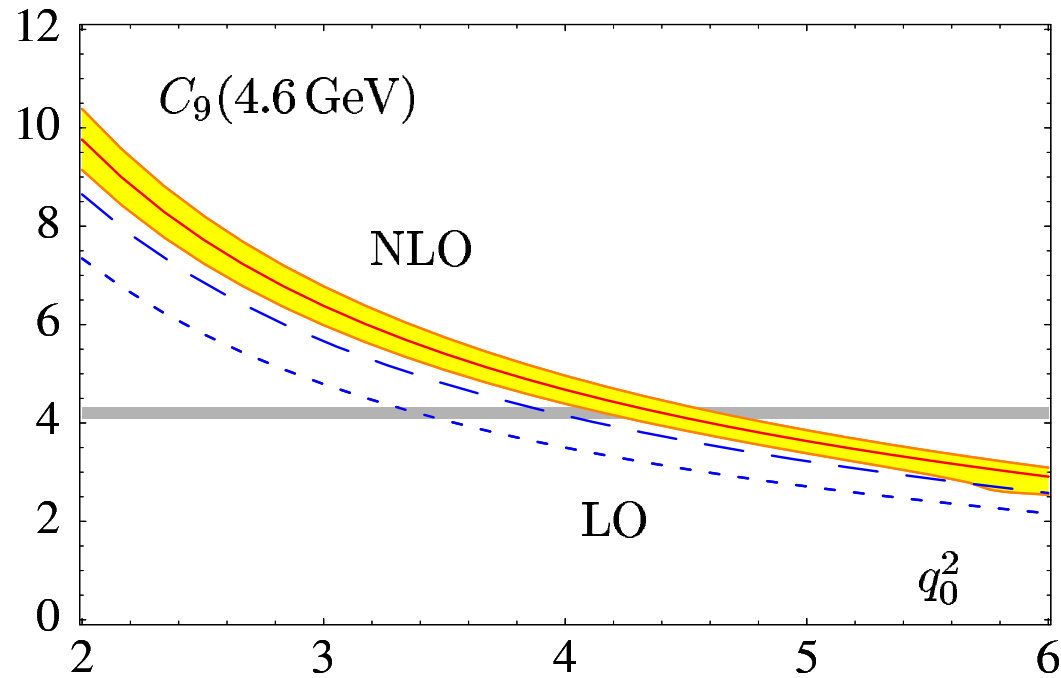


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- reduction of hadronic uncertainties around  $q_0^2$  due to form factor relations



## $C_9$ from FB asymmetry



[from Beneke/TF/Seidel 01]

Test of Wilson coefficient  $C_9(m_b)$  with  $\sim 10\%$  theoretical accuracy!



## 3.2 Isospin asymmetry

$$\frac{dA_I}{dq^2} \equiv \frac{d\Gamma[B^0 \rightarrow K^{*0}\ell^+\ell^-]/dq^2 - d\Gamma[B^\pm \rightarrow K^{*\pm}\ell^+\ell^-]/dq^2}{d\Gamma[B^0 \rightarrow K^{*0}\ell^+\ell^-]/dq^2 + d\Gamma[B^\pm \rightarrow K^{*\pm}\ell^+\ell^-]/dq^2}$$

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- Isospin asymmetry vanishes in “naive factorisation”

## 3.2 Isospin asymmetry

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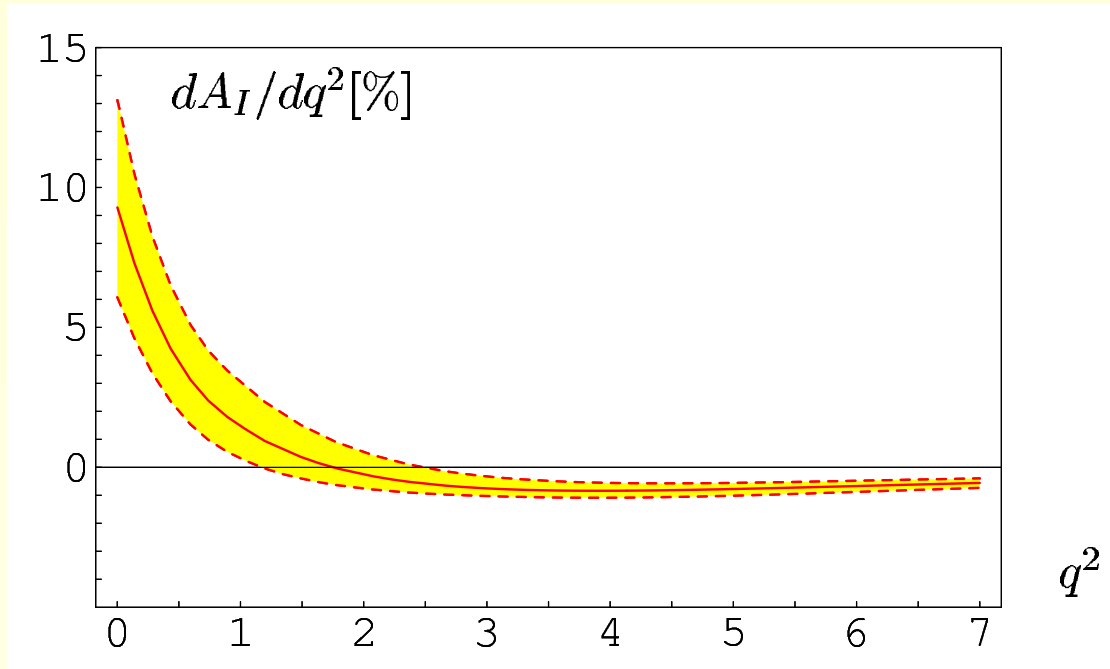
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Test of four-quark penguin-coefficients

(basis defined in Buchalla/Buras/Lautenbacher)

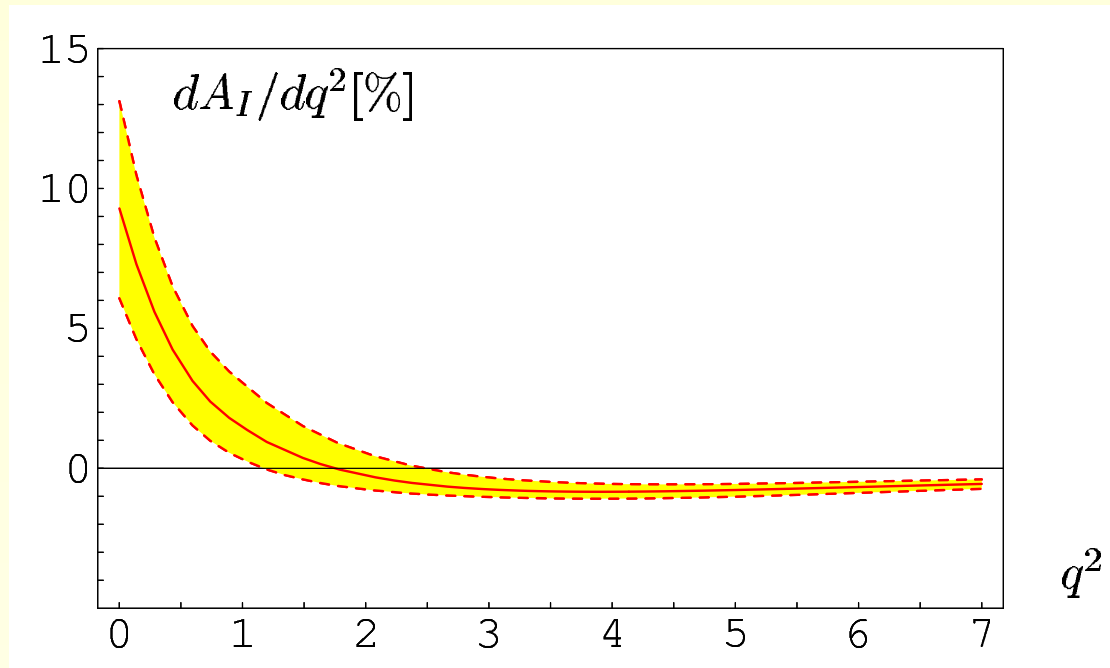


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[from TF/Matias 03]

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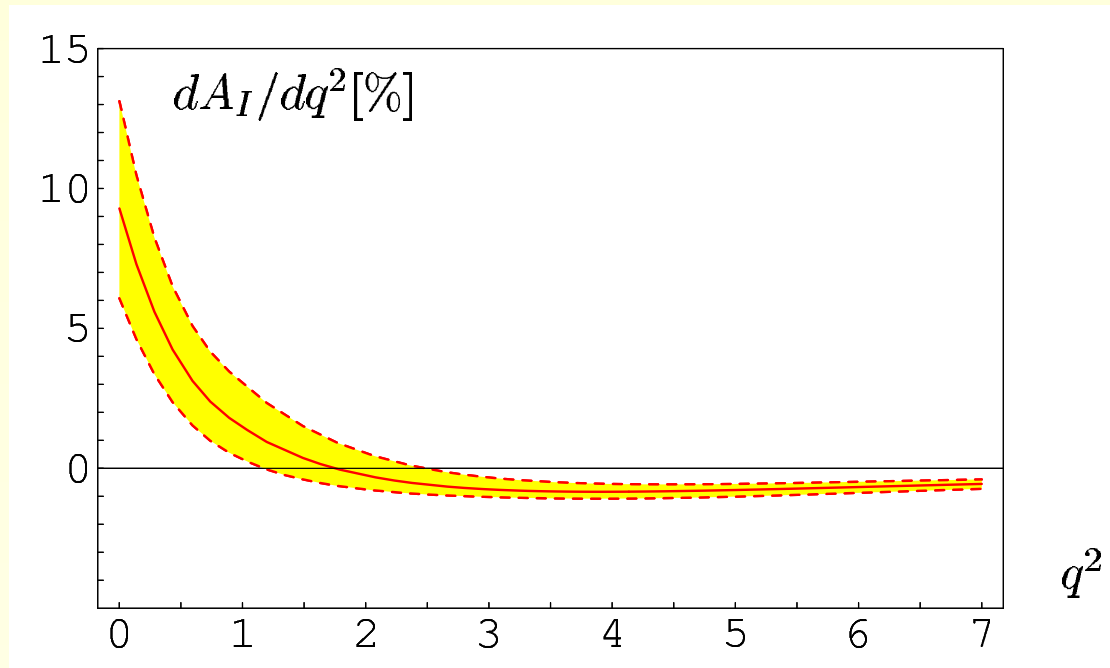
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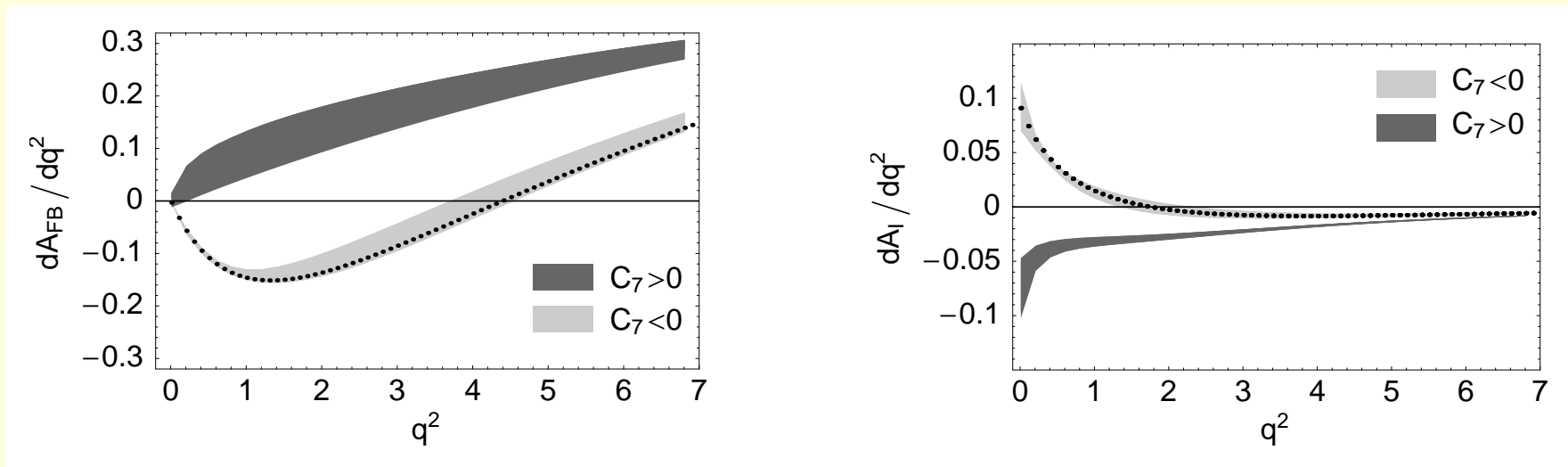
- isospin asymmetry decreases with  $q^2$  and changes sign around  $q^2 \simeq 2 \text{ GeV}^2$



### 3.3 Asymmetries in constrained MSSM model

illustration of new physics effects

(for model set-up see [TF/Matias 03])

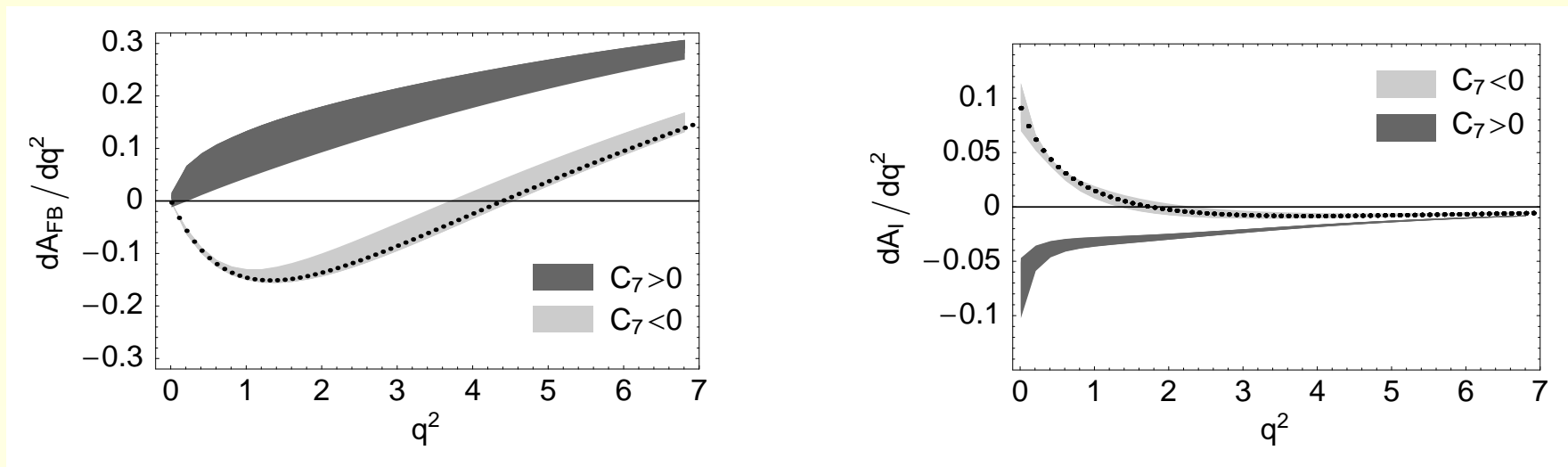


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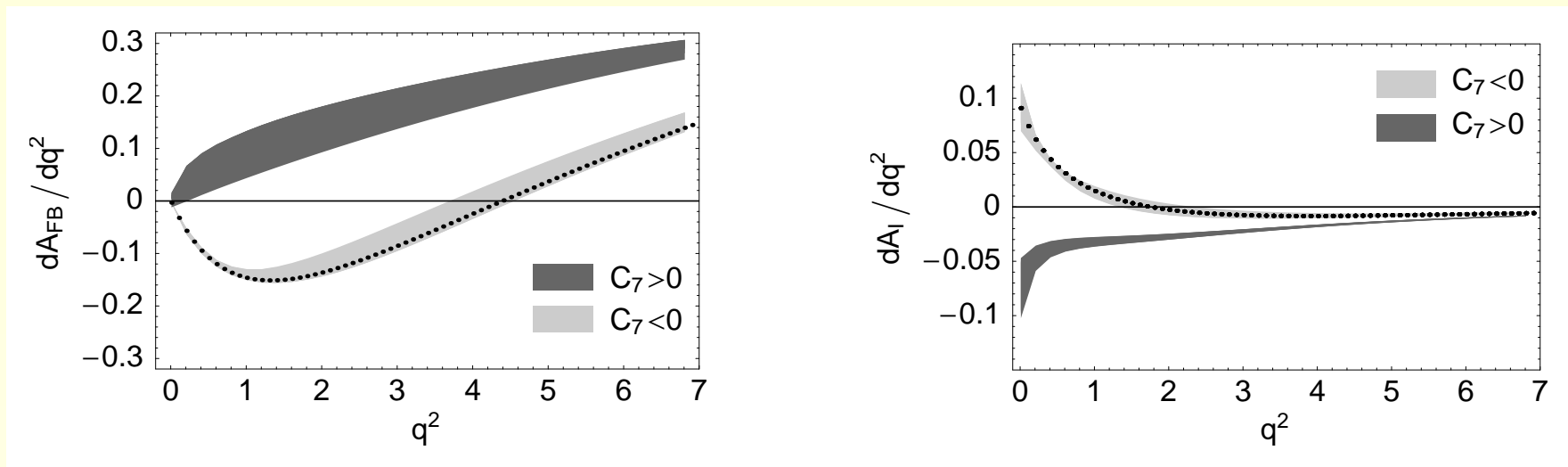


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- Parameter spread **within** one band indistinguishable from theoretical uncertainties
- Sensitivity to penguin operators  $C_{3-6}$  may be more important in models beyond MSSM with extended operator basis etc.



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- not discussed:  $CP$  asymmetry (generically small in SM + QCD factorisation)



*“that’s all, folks . . . ”*